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## COMMERCIAL ARITHMETIC AND ACCOUNTS

PART1I

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# COMMERCIAL ARITHMETIC AND ACCOUNTS 

BY

A. RISDON PALMER, b.Sc, b.A.<br>HEAD OF THL PROFESSIONAL SIDE THL POLYIECHNIC RTGENT STREF:<br>LONDON, W<br>IDIIOR OF 'HOBBS' ARITHMEIIC OF EILCTRICAL MLASURLMENTS' EIC

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## PARTII



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## PREFACE

The present treatise on Commercial Arithmetic and Accounts has been written not only to meet the needs of that great and ever-increasing army of students which is receiving a thorough commercial training in our modern schools and colleges before entering on a business career, but also to provide for every one, who has to earn and invest money and discharge with it the everyday duties of a citizen, a comprehensive, interesting, and simply expressed exposition of the fundamental principles upon which the financial progress of the individual, of the urban community, and of the Empire depend.

It is becoming increasingly evident that purely arbitrary methods have to be abandoned, and that students must enter commercial life well equipped with a knowledge of the principles on which their calculations will depend, and endowed with the power of applying those principles. The changes and modifications in methods of calculation are so frequent and subtle that only students who have had a sound mathematical education are able to cope with the exigencies that continually arise in modern mercantile transactions. The day of the man who can do no more than "look up the tables" is past.

While endeavouring first and foremost to train the student for his future commercial work, we have yet kept in view throughout the requirements of various examinations, e.g. those of the Union of Institutes of Lancashire and Cheshire, the Society of Arts, etc. In each section of the book the fundamental principles are carefully explained, and copious "drill" examples are set to ensure that the student has thoroughly mastered them; following immediately on these "drill" examples are "applicational" examples, drawn for the most part from actual commercial transactions, and not evolved ex cathedra; the methods given being, as far as possible, in accordance with the recommendations of the Mathematical Association. No mention is made, e.g., of "recurring decimals," as they are of academic
interest and not of commercial importance. On the other hand, "rough checks," "rough estimates," and the degree of accuracy to which a decimal should be taken receive careful attention throughout the work, and are illustrated by a large number of concrete examples. ${ }^{1}$

In order to make the book commercial in spirit an attempt has been made to present, in perspective, the commerce of the British Enpire, and on almost every page appear facts relating to the Colonies or Dependencies which have been linked up with the Mother Country, with one another, and with foreign comntries by means of trade relationships. Among the latter, considerable prominence has been given to Russia, France, and Brazil.

In many cases it has seemed desirable to translate into English parts of records published in foreign languages, so as to place the most recent data at the disposal of the student, and, in addition, rather more than a thousand authorities in the various departments of commerce have given information which has proved invaluable to us.

We may quote the following as instances of the predagogic method and spirit of the book:-

After the Metric System has been taught (Section XI.), its important bearing upon commerce is never again lost sight of. Mensuration is dealt with in Sections XII. to XIV., and we hope that some pleasure may be derived from learning it through its applications to commerce. The diagrams, many of which are original, the facsimile documents, and the coloured plates may prove useful in making difficult points clear, while the method of presentation in Section XIX. will, we hope, contribute to the simplification of the important subject of Double Entry in Accounts.

The Coloured Industrial Map will probably be found valuable

[^0]if it is kept constantly open for reference as the examples are being worked.

The pleasure of paying a tribute to those who have so generously and willingly helped us is, indeed, very great.

We owe to Dr. W. P. Milne our sincerest thanks, not only for placing his wide experience at our disposal, but also for the constructive criticism which he has brought to bear upon the book.

Our acknowledgments are also due to the ofticial representatives of Foreign Governments (attached specially to Commerce) accredited to this country, to the High Commissioners of the Colonies, and to some Government Departments at home, who have either lent (or given) us books which would otherwise have been inaccessible.

Mr. Gordon Groom, B.Sc., has rendered us invaluable assistance in working the examples, and we are also indehted to Mr. G. F. New, B.Sc., for help in this connection.

Our thanks are also due to the Controller of His Majesty's Stationcry Office for permission to reproduce the War Loan Voucher and the Inland Money Order Form ; to the Great Northern Railway Company for authorising the reproduction of their Goods Consignment Note ; to the United Kingdom Temperance and General Provident Institution for similar permission in regard to the Insurance Policy; and to the Board of Trade, whose publications we have consulted.
A. R. P.
J. S.

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## PARTII



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## PAR'T II

SECTION XIV

## VOLUMES ${ }^{1}$

## A. Rectangular Objects

## EXAMPLES. LIII.

Experiment 1.-Take a piece of stiff squared paper, draw upon it, and then cut out from it a figure such as is shown in the diagram. Each of the lines $A B, B C, B D, B E, D F$ is 1 inch long. The paper is folded along the dotted lines shown, and the shaded parts allow one side of the cube formed to be stuck to the adjacent side. Thoroughly varnish the cube inside and out, and, if necessary, stop any small holes there may be with melted paraffin wax-" candle grease "if you like.


1. How many external surfaces has a cube (1) open at the top, (2) closed at the top (i.e. "covered in")?
2. How many edges has a cube (1) open at the top, (2) closed at the top?
3. Tabulate the number of edges and surfaces of the following objects: (1) A closed rectangular biscuit box, (2) the top of a counter, (3) a plain wooden door to an outhouse, (4) a covered box of sugar, (5) a pound packet of tea, (6) a sandwich loaf, (7) a jelly "square," (8) a closed box of kippers, (9) a closed handkerchief box, (10) a portmanteau, (11) an egg box, (12) a square of plate glass, (13) a jewel case, (14) a centimetre scale, (15) a lump
${ }^{1}$ Some practical questions will be found in this section, many of which can be performed by the students themselves or, if it is thought more desirable, by the teacher.
of sugar, (16) a penny, (17) a "round" cocoa tin, (18) a football, (19) a solid iron bar, circular in section, (20) a cask, (21) a weather cone, (22) a goal-post, (23) a drum of pitch, (24) a glass tumbler.

| Object. | Number of <br> Edges. | Number of <br> Surfaces. |
| :---: | :---: | :---: |
| (1) A closed rectangular biscuit box |  |  |

4. From the results of the last question, parts 1 to 15 , state how many edges and how many surfaces there are in an ohject bounded by plane surfaces and having all its angles right angles.
5. Employing the results of Question 3, parts 15 to 24, fill in a table, giving in column 1 the names of the following objects: a sphere, a closed cylinder, a cylinder open at the top, and a closed cone; in column 2, the number of surfaces; and in column 3, the number of edges which each object has.
6. A covered cattle truck is to be entirely whitewashed inside, and painted outside except for the lower side of the floor. How many surfaces have to be whitewashed and how many painted 9
7. What is the length of all the edges of a (rectangular) biscuit tin if each edge is 9 inches long?
8. What is the outside surface area of the tin referred to in the last question, presuming it to be covered?
9. What is the outside surface area of a refrigerator which is 3 ft . by 2 ft . by 2 ft .? (i.e. it is 3 ft . long, 2 ft . wide, and 2 ft . deep.)
10. What would it cost to gild the sides and top of an ornamental rectangular handkerchief box, 18 cm . long, 12 cm . wide, and 3.5 cm . deep, at a cost of 1 franc for $8 \mathrm{sq} . \mathrm{cm}$. ?
11. A Sheraton china cabinet is 2 m . high, 2.25 m . wide, and 0.8 m . deep; find the cost of glazing the sides and front at 1 mark 20 pf. per $250 \mathrm{sq} . \mathrm{cm}$.
12. A box which contains Tasmanian apples is nailed parallel to its edges with five nails along the vertical sides, eight along each of the longer edges top and bottom, and six along each of the shorter edges top and bottom. Draw a diagram showing the method of nailing, and find how many nails are required for each box.

Experiment 2.-Make a cube exactly the same as in Experiment 1, but with its edges 1 cm . long, and, after having allowed it to dry thoroughly for forty-eight hours, fill up the

1 in . cube with water, using the centimetre cube as the measure, and so find how many cubic centimetres make 1 cubic inch. ${ }^{1}$

Experiment 3.-Employ the inch or centimetre cube and the measure stated to write down the following:
(1) The number of cubic inches in 1 pint, and (2) in 1 litre.
(3) , , cubic centimetres ,, 1 litre, ,, (4) ,, 1 pint.
(5) Express the volume of a $\frac{1}{2}$-pint tumbler in cubic inches.
(6) ", ", cubic centimetres.
13. From the results of parts 5 and 6 of the last question, find roughly (1) the decimal of a cubic inch which is equal in volume to a cubic centimetre, and (2) the decimal by which any number of cubic centimetres must be multiplied to give their volume in cubic inches.

Experiment 4.-Find the number of cubic inches of sand necessary to fill vessels, which should be made in cardboard to the dimensions given, ${ }^{2}$ using the inch cube as a measure: (1) A cube of 2 in . edge ; (2) a cube 3 in . edge; (3) a vessel 2 in . long, 1 in. high, 1 in . wide ; (4) 3 in . long, 2 in . high, 2 in . wide ; (5) $3 \frac{1}{2} \mathrm{in}$. long, $2 \frac{1}{2} \mathrm{in}$. high, 2 in . wide.
14. Tabulate the results of Experiment $4^{3}$ as follows:

| No. of Question. | Dimensions of Vessel. | No. of Cubic Inches of Sand required to fill the Vessel. | Product of the Dimensions. |
| :---: | :---: | :---: | :---: |
| (1) . . | $2^{\prime \prime} \times 2^{\prime \prime} \times 2^{\prime \prime}$ |  |  |
| (2) • • | $3^{\prime \prime} \times 3^{\prime \prime} \times 3^{\prime \prime}$ $2^{\prime \prime} \times 1^{\prime \prime} \times 1^{\prime \prime}$ |  |  |
| $\left(\begin{array}{l}\text { (3) } \\ (4)\end{array}\right.$ | $\begin{aligned} & 2^{\prime \prime} \times 1^{\prime \prime} \times 1^{\prime \prime \prime} \\ & 3^{\prime \prime} \times 2^{\prime \prime} \times 2^{\prime \prime} \end{aligned}$ |  |  |
| (5) | $3 \frac{1}{2 \prime}^{\prime \prime} \times 2 \frac{1}{2 \prime}^{\prime \prime} \times 2^{\prime \prime}$ |  |  |

15. Make a statement concerning the number of cubic inches which the vessel contains and the product of the three dimensions, and so state a rule for finding the volume of a rectangular vessel.
16. What difference is there between the volume of the sand

[^1]and the number of cubic inches obtained by multiplying the area of the base of each of the rectangular vessels by its height?

200 We now summarise the results of our practical work:
The volume of a rectangular vessel is the product of its length, breadth, and depth;

$$
\text { or } V=I \times b \times d ;
$$

$$
\text { or volume }=\text { area of base } \times \text { depth or height } .
$$

The latter rule applies to all solids which are of uniform section, e.g. a cube, a triangular or any other prism, or a cylinder, but not to a cone or to a pyramid (see $\$ 201$ ).

It is easy to prove this relationship geometrically, thus: the figure represents a rectangular vessel 3 in . by 1 in. by 2 in . The base contains 3 square inches, and the
 total number of cubic inches is found, by counting, to be 6 cubic inches. Hence

$$
\begin{aligned}
\mathrm{V} & =l \times h \times d=3 \times 1 \times 2=6 \quad \text { cub. in., } \\
\text { or, } \mathrm{V} & =\text { area of base } \times \text { height } \\
& =3 \times 2 \text { cubic inches }=6 \text { cub. in. }
\end{aligned}
$$

A number of students should draw vessels with sides of very different lengths and so convince themselves of the truth of the rule.
201. We collect here for convenience a number of useful relationships for areas and volumes:

| Areas. | Volumes. |
| :---: | :---: |
| Rectangle . . Length $\times$ breadth. | RectangularLength $\times$ breadth $x$ <br> height. |
| Parallelogram . Base $\times$ perpendicular dis. tance between base and opposite side. | Any prism . . Sectional area $\times$ height. |
| Triangle . . . Base $\times$ height +2. |  |
| Trapezium . . Average length of the two parallel sides $\times$ perpendicular distance between them. |  |
| Circle . - . $\pi r^{2}$. |  |
| Ellipse . . . $\frac{\pi}{4} \times$ product of length of |  |
| Curved surface Circumference or periof cylinder ${ }^{1}$ meter $x$ height. | Cylinder . . . Area of base $\times$ height $=\pi r^{2} \times h$. |
| Ourved surface Circumiference of basex of cone slant height $\div 2$. | Cone . . . . Area of basexvertical height +8 . |
| Curved surface $4 \pi r^{2}$. of sphere | Sphere . . . $\frac{4 \pi r^{8}}{8}$. |

[^2]202. Example.-Determine the volume of a case, the internal dimensions of which are 4 ft .6 in . long, $1 \frac{1}{4} \mathrm{yd}$. wide, and 36 in deep.
\[

$$
\begin{aligned}
\text { Volume } & =l \times b \times d . \\
& =4.5 \mathrm{ft.} \times 3.75 \mathrm{ft} . \times 3 \mathrm{ft} . \\
& =50.625 \text { cub. } \mathrm{ft.} \\
& =50 \text { cub. } \mathrm{ft} .108 \text { cub. in., to the nearest cubic inch. }
\end{aligned}
$$
\]

## EXAMPLES. LIV.

1. The dimensions given are the length, width, and depth of rectangular vessels. Write down their volumes in the units named. ${ }^{1}$
(1) 3 yds . by 2 ft . by 4 ft ., in cubic feet.
(2) 56 cm . by 30 cm . by 10 cm ., in cubic centimetres.
(3) 3 m . by 40 cm . by 65 cm ., in cubic metres.
(4) 4 yds. by 5 ft . by 18 in ., in cubic feet.
(5) $2 \frac{1}{2}$ yds. by $4 \frac{1}{2}$ yds. by 3 yds., in cubic yards.
2. What is the volume of a packet of tea 4 in . by $2 \frac{1}{2} \mathrm{in}$. by 2 in. $?$
3. What is the volume in cubic centimetres of the packet of tea referred to in Question 2 ? ( 1 inch $=2.54 \mathrm{~cm}$.)
4. A paving brick is 9 in . by $4 \frac{1}{2} \mathrm{in}$. by $1 \frac{3}{4} \mathrm{in}$. ; find its volume in cubic inches.
5. What is the volume of a bag of flour 10 in . by $6 \frac{1}{2} \mathrm{in}$. by $2 \frac{1}{4} \mathrm{in}$. 3
6. Express the volume of a tank, 3 ft . 6 in . by 4 ft . by 2 ft . 6 in ., in cubic feet.
7. What weight of water would the tank in the last question contain? (l cubic foot of water weighs 62.3 lb .)
8. Find the volume of a trough 1.88 m . long, 0.75 m . wide, 0.12 m . deep, giving the result in cubic metres.
9. How many litres of water would the trough in the last question contain?
10. How many cubic inches are there in a box which is 16 in. long, $12 \frac{1}{2} \mathrm{in}$. wide, and 8 in . high ?

[^3]11. The length of a laundry basket is 2 ft .6 in ., and the ratio of the length to the width is as 2 is to 1 , while the depth is 1 ft .3 in . Find its volume.
12. What would have been the volume in the last question if the ratio of the length to the width had been as 5 is to 3 , the depth being 1 ft .4 in .?
13. Compare the volume of a trough 3 ft .3 in . by 2 ft .6 in . by 8 in . with that of another trough 1 m .25 cm . by 95 cm . by $15 \mathrm{~cm} . \quad(2 \cdot 54 \mathrm{~cm} .=1$ inch. $)$
14. A jewel case, 10 in . by 5 in . by $2 \frac{1}{2} \mathrm{in}$., costs 15 s .6 d ., and another one, 14 in . by 6 in . by $3 \frac{1}{2} \mathrm{in}$., costs $£ 1 \mathrm{ls}$. Are the prices in proportion to the volumes? If not, why not?

Hint.- If the volume of the first case divided by the volume of the second case equals the price of the first divided by that of the second, then the prices are proportional to the volumes. See § 222.
15. If in the last question the prices are not proportional to the volumes, then find what must be the price of the second case in order that the prices may be proportional to the volumes.

Hint. - Find the price of 1 cubic inch of the first case, and taking this as a basis for the second case, find what its price should be.
16. From the last two questions, find by what decimal of $£ 1$ the jeweller is better or worse off by selling the second case for $£ 1 \mathrm{ls}$. than if he sold it at the price found in Question 15.
17. A half-pound package of butter is $4 \frac{1}{2} \mathrm{in}$. long, 2 in . wide, and $1 \frac{3}{4} \mathrm{in}$. thick. What are the internal dimensions of a case which will contain twelve dozen half-pounds? lach row is to contain six packages placed end to end, and there are to be six rows in each layer of packages, the largest faces of which are horizontal.
18. If in the last question the wood of the case be $\frac{3}{8} \mathrm{in}$. thick, what are the external dimensions of the case?
19. How many apples, the average diameter of which, including packing material, is $2 \frac{1}{2}$ in., can be packed in a case 1 ft .8 in . by 1 ft .3 in . by $12 \frac{1}{2} \mathrm{in}$.?
20. A particular kind of briquette is $5 \frac{1}{4} \mathrm{in}$. by $4 \frac{1}{2}$ in. by $2 \frac{1}{2}$ in. What size coal cellar would you want to hold 50 gross, presuming them to be packed in carefully (with their largest faces placed horizontally) twenty-four in a row and twelve rows?

## B. Specific Gravity

203. The weight of 1 cub. in. and of 1 c.c. of water have been determined by weighing with great care. We assume the values given on pages 196 and 198.

Note.-The NUMBER OF TIMES that any volume of a substance is
heavier or lighter than an equal volume of water is called its SPECIFIC GRAVITY. Hence the specific gravity of gold is $19 \cdot 3$ (Question 9, p. 105).

## EXAMPLES. LV.

1. If $1 \mathrm{Kgm} .=2 \cdot 2046 \mathrm{lb}$., calculate the weight of 1 cub. ft . of water in Kilograms.
2. What is the weight of 1 cub. in. of gold if that metal is $19 \cdot 3$ times heavier than water?
3. What should be the weight of 1 c.c. of gold?
4. Explain why one of the last two questions is much simpler than the other, and suggest some ready means of simplifying the harder one, presuming that you can change the unit of weight ${ }^{1}$ or unit of length as you please.
5. We give now the weight of 1 cubic foot of a number of different substances and ask the student to fill in column 3 :

| 1. <br> Substance. ${ }^{2}$ | 2. <br> Weight of 1 Cubic Foot. | 3. <br> Weight of 1 Cubic Foot of Substance Weight of 1 Cubic Foot of Water or the Specific Gravity of the Substance |
| :---: | :---: | :---: |
| Water | $62 \cdot 321 \mathrm{lb}$. |  |
| Salt . | 74.7852 , |  |
| Powdered chalk | $69 \cdot 306$ ", |  |
| Powdered coal . | 93.481 ", |  |
| Sand | 118.41 " |  |
| Iron filings | $448 \cdot 711$ " |  |
| Mercury . | 847.565 |  |
| Paraftin . | $49 \cdot 857$ |  |
| Glycerine | 77.9 |  |

Use the results of the last question to work Questions 6 to 12 :

[^4]6. A merchant is going to export salt in a case, 3 ft . by 2 ft . by $1 \mathrm{ft} .6 \mathrm{in} .$, which weighs 18 lb . What is the total weight of the package?
7. A wheelbarrow is 2 ft .6 in. long; what weight of sand will it hold if the volume of the sand equals the area of the section shown in the diagram multiplied by the length?

8. What volume should a case have in which to export half a ton ( 1120 lb .) of iron filings?
9. How many cubic feet are there in a "bottle" of mercury which contains 84 lb . of the metal?
10. What is the weight, in tons, of a million gallons of paraffin delivered from a well and run into suitable tanks? (l gallon of water $=10 \mathrm{lb}$.; and $2240 \mathrm{lb} .=1 \mathrm{ton}$.)
11. What should be the weight of a pint of glycerine?
12. How many cubic feet are there in half a ton of powdered chalk ?
13. Take the weight of 1 cubic foot of water as being 1000 ounces, and fill in the table given below :

14. Working as in the last question, and using the fact that 1 c.c. of water weighs 1 gram, find the weight of 1 c.c. of each of the substances, tabulating as before. Why is this question easier than the last

A pint of pure water weighs a pound and a quarter.
15. Find the weight of 1 pint of each of the following liquids whose specific gravities are given in brackets: Lubricating oil ( 095 ), methylated spirit ( $0 \cdot 85$ ), linseed oil ( 0.94 ), turpentine ( 0.87 ), sea water ( 1.025 ), milk ( 1.03 ).
16. A gallon of water weighs 10 lb . and 1 cubic foot werghs 62.321 lb ., find the number of gallons of water in 1 cubic foot.
17. Find, from the rosults of Questions 15 and 16, (1) the weight of a gallon of each of the liquids named; (2) the weight of 1 cubic foot; (3) the number of gallons of each to 1 cubic foot.
18. What volume of oil would be contained in a tank 10.6 in. long, 5.84 m . wide, and 3.6 m . deep ?
19. If the specific gravity be $0 \cdot 8$, find the weight of oil in Question 18.
20. If a box 4 ft . by 3 ft .9 in . by 2 ft .10 in . were fillel with gold, a culie foot of which weighs 0.49 tons, what weight of the metal would the box contain?
21. A brick is 9 in . by $4 \frac{1}{2} \mathrm{in}$. by $1 \frac{8}{4} \mathrm{in}$., and it weighs 7 lb . How many times is it heavier than an equal volume of water?
22. What is the specific gravity of olive oil if a litre weighs 900 grams?
23. What is specific gravity of an oil if 1 cubic foot weighs 56.089 lb . ?
24. What is the weight of a piece of lead 6 in . by 8 in . by 5 in .? (Specific gravity $=11 \cdot 4$.)
25. How many cubic feet of lead are there in a sheet 168 in . long, 56 in. wide, and $\frac{3}{8}$ inch thick?
26. If a cubic foot of lead weigh $707 \cdot 4 \mathrm{lb}$., what is the weight of the lead in the last question?
27. If the piece of lead referred to in Question 25 were used to cover a flat roof supported by six uprights, what decimal of a ton weight would each upright sustain, supposing the weight to be distributed evenly?

## C. The Prism Law

204. Each of the objects represented in Figures 1 to 5 is of uniform sectional area. Any such object is called a Prism. If its section is triangular, then it is called a Triangular Prism; if pentagonal (5-sided) or circular, it is called a Pentagonal Prism
or a Circular Prism, as the case may be. The usual name for the latter is, of course, a Cylinder.


(4)

(5)

The volume of any prism
$=$ area of base $\times$ height, or sectional area $\times$ height,
i.e. $\mathrm{V}=\mathrm{A} \times h$.

If the cylinder were only roughly uniform, such as a tree, then the volume would be approximately equal to the average sectional area $\times$ height.
205. Tins of circular and elliptical section are largely used in conmerce. For example, a world-famed firm of cocoa manutacturers puts up a quarter of a poond of cocoa in a cylindrical tin, 2 in in diameter and 4 in . high, and an equally famous firm puts up mustard in small elliptical tins 2 in . high and $1 \mathrm{l}_{4}^{\mathrm{s}} \mathrm{in}$. for the longer diameter and 1 in . for the shorter dianneter of the bottom and top.

The area of an ellipse is $\frac{\pi \times \mathrm{AB} \times \mathrm{CD}}{4}$ or $\pi a b$ where $a$ and $b$ are the semi-axes.

If $a=b$ theu the ellipse becomes a circle and $\pi a b=\pi r^{2}$ where $r=a$ or $b$.

206. Example.-Find the volume of a cylinder of iron 8 ft . long and $3 \frac{1}{2} \mathrm{in}$. in diameter.

$$
\begin{aligned}
\text { Volume } & =\text { area of base } \times \text { height } \\
& =\pi r^{2} \times \text { height } \\
& =\frac{11}{2 d} \times \frac{\pi}{4} \times \frac{7}{4} \times \$ \\
& =77 \text { cubic feet. }
\end{aligned}
$$

Whence it is easy to calculate the weight of metal if we know its specific gravity.

## EXAMPLES. LVI.

Apply the above rule (§204) to find the volumes of the following objects in cubic feet or cubic metres (Questions 1 to 7 ):

1. An oak strip which is square in section, edge 1 in . and length 5 ft .
2. A plank, 12 ft . long, 9 in . wide, and $2 \frac{1}{2}$ in. thick.
3. A whitewood strip, $4 \mathrm{in} . \times 4 \mathrm{in} . \times 8 \frac{1}{2} \mathrm{ft}$.
4. A cylindrical rod, 6 ft . long and 1 in . in diameter.
5. A bar of iron, of the section shown, 20 cm . long.
6. A roughly hewn tree whose diameter at three points is $35 \mathrm{~cm} ., 30 \mathrm{~cm}$., and 25 cm .,
 and length 10 m .
7. The roller of a blind of the section shown, $1 \frac{1}{2}$ yd. long. (See § 194.)
8. The section of a pillar which helps to support the roof of a church is in the shape of a regular hexagon of 1 ft .6 in . side and height 20 ft . Find the volume of the brickwork of which it is made.

9. What weight must the foundations be capable of supporting if the specific gravity of the brick work of the last question is 2.2 and the weight that the pillar supports is two-thirds of iis own weight?
10. The Royal Albert Bridge, which carries the Great Western Railway over the Tamar into Cornwall, was erected by the great engineer I. K. Brunel, and opened in 1859. The supports in the middle are hollow octagonal cast-iron (not steel, observe) columns 10 feet in diameter and 100 feet high. Calrulate the volume of the cavity inside each column.
11. Continuing the theme of the last question, the student is informed that the railroad is supported from two oval tubes made of malleable-iron plates, the diameters of each are 17 feet and 12 feet, while the mean length is 460 ft . Calculate the volume of the hollow in each tube, neglecting the thickness of the iron.
12. An oil merchant buys a drum of linseed oil which is 12 in . in diameter and 2 ft .6 in . high. How many pints of oil does it contain?
13. A merchant offers a conical heap of sand for sale and asks $£ 9$ for it. A would-be purchaser offers him 3s. 6d. a cubic yard. The circumference of the heap is 132 feet and the height that of a walking-stick, namely, 3 feet. Does the merchant ask more than he is offered, or less? (§201.)
14. A Canadian farmer has a rick of hay 30 feet long, and shaped, roughly, as shown in the figure. He wishes to export it, and knows that 40 cubic feet go to the shipping ton. How many shipping tons has he?

15. How many cubic yards of merchandise could be stored in a shed shaped as shown in the figure, if its length be 120 feet?

16. In erecting a new building the gravel soil has to be excavated to a depth of 21 feet for cellars. The ground is at the corner of two roads and is shaped as shown. How many cubic yards of gravel have to be removed? What is the value of it at 2s. per cubic yard ?

17. Example.-A covered box is made of metal of specific gravity 5 , and its dimensions are: internal, 2 ft . by 1 ft . by 9 in . ; external, 2 ft .2 in . by 1 ft .1 in . by 12 in. Find its weight.

$$
\begin{aligned}
\text { Internal volume } & =2 \times 1 \times \frac{3}{4} \text { cub. } \mathrm{ft} . \\
& =1.5 \text { cub. ft. } \\
\text { External " } & =2 \frac{1}{6} \times 1 \frac{1}{12} \times 1 \text { cub. ft. } \\
& =2.35 \mathrm{cub} . \mathrm{ft} .\left(\text { to nearest } \frac{1}{10} \mathrm{th}\right) \\
\therefore \text { volume of MeTAL } & =2.35-1.5 \\
& =0.85 \text { cub. } \mathrm{ft} .
\end{aligned}
$$

1 cub. ft . of water weighs 1000 oz .
1 cub. ft. of metal

$$
\begin{array}{rl}
" & 5000 \mathrm{n} \\
" & 0.85 \times 5000 \mathrm{oz} \\
= & 4250 \mathrm{oz} . \\
= & 0.12 \text { tons },
\end{array}
$$

## EXAMPLES. LVII.

## Miscellaneous Questions

(For any constants required, sec $\S \S 145$ and 146.)

1. Sappers wish to mine an enerny's trench 150 yds. from them, and to this end they have to dig a tunnel 4 ft . by 2 ft .6 in . If they can throw out l cub. yd. of material (and fix up the sides of the tunnel as well) every ten and a half minutes, how long will it be before they can put the charge ready to blow up the trench?
2. A railway company has a truck for carrying gas in a cylinder which is 15 ft . long, and contains $6930 \mathrm{cub} . \mathrm{ft}$. of gas which, on being forced into the cylinder, are compressed to one-third the volume they occupy under ordinary atmospheric conditions; what must be the diameter of the cylinder?
3. A timber merchant wants to have a saw-pit dug, and its dimensions are to be 20 ft . long, 8 ft . wide, and 8 ft . deep. The first 18 in . of soil are earth and the remainder clay. It costs 1 s . and 4 s .6 d . to dig out 1 cub. yd. of earth and of clay respectively. Calculate what it will cost to dig the saw-pit.
4. In a building constructed of reinforced concrete ${ }^{1}$ the dimensions of a vertical rectangular pillar are $20 \frac{1}{2} \mathrm{ft}$. by 15 in . by 12 in . ; what is the volume of the pillar in cubic yards?
5. If the iron standard within the concrete referred to in Question 4 occupies 0.7 of the volume, determine the weight of the concrete if its specific gravity is 2.2 .
6. In the west end of London stiff cardboard boxes are packed in dozens into skeleton crates. If the size of each cardboard box is 1 ft .9 in . each way, and they are packed in three tiers of four in each tier, what are the dimensions of the crates?
7. If a room 25 ft . by 18 ft . by 15 ft .6 in . be arranged to accommodate thirty-two people, determine how many cubic feet are allowed for each person.
8. How many loads of rough timber are there in a stack 40 ft .6 in . by 25 ft . by 18 ft .6 in ., if a load of rough ${ }^{2}$ timber is reckoned as being 40 cub. ft .
9. A cord of wood ${ }^{3}$ is 128 cub. ft . What will be the height of a stack of wood containing 30 cords if the ground on which it stands is 24 ft . by 16 ft ?

[^5]10. What is the weight of a load ( 50 cub. ft.) of walnut wood if its specific gravity is 0.7 ?
11. A hard ware merchant in Birmingham consigns goods to a customer in South Africa in three cases whose dimensions are-

|  | Case. | Length. | Width. | Height. |
| :---: | :---: | :---: | :---: | :---: |
| 1 | - - | 3 ft .6 in. | $2 \mathrm{ft} 6 in.$. | $1 \mathrm{ft}$.6 in . |
|  | - . | 2 ft .9 in . | 3 ft .4 in . | 2 ft .6 in . |
| 3 | - - | 3 ft .4 in . | 2 ft . | 3 ft .6 in . |

If a shipping ton of merchandise is 40 cubic feet, find the number of shipping tons consigned.
12. If a case of cloth is 4 ft .6 in . long and 3 ft .6 in . wide, what height can be allowed so that it may not exceed one shipping ton?
13. What is the average sectional area in square centimetres of a cylindrical glass measure, made in Belgium, capable of holding one-half an imperial pint, if the half-pint mark is to be 10 cm . from the bottom of the measure inside?
14. What is the diameter in centimetres of the half-pint measure of the last question?
15. A brass cylinder 4 in . in external diameter and $10 \frac{1}{2} \mathrm{in}$. high, has internal dimensions $3 \frac{1}{2} \mathrm{in}$. in diameter and $8 \frac{1}{2} \mathrm{in}$. high. Find the volume of the metal.
16. Taking the specific gravity of brass as 8.00 , find the weight of the metal in the last question.
17. The internal diameter of a bucket which is circular in plan is 11 in . at the top and 9 in . at the bottom; its height is 12 in . How many gallons of water will it hold?
18. A dredger, made by a French company, is provided with buckets whose capacity is 2500 litres each. They are elliptical in shape, 125 cm . being the length of the major (longer) diameter and 120 cm . that of the minor (shorter). What is the depth of each bucket?
19. How many buckets must there be on the dredger of the last question if it is to comply with a recent specification of the South Australian Government for a delivery of 27000 cubic feet an hour, and each bucket is used six times per hour? (1 in. = 2.54 cm .)
20. Trenches called "leats" run across Dartmoor, by means of which water is conveyed from the hills to the coast towns. ${ }^{1}$ Much of the water has pow been "piped."

Some of these leats are said to have been dug by Sir Francis Drake, in whose honour "Ye Fishinge Feaste" is still held. If a particular leat is 4 ft .6 in . wide, with a depth of water of 8 in . flowing at 4 miles an hour, determine the number of gallons of water that it will deliver per day into the town which it feeds.
21. What is the volume of the circular "bob" of the pendulum of a grandfather clock if it is 5 in . in diameter and $\frac{3}{8} \mathrm{in}$. in average thickness?
22. What is the weight of the "bob" in the last question if the specific gravity of lead is 11.35 ?
23. It is usual for companies which supply water to do so at the ordinary charge, provided the bath does not contain more than 80 gallons when filled to the level of the overflow pipe. The diagram represents the average section of an ordinary bath. What depth of water could be put into this bath without exceeding the limit fixed. Is it a reasonable limit?
(Take the area of ABC as one-half of the semicircle of radius $10 \frac{1}{2} \mathrm{in}$., so as to allow for the slope of the bath.)

24. The parapet of a terrace is ornamented with marble, and at intervals there are marble balls ${ }^{1} 9 \mathrm{in}$. in diameter. What would be the weight of marble required for each ball if its specific gravity is 2.7 ?
25. A hemispherical silver rose-bowl is 28 cm . in internal diameter and 3 mm . thick. How many cubic centimetres of metal does it contain if 12 cub. cm . must be added for its supports?
26. What is the weight of the bowl of the last question in ounces Tr .? (The specific gravity of silver is 10.51 .)
27. What is the value of the metal in the bowl of Question 25 if silver be worth $23 \frac{1}{8} \mathrm{~d}$. per oz. ? (§ 145.)
28. What must be the internal diameter of a hemispherical "finger bowl" if it is to contain 0.352 ditre of water?
29. What is the height of a cylindrical litre measure the internal diameter of which is 11.2 cm .?
30. If the metal in the last question be 2 mm . thick, and the measure has no cover, calculate the volume of the metal.
31. If the metal of which the measure of Question 29 is made has a specific gravity of $6 \cdot 5$, find its weight.
32. Emigrants to Canada are allowed two boxes, each ${ }^{1}$ See § 201.
$2 \mathrm{ft} .5 \mathrm{in} . \times 1 \mathrm{ft} .6 \mathrm{in} . \times 1 \mathrm{ft} .6 \mathrm{in}$., free, on board ship, supposing they travel steerage. How many shipping tons will 325 emigrants carry, supposing each one takes the full quantity?
33. A firm of instrument makers wishes to quote for 1000 spherical copper balls each 2 in . in diameter. If the metal stand at $£ 65$ per ton of 2240 lb ., what will be the actual value of the balls? ( Sp . gr. of copper is 8.9 .)
34. What is the internal volume of the cylinder of an engine if it be 6.8 cm . long and 2.2 cm . in radius of cross-section?
35. The dam at Gatun, on the Panama Canal, consists of a core of fine sand and clay surrounded with earth. It is 7700 ft . long, 115 ft . decp, 2100 ft . wide at the bottom, and 398 ft . wide at the top. Calculate to the nearest thousand the number of cubic yards of material that were employed in its construction.
36. The great dam at Assouan ( 600 miles south of Cairo) is $1 \ddagger \mathrm{mi}$. long, 120 ft . high, 23 ft . thick at the top, and 81 ft . thick at the bottom. Calculate to the nearest thousand the number of cubic yards of masoury employed in its construction.
37. The Suez Canal is 87 mi . long, 240 ft . wide at the water level, 72 ft . wide at the bottom, and has an average depth of 29 ft . Calculate to the nearest thousand cubic yards the volume of sand and clay excavated in its construction.
38. Wood is sold in Canada by the "cord," one of which occupies a space 8 ft . by 4 ft . by 4 ft . In Regina a cord of wood is worth 9 dollars. In England, four bundles of wood occupy a space $7 \frac{1}{2} \mathrm{in}$. by $7 \frac{1}{2} \mathrm{in}$. by 5 in ., and are sold for a halfpenny each bundle. Is wood dearer in England than in Canada or cheaper, and how many times?
39. The top of a pepper dredge is shaped as shown in elevation in the diagram. ABCD is a cylinder and $A E B$ is a hemisphere, the mean diameter of each being $2 \cdot 4 \mathrm{~cm}$. The thickness of the metal is 0.7 mm ., its specific gravity $6 \cdot 5$, and $A D=2 \mathrm{~cm}$. Calculate the weight of metal necessary to make a gross of "tops," expressing the result in Kilograms.

40. The dimensions of the bottom of a reservoir are 1000 yds . by 250 yds . It contains 500 million gallons of water. What is the average depth of the water? (1 gallon occupies 277.272 cubic inches.)
41. What must be the area of a rescrvoir, in Hectares, in which the average depth of the water is to be 5.5 metres, and in which 110 million Hectolitres of water are to be stored?
42. Express the result of the last question in the decimal of a square mile.
43. The larger of the Latchford locks on the Manchester Slip Canal ${ }^{1}$ is 600 ft . long, 65 ft . wide, and has a rise of 14 ft .6 in How many gallons of water are required to raise a ship from the lower to the higher level by means of the lock? ( 1 cubic foot water $=62.321 \mathrm{lb}$., and 1 gallon of water $=10 \mathrm{lb}$.)
44. The Empress Open Dock at Southampton is $18 \frac{1}{2}$ acres in area, with a minimum depth of 26 ft . at low water. Calculate the number of gallons of water which enter the dock for a rise of 13 ft . in the tide above the low-water mark.
45. How many cubic yards of stone are there in the shaft of a circular column, if it is 14 ft . in diameter and 120 ft . high ?
46. The height of a Corinthian column (such as the Nelson Column or those which form part of the façade of the National Gallery) is usually 9.78 times the diameter of its cross-section What would be the volume in cubic yards of a column 7 ft . in diameter?
47. What weight must the foundations of the column of Question 45 be able to support if the specific gravity of the stone be 2.00 ?
48. There is a trade in pottery in South Devon in which the red clay of the neighbourhood is employed. The baking (for forty-eight hours) is carried on in an oven 9 ft .6 in . high, 8 ft .5 in . deep, and 2 ft .6 in . wide, and 960 articles were in it on one occasion. Find the average number of cubic inches allowed per article.
49. A block of copper is 2 ft . by 6 in . by $3 \frac{1}{2} \mathrm{in}$. What length of wire $\frac{1}{8} \mathrm{in}$. in diameter can be made from it?
50. The corporation of a town in Norway is inviting tenders for the supply of a stone crusher to crush 6 cub. m . an hour. Convert this into cubic feet an hour for the information of a British contractor who wishes to tender.
51. The corporation referred to in the last question requires two four-wheeled water-carts of tank capacity 1500 litres. Express this capacity in gallons.
${ }^{2}$ Opened for traffic 1st January 1894.

## SECTION XV

## WEIGHT AND CAPACITY

208. We shall assume the following relationships in this section unless otherwise stated (for others, see $\$ \S 145$ and 146):

1 cub. ft. of water weighs 62.321 lb .
1 cub. ft. of any substance weighs $62.321 \times \mathrm{sp}$. gr . of that substance.
1 gallon of water
1 gallon
1 ton
1 Kgm .
1 litre
1 metric ton
1 pood ${ }^{1}$
1 dessiatine ${ }^{1}$
weighs 10 lb .
$=4543$ litres.
$=1016.05 \mathrm{Kgm}$.
$=2.2046 \mathrm{lb}$. (Av.).
$=32.151 \mathrm{oz}$. (Tr.).
$=1.76$ pint.
$=2204 \cdot 6 \mathrm{lb}$.
$=36 \mathrm{lb}$.
$=2.7$ acres.
1 franc $=9.513 \mathrm{~d}$.
Yen $1^{2}=2 \mathrm{~s} .0 \frac{1}{2} \mathrm{~d}$.
$1 \mathrm{kin}^{2}=1.323 \mathrm{lb}$. (Av.).
$1 \mathrm{koku}^{2}=4 \cdot 96 \mathrm{imp}$. bushels.
1 chō $^{2}=2 \cdot 45$ acres.

## EXAMPLES. LVIII.

## Miscellaneous Questions

1. How many trusses of old hay ( 56 lb .) can be placed on a cart constructed to carry 2 tons?
2. A load and a half of old hay weighs 27 cwt. How many trusses are there in a load?
3. A truss of new hay weighs 60 lb . What is the weight of a load ( 36 trusses) in hundredweights, quarters, and pounds?
4. A United States barrel of flour contains 196 lb . How many barrels can be filled from 36 cwt . of flour?
5. A bushel of rye or of maize weighs 60 lb . How many bushels are there in a consignment weighing 5 tons 3 cwt. 2 qrs.?
6. A bushel of English oats contains 39 lb . What is the weight of 115 qrs. 6 bushels in tons, to two places of decimals?
7. Potatoes are sold in one quality at 3 lb . for $2 \frac{1}{2} \mathrm{~d}$., and in another at 8 lb . for $5 \frac{1}{2} \mathrm{~d}$. Find the difference in price of 1 cwt . of each quality.
8. If 2 cwt . of potatoes costing 7s. 6d. per cwt. be mixed with ${ }^{1}$ Russia.

3 cwt. costing 6s. 8 d . per cwt., what must be the selling price per stone in order to gain half the original outlay?
9. A dairyman buys 3 cwt . of butter for $£ 12$, and after mixing a gallon and a half of water with it sells it at 1s. 1d. per lb . What is his profit per pound?
10. A wine merchant mixes 80 gallons of wine at 15 s 6 d . a gallon with 120 gallons at 12 s . 9 d . a gallon, and sells it at 2 s . a pint. What does he gain per gallon, to the nearest penny?
11. 3 cwt . of coffee is bought for $£ 88 \mathrm{~s}$. per cwt., and after being ground is mixed with 28 lb . of chicory at $£ 512 \mathrm{~s}$. per cwt. The whole is sold for 2 s . per lb . Calculate the total profit.
12. A provision merchant buys 21 ewt. of butter at $£ 80$ per ton, mixes with it 4 cwt . of inferior fat which costs him 15 s ., and sells 14 cwt . at 1 s . per lb. He is then prosecuted, convicted, fined $£ 15$, and the rest of his mixture is confiscated. What does he gain or lose by the transaction?
13. What is the difference in weight between a bar of wood circular in section of $\frac{1}{2}$ inch radius and 3 ft . long, and an iron bar of the same size? (Sp. gr. of iron $=7.85$, and of wood $=0.85$.)
14. What is the weight of forty-eight iron bars, such as are used for making cart wheels, each of which is $20 \mathrm{ft} . \times 1 \frac{1}{2} \mathrm{in} . \times \frac{3}{8} \mathrm{in} . ?$
15. What would be the cost of sending the iron mentioned in the last question from Birmingham to London at 15 s .8 d . per ton?
16. Furniture is conveyed from London to a station 200 miles down the country for 42 s .6 d . per ton. What is the cost per cwt.-mile?
17. If a merchant have 18 tons 7 cwt .2 qrs. weight of furniture, what would it cost him to have his furniture removed under the conditions mentioned in the previous question?
18. The price quoted in Question 16 does not include packing, nor is it at the company's risk. A firm of carriers packs and accepts risk for conveyance at 4 s .9 d . per cwt. Determine the total cost of packing and conveying the weight of furniture given in Question 17.
19. A bottle of mercury contains 84 lb . and costs $£ 11 \mathrm{ls}$. Find the value of a consignment of the metal weighing 15 cwt . 2 qrs. 18 lb.
20. Nainsook and similar cloths (white, black, or coloured) imported into Egypt have to pay a duty of 239 milliemes per Kilogram. Find, in English money, the duty on a consignment of 1 ton, allowing 3 per cent. off the gross weight for tare. ( 1000 millièmes $=£ \mathrm{EL}=£ 10 \mathrm{~s} .6 \mathrm{~d}$.)
21. The largest iron ore deposit in South Australia is situated
about 40 miles from Port Augusta. The average yield of the ore is 68.5 per cent. of metallic iron, and it is estimated that 21 million tons of ore are available. Calculate the value of the iron in the ore at 62 s . per ton.
22. Trebizond (Russia) tobacco made 21 roubles per pood ${ }^{1}$ in 1914. What was the price per pound? ( 1 rouble $=2 \mathrm{~s} .1 \frac{1}{3} \mathrm{~d}$.)
23. The total quantity of gold imported into India from all sources in 1913 was $6,813,489$ oz., valued at $£ 27,527,190$. Calculate the average value of 1 oz . of gold to the nearest penny.
24. Taking the circumstances of the last question, find the average value of 1 oz . of silver if the importation of $107,190,427 \mathrm{oz}$. was valued at $£ 13,693,978$.
25. Up to the present the greatest productivity of beet sugar in Russia occurred in 1910-11, and then 193.36 poods were produced per dessiatine. Calculate the weight of sugar derived from one acre.
26. A company conveyed goods as follows:


Find the receipts per ton in the case of each class of goods.
27. A great hundred of eggs consists of 120 , and in the trade dairymen reckon that 8 large eggs or 10 small ones weigh 1 lb . Taking the tare of the containing case as $11 \frac{1}{2} \mathrm{lb}$., find the cost of sending a great hundred of each size egg by rail at $2{ }_{4}^{3} \mathrm{~d}$. per lb .
28. Very large quantities of platinum are produced in Russia and reach London through continental intermediaries. On one occasion no less than 33180 Troy oz. of the metal were pledged with Russian Banks because of the absence of a market. Presuming the value in English money per Troy ounce to be $£ 510 \mathrm{~s} .6 \mathrm{~d}$., find to the nearest pound the amount of capital lying idle as a result of this absence of market.
29. An army of a million men has 20 tons of vaseline issued to it each month. Determine what is the average weight in ounces issued to each man per month.
30. If 1 cwt . of vaseline cost $£ 1$, find the value of this substance issued to the army in a year.
${ }^{1}$ This was a fairly high price.
31. A railway company has open goods wagons as follows:

$$
\begin{array}{lc}
\text { Average Tare. } & \text { Number. } \\
7 \text { tons } 3 \text { cwt. } 2 \text { qrs. } & 202 \\
9 \text { tons } 15 \text { cwt. } 1 \text { qr. } & 9325
\end{array}
$$

Find the average tare for these two classes of wagons taken together.
32. A steamship company has twelve steamboats of over 250 tons each. Their total registered tonnage is 4906.09 tons, and their indicated horse-power 44546. What is the average horse-power per hundred tons registered?
33. Last year 9600 chests of Excise opium were issued in Bengal, and their total weight was 14400 maunds. Taking 1 maund as 82.286 lb ., calculate the average weight of each chest in pounds to one place of decimals.
34. The Russian tobacco production is slowly becoming more valuable, and consequently the importation of that commodity is diminishing in value. In 1912, 30400 poods valued at one and a half million roubles were imported. What was the average value in shillings per pound of the imported tobacco? ${ }^{1}$
35. A railway is ahout to be built in Spain from Madrid to Valencia; the rails are to be 12 metres long and must weigh 40 Kilograms per lineal metre. Calculate the total weight of iron used in rails (single track) if the distance between the cities is 560 Kilometres, and also the number of rails which must be employed.
36. What is the duty on 3 cwt .1 qr .28 lb .14 oz . of ivory exported from the Nyassaland Protectorate at the rate of 10 s . per lb. $?$
37. What is the duty on 2 qrs. 18 lb .8 oz . of asbestos at 6 d . per lb. exported as in Question 36 ?
38. A duty of 1 centavo per Kilogram is imposed on paper imported into the Argentine to be used for newspapers. What is the duty per ton? ( 100 centavos = 2s.)
39. The grain elevator on the Manchester Ship Canal can deliver 1075 sacks per hour into the holds of vessels at the wharf. If this quantity weigh 120 tons, calculate in pounds the weight of a sack of grain.
40. If the elevator of the last question deliver grain in bulk, then its capacity is 450 tons per hour. Reckoning that a bushel of English wheat weighs $60 \mathrm{lb} .$, calculate the number of bushels delivered per minute.
${ }^{1}$ In the year given, Russia exported tobacco of value 7,654,000 roubles.
41. A steamboat of 4500 registered tons sails regularly fron. Hong-Kong to Yokohama. Calculate the dues paid in English money, at the rate of sen 15 per registered ton per annum.
42. A duty of 80 reis per litre is imposed on beer of high fermentation whether imported into Brazil or of domestic manufacture ; calculate the duty on a barrel of beer of 36 gallons, exported from England to Brazil. ( 1 milreis $=1 \mathrm{~s} .4 \mathrm{~d}$.)
43. Taking 1 gallon of water as weighing 10 lb . and the specific gravity of petroleum as $0 \cdot 8$, find the number of gallons by which the production of petroleum in Russia in the intervals given in Question 46 varied.
44. If leather, cut out for boots and shoes, pays a duty of 12 pesos per Kilogram on importation into Uruguay, find the duty per ton in English money. ( 1 gold peso $=100$ centesimos $=$ 4 s .3 d.$)$
45. A duty of 25 reis is payable on each box of stearine, spermaceti, or paraffin candles weighing 250 grams or less, imported into Brazil. Find the duty payable on $3 \frac{1}{2} \mathrm{cwt}$. of candles exported from London to Brazil. ( 1 milreis $=2 \mathrm{~s} .3 \mathrm{~d}$.)
46. In the first half of last year $2,245,814$ proods of petroleum were produced in the Maikop region of Russia, while in the year before, the production was $2,563,846$ poods. Express, in tons, the difference in the production for the years given.
47. Canada imported 4147 gallons of perfume from France in bottles not containing more than 4 oz . each in 1913. The value of the importation was 33987 dollars. What was the average value of the perfume per quarter-pint in English money?
48. The United Kingdom exported 537069 gallons of ale, beer, and porter into Canada in 1913, and the value of that quantity was 493212 dollars. What did the United Kingdom brewers charge Canada per quart, to the nearest halfpenny?
49. A Spanish construction company has undertaken to build twenty liners of a total tonnage of 100000 tons and of a value of $£ 4,000,000$. Find the cost of each liner in francs, and the cost per ton in francs.
50. The output of a continental coal syndicate was $3,918,000$ metric tons of briquettes; convert this weight into tons, and calculate the value at 25 s . 6 d . per ton.
51. About 18 million poods of flax are exported from Russia in a (normal) year, and the production is $18 \frac{1}{2}$ poods per dessiatine. Calculate what number of acres yield one ton of flax.
52. Convert the following weights into Kilograms correct to $\frac{1}{10}$, the details being for one of the best types of English motor cycle: Weight of engine, carburettor, magneto, and silencer,

90 lb .; weight of flywheel, $36 \frac{1 \mathrm{lb} . ; \text { weight of magneto, } 7 \mathrm{lb} . ; ~}{\text {; }}$ weight of carburettor, $3 \frac{3}{4} \mathrm{lb}$.; weight of piston with rings, gudgeon pin, and springs, 2 lb . ; weight of cylinder (bare), 13 lb. ; weight of $3 \frac{1}{2}$ H.P. machine, 214 lb ; weight of $5 \frac{1}{6} \mathrm{H} . \mathrm{P}$. machine, 242 lb .
53. In the Board of Trade returns we are informed that 788956 metric tons of pig iron were produced in Germany in November 1914, and 729822 metric tons in the previous month. Find, in English tons, the excess of the former over the latter.
54. Canada exported 600481 gallons of whale oil, valued at $£ 48721$, to the United Kingdom in 1913. Determine the average value of the oil per pint, to the nearest $\frac{1}{10}$ of a penny.
55. China imported $112,459,920$ gallous of American kerosene oil in 1913, which was valued at 14,349,720 Haikuan taels. Taking the Haikuan tael as being worth 3 s . $0 \frac{1}{4}$ d., calculate the value of 100 gallons of oil in English money.
56. The yield of barley and wheat in Japan in 1913 was $25,050,450$ koku from an area of $1,828,370$ chō. Find the average yield in koku per chō and in bushels per acre.
57. The yield of wheat in Australia in 1913 was $91,969,547$ bushels, from 7,339,101 acres. Calculate to two places of decimals the yield per acre, and compare with the result of Question 56.
58. Fish scales are used in the manufacture of iridescent glaze for pottery and for imparting a pearl finish to varnish, and they are exported from Russia. Find the price in roubles per pood if it be $£ 310 \mathrm{~s} .6 \mathrm{~d}$. per ton. ( 1 rouble $=2 \mathrm{~s} .1 \mathrm{~d}$.)
59. In one week 242077 cwt . of oranges were imported into the United Kingdon. If the average weight of an orange is 4 oz., calculate the number imported in the week considered.
60. What is the retail value of the importation of the last question, if the oranges are sold at three a penny?
61. The large lock at Irlam, on the Manchester Ship Canai, is 600 ft . long, 65 ft . wide, and has a rise of 15 ft . How many tons of water will flow out of the lock in allowing a ship to descend from the higher to the lower level?
62. Last year there was a yield of 36.5 bushels per acre of oats in the province of Ontario. Convert this yield into Hectolitres per Hectare for the information of a French agriculturist.
63. If wheat costs 56 s . a quarter, find what this price would be in francs per Hectolitre.
64. Last year New South Wales imported 63320 centals of oats, upon which a duty of $£ 4749$ was paid. What was the duty in shillings per quarter? (A bushel of oats weighs 40 lb .)
65. Express the duty referred to in the last question in
francs per quintal for continental customers, reckoning 1 quintal $=$ 3.67 bushels.
66. Express a duty of 1 franc per quintal in pence per cental and in shillings per quarter.
67. Some carts in which ice is delivered at hotels and restaurants in the West End of London carry 27 blocks, each of which is 4 ft .6 in . by 2 ft .6 in . and 10 in . thick. If the specific gravity of ice is 0.85 , what weight of ice does each cart carry?
68. What is the value of the ice in each cart (Question 67), if the retail price is 2 s . per cowt.?
69. The average weight of each of forty-five coal carts which pass over a weighing platform loaded is 2 tons 9 cwt. 1 qr., find the total weight of the carts and their loads.
70. The average tare in the previous question is 6 cwt .2 qrs., what is the weight of coal in the forty-five carts?
71. In a surveyor's office there is a map of London which is attached to a roller 5 ft . long and 1.5 in . in diameter. If the specific gravity of the wood of which it is made be $0 \cdot 7$, calculate the weight of a consignment of a thousand such rollers.
72. What is the weight of a dozen 5 ft . oak strips, of $\mathrm{sp} . \mathrm{gr}$. 0.8 , square in section, each edge being $1 \frac{1}{4}$ in. long?
73. What would be the weight of a sphere of platinum of radius 3.5 cm . if the specific gravity of platinum is 21.42 ?
74. Find the radius of a sphere of platinum weighing $89.76 \mathrm{oz} .(A v$.$) . ( 1$ cubic ft. of water weighs 1000 oz .)
75. The Rhodesian gold output for January of this year was 70082 oz. as against 73889 oz . for December last. Find by how much the value of the output for January was less than for December, pure gold being worth $£ 44 \mathrm{~s}$. $11 \frac{1}{2}$ d. per ounce.
76. 1 lb . (Troy) of standard silver is coined into 66 shillings. If the value of silver be $28 \frac{1}{18}$ pence per oz. (Troy), find the actual value of a shilling.
77. The alloy (standard gold) of which English sovereigns and half-sovereigns are made consists of 22 twenty-fourths pure gold, or 22 carats. What is the "fineness" of a sovereign-that is, how many parts are there of pure gold in 1000 parts of alloy?
78. 40 lb . Troy of standard gold is coined into 1869 sovereigns. What is the value of one Troy ounce of standard gold, neglecting the value of the base metal?
79. Employing the data of the last two questions, find the value of an ounce of pure gold.
80. What is the actual value of the fine gold in a sovereign which weighs $123 \cdot 27447$ grains?
81. A penny should weigh $\frac{1}{8}$ oz. Avoirdupois. What is the weight of $£ 10$ worth of pennies?
82. Express the weight of a penny as the decimal of 1 oz . Troy.
83. What is the actual value in English money of 1 gram of fine gold? ( 1 gram $=15.43235$ grains.)
84. The gold 10 -florin piece, which is the standard coin in the Netherlands, weighs 6.720 grams and is 900 fine. What weight of fine gold is there in the coin?
85. Find the actual value in English money of the gold in a Netherlands 10 -florin piece (see Question 84).
86. 155 twenty-franc pieces, ${ }^{1} 900$ fine, weigh 1 Kgm . What is the value of the gold in a 20 -franc piece? (See Question 83.)
87. 124 twenty-kroner pieces (Deumark and Scandinavia), 900 fine, are coined from 1 Kgm . of fine gold. What is the value of the gold in a 20 -kroner piece?
88. A 10 -kroner piece weighs 4.480286 grams. What weight of fine gold does it contain?
89. Since the passing of the Coinage Law in 1897, gold 5 -yen pieces of Japan have weighed $1 \cdot 1111$ momme and are 900 tine. Find the weight of a 5 -yen piece in grams, if 160 momme $=0.6 \mathrm{Kgm}$.
90. What is the value in English money of the gold contained in a 5 -yen piece? ( $1 \mathrm{Kgm} .=32 \cdot 151 \mathrm{oz}$. (Tr.).)
91. A 50 -sen silver coin weighs 2.7000 momme and contains 800 parts of pure silver and 200 parts of copper. With silver at $22 \frac{7}{8}$ pence per oz. (Tr.), find the value of pure silver in a $50-$ sen piece (see Questions 89 and 90 ).
92. What is the actual value of a 5 -yen piece in terms of 50 -sen pieces, ignoring the value of the copper in the latter?
93. The United States gold 10-dollar piece weighs 258 grs . (Tr.) and is 900 tine. What is the value of the gold which it contains? (Question 79.)

94 . Taking the value of copper as $£ 652 \mathrm{~s}$. 6 d ., of tin as $£ 150$, and of zinc as $£ 60$ per ton, calculate the actual marketable value of the metal contained in twelve pence, ${ }^{2}$ given that bronze of which pence are made is an alloy of 95 copper, 4 tin, and 1 zinc, and that a penny weighs $\frac{1}{3} \mathrm{oz}$. (Av.).
95. Use the results of Question 76 and of Question 80 to determine the difference between the actual value of two sovereigns and of forty shillings.
96. How could the Government make money by striking silver coins?

[^6]97. A halfpenny weighs $\frac{1}{6}$ oz. (Av.), its diameter is 1 in ., and its thickness $\frac{1}{18} \mathrm{in}$. What is the sp. gr. of the alloy of which it is made ?
98. A brass weight is circular in shape and is shown in elevation in the diagram. It weighs 4 oz . Whatis the specific gravity of the metal of which the
 weight is made?
99. A pat of butter (such as one gets at a restaurant for ld.) weighs $\frac{3}{4} \mathrm{oz}$. Find, to the nearest ten pats, the number that can be made from 1 cwt . of butter.
100. Find the cost of conveying 28 tons 5 cwt. 2 qrs. of raw cotton by goods train from Manchester to Bralford, a distance of 37 mi .75 chs., if the charge per ton per mile is $2 \cdot 18$ pence, and the charges for loading, unloading, cartage, etc., are $£ 612 \mathrm{~s} .8 \mathrm{~d}$. for the consignment.
101. What is the cost of conveying slate slabs ${ }^{1}$ (unpolished, but packed in cases) per goods train from Leeds to Northampton, a distance of 120 miles, given that (1) the weight of the consignment is 42 tons 17 cwt. 3 qrs.; (2) the charge for transport is for the first 20 miles 1.8 d . per ton per mile; for the next 30 miles, 1.65 d . per ton per mile; for the next 50 miles, $1 \cdot 25 \mathrm{~d}$. per ton per mile; for the remaining distance, 0.65 d . per ton per mile ; (3) terminal and other charges are $£ 712 \mathrm{~s}$. 8 d.?
102. The gates to the locks on the Panana Canal are made of sheet iron, with air- and water-tight compartments which help to take some of the dead weight off the hinges and pivots. A gate 65 ft . long, 55 ft . high, and 7 ft . thick weighs 450 tons. Calculate the average weight of the gate in hundredweights for every square foot of surface area in the front of the gate.
103. From the data of the last question find the average weight, in pounds, of every cubic foot in the volume of the gate.
104. How would it be possible to determine whether the lock gates were of solid metal, employing the data of Question 102, and knowing that the specific gravity of iron is 7.5 ?
105. The rubber tree grows wild in the northern parts of Brazil and it has been cultivated with great success, but the industry has not yet properly developed. ${ }^{2}$ Last year 42,290,000 Kilograms of rubber were exported, at a value of $241,425,000$

[^7]milreis. Calculate the value of the export in shillings per lb . ( 15 milreis = £1.)
106. If copper stands at $£ 6410 \mathrm{~s}$. per ton on the London market, at what price must it stand in francs per Kilogram at Paris in order that French merchants may quote on equal terms with London merchants (disregard freight charges, etc.) ?
107. A particular society in London collects tinfoil, which is sold in fairly large quantities and the receipts of the sale used for the benefit of a hospital. In the three years ending January $1915,24881 \mathrm{lb}$. of metal waste tinfoil were sold for $£ 23616 \mathrm{~s} .1 \mathrm{~d}$. Find the average price paid for 56 lb .
108. What would be the cost of sending 20 dozen iron hinges $4^{\prime \prime} \times 1^{\prime \prime} \times \frac{1^{\prime \prime}}{4^{\prime \prime}}$ from Birmingham to Bristol if the cost of transit per ton is 11 s . 8 d . (Class 1 goods), ${ }^{1}$ and 1 cubic foot of iron weighs 500 lb .?
109. How many iron nails $3 \frac{1}{2} \mathrm{in}$. long and of average diameter $\frac{1}{8} \mathrm{in}$. would there be in 10 lb . of the metal? ( $\mathrm{Sp} . \mathrm{gr} ., 7 \cdot 85$.)
110. Employing the data of the last question, find how many nails there would be in a Kilogram.
111. In Trinidad and Tobago it is proposed to raise money for immigration and agriculture by imposing (among other things) an export duty of $1 \frac{1}{2} \mathrm{~d}$. on every 100 lb . of cocoa. What would be the duty on 2 tons 3 cwt. of cocoa?
112. At Busanga, in the Belgian Congo, there is an alluvial deposit of tin ore over a space of 33000 square yards to a depth of 1 yard. The ore is found in the form of cassiterite, and contains 78 per cent. of pure tin. Each cubic yard produces 15 lb .
${ }^{1}$ The student is informed that for the purposes of conveyance by rail there are Classes A, B, C, 1, 2, 3, 4, 5, for goods and minerals, while animals, carriages, and exceptional things (e.g. elephants, explosives, bullion, etc.) form separate sections, the maximum charges per mile for conveyance being fixed by Parliament.

| lass |  |  |  |
| :---: | :---: | :---: | :---: |
| ", | ", | ", | bricks, china, clay, shot, building stone. potatoes, rice, sawdust, spelter, waste paper. |
| " | ", | " | soap, solder, vinegar, timber, wheels. |
| ", | " | " | butter, cheese, cocoa, accumulators. |
| " | " | " | carpets, china in hampers, cutlery. |
| " | " | " | haberdashery, furniture, hares (dead). |
| " | , | " | drugs, fruit (hothouse), mirrors, perfumery, plants. |

The charges per ton per mile (e.g. up to 20 miles) range from 1d. in Class A to 4.3 d . in Class 5, to which must be added loading, unloading, covering and uncovering charges, ranging from no charge for Classes $A$ and $B$ to 48. for Olass 6 . (See Part III.)
of ore. Find, in tons, the probable weight of pure tin derivable from the whole deposit.
113. Lake steamers on the Continent carry 50 Kilograms of luggage free per passenger. How much should an English tourist pay if his luggage weighs 350 lb . and the excess charge is 5 centimes per Kilogram?
114. During the first three months of working, the average net tonnage of vessels engaged in the Pacific Coast trade with Europe which passed through the Panama Canal was 4068 tons. The average charge was 1.20 dollars per ton for tolls. Find the average cost for each vessel to pass through the canal, giving the result in English money. ( 1 dollar $=4 \mathrm{~s} .1 \cdot 32 \mathrm{~d}$.)
115. From lst January 1915 a frasila of rubber exported from British East Africa is liable to a duty of 36 rupees. If a frasila weighs 36 lb . and a rupee equals 1 l .4 d . (fixed rating), calculate the duty per hundredweight in English money.
116. In Uruguay refined cotton-oil seed has to pay, on importation, a duty of 15 centesimos per Kilogram; find the duty per pound. ( 1 centesimo $=\frac{1}{2} \mathrm{~d}$.)
117. If figs are imported into Switzerland to be used for distillation a duty of 40 francs has to be paid for 100 Kilograms. What is this duty in pence per pound?
118. Cocoa-nut oil imported into Greece must pay 435 drachma per 100 okes. Express this in shillings per pound, if 1 drachma $=9.5 \mathrm{~d}$., and 1 oke $=2.8 \mathrm{lb}$.
119. There was a famine in Shiraz (Persia) towards the close of 1913, and the enormous quantity (for Shiraz) of 1400 tons of flour, valued at $£ 14448$, was imported. What should have been charged for a barrel of flour of 196 lb . weight?
120. In the year 1914 the Korean and Japanese rice crops were above anticipation and there were 4 million koku left in stock. If 1 koku $=4.99918$ imperial bushels, determine the quantity of rice in stock in bushels.
121. In the year 1912 the United States produced $1,243,269,000 \mathrm{lb}$. of copper, of value 205,139,340 dollars, and the United Kingdom produced 2569 tons, of value $£ 211380$. Compare the prices per ton in the two countries.
122. In the year 1913 the United Kingdom exported $12 \frac{3}{4}$ million tons of coal to France, and this weight was $\frac{10}{57}$ of the total weight exported. Find the latter weight to the nearest thousand tons.
123. Free conveyance of 150 lb . of luggage is allowed on a first-class railway ticket in Great Britain, and 30 Kilogramon the Paris and Lyons Railway. How many more poande leand
tourist travelling first class in Great Britain take free than in France?
124. How many Kilograms fewer are allowed free on the Paris and Lyons Railway than would be allowed to a French tourist in Great Britain?
125. Cutch ${ }^{1}$ makes 28s. 6d. per cwt. in England; convert this into yen per kwam for the information of Japanese fishermen. (Kwam l=8.27 lb. Av.)
126. Tenders are sought for the delivery of 270 tons of pitch for road purposes during the present year in Cairo. A firm in San Francisco tenders for this contract, and agrees to deliver the pitch via the Suez Canal. The dues through the canal are 6 fr .25 c . per ton. Calculate in dollars, for the benefit of the American firm, the total freight charge for the cargo through the canal.
127. A merchant in London places an order in Jersey for 28 cwt . of tomatoes, supposing that the wholesale dealer in Jersey has quoted in English hundredweights. He subsequently finds out that the quotation is in Jersey hundredweights of 112.3 lb . If the value of the latter be 22 s .6 d ., find how many shillings the London merchant gains or loses by his mistake.
128. If the tomatoes referred to in the last question are sold in London at $4 \frac{1}{2} \mathrm{~d}$. per lb ., and 20 lb . are damaged so that they are valueless, find what profit is made if the whole consignment cost £26 4s.
129. The value of the butter produced in Queensland last year was $£ 1,512,210$, and it made $11 \frac{1}{2} \mathrm{~d}$. per lb . Find the weight of butter produced in pounds, to the nearest hundred pounds.
130. The tractive effort of a modern type of locomotive is 22500 lb ., and the total heating surface $1215 \cdot 52 \mathrm{sq}$. ft. Calculate the pull for every square foot of heating surface as the decimal of a ton.
131. In Queensland it has been necessary to bore artesian wells which supply altogether $529,817,860$ gallons per day. The cost of boring has been $£ 2,538,875$. If now the Government looks for a return of 5 per cent. every year on the capital spent, calculate the value of 1000 gallons of water, in pence, to two places of decimals.
132. A Russian firm sold $9,627,920$ poods weight of iron girders in twelve months. Find the average sale in tons per month.
133. By how many pounds does 1000 poods differ from 16 tons?

[^8]134. The total quantity of rubber sold last year at Singapore was 44894 piculs, which ranged in price from 1 s. $6 \cdot 18 \mathrm{~d}$. to 2s. 6.66d. per lb. Find, in English money, the greatest possible difference there could have been in the sale price of the weight named. ( 3 piculs $=400 \mathrm{lb}$. Av.)
135. In 1912, 452 million quarters of wheat were produced in the world. Taking a quarter of wheat as 480 lb ., find the weight of the wheat production of the world, to the nearest ton.
136. Under the same circumstances as detailed in the previous question, $182,500,000$ quarters of barley of 400 lb . each in weight were produced. Calculate the weight of barley to the nearest ton, and then express the weight of barley produced in 1912 as the decimal of the weight of wheat produced in that year. (Question 135.)
137. Russia produced in $1910,70,340,000$ barrels of petroleum of 42 gallons each. The specific gravity of petroleum is 0.88 . Calculate the weight of the production to the nearest hundred weight.
138. Electrically-driven turbine pumps of 88000 gallons per hour capacity are to be installed in a town in New Zealand, and a French firm wishes to contract for them. What must be the delivery capacity of their pumps in litres per hour so that they may comply with the specification.
139. In a country in Southern Europe the Government is prepared to allow electrical plant to be put down for industrial and illuminating purposes, and to allow a concession for the utilisation of the waters of the river near the site for purposes of generating the current, water to be used at a rate not exceeding 2500 litres per second. Express this rate in gallons per hour.
140. There is a considerable export trade in mackerel and pilchards from Cornwall to Italy or to South Africa, and the treatment to which the fish are subjected depends on whether they are to be exported in sealed tins or in barrels. A consignment of tinned iron from which the "tin boxes" are stamped weighs 3 tons 15 cwt. 3 qrs. 25 lb ., and costs 14 s .6 d . per cwt. Calculate the amount which the fish merchant must pay for it.
141. Under the circumstances of the last question, find the value of a shipload of salt for curing purposes, weighing 22 tons 16 cwt. 3 qrs. 23 lb ., at a cost of 15 s . per ton.
142. This year's yield of cotton in the United States is estimated at $15,966,000$ bales of 500 lb . gross weight (excluding linters) and constitutes a record. Taking this yield as 207.9 lb . per acre, find the number of acres under cotton in the United States.
143. The price of lighting oil for home consumption is 7 francs 80 centimes per 100 Kilograms in Roumania. If the sp. gr. of the oil is 0.88 , find the cost in pence per gallon.
144. A record crop of winter wheat in the United States produced 19 bushels per acre. Taking a bushel as 62 lb ., find the yield in tons per acre.
145. If 50 bushels of wheat yield a ton of flour, and Australia produced $91,970,000$ bushels last year, find the weight of flour to which this is equivalent.
146. If the ocean freight is 8.9 cents per bushel, find, in English money, the cost of sending 1 million bushels from New York to Liverpool. (Question 145.)
147. In converting 10 tons into Kilograms it is assumed that $2.2 \mathrm{lb} .=1$ Kilogram, while a nearer value is $2.2046 \mathrm{lb} .=1$ Kilogram. Find the error made in the first case.
148. Express the error in the last question as the decimal of a metric ton.
149. Cotton is grown in Siam, and 1 rai produces 1 picul of cleaned cotton. It is estimated that there will be 7996 rai under cotton during the present season. How many tons of cotton will be produced upon the basis of these figures? ( $1 \mathrm{rai}=\frac{2}{3}$ acre.)
150. The report of a gas manufacturing company in Japan states that 570 thousand kin of coal produced $3,270,000$ cubic feet of gas and left 64 thousand kin of coke and 40 koku of coal tar. Calculate (1) the volume of gas produced from 1 ton of coal; (2) the proportion that the weight of coke bore to the weight of coal ; (3) the number of gallons of coal tar per ton of coal.
151. From the data given in the last question, find (1) the value of the coal at yen 5 per 1000 kin ; (2) the value of the coke at yen 4 per 1000 kin ; (3) the value of the coal tar at yen 2.5 per koku.
152. Determine the value of the gas referred to in Question 150 at 2 s .8 d . per 1000 cubic feet (the price charged around London).
153. The rate for the transport of goods in Morocco is 50 centimes per metric ton. Calculate the cost, in francs, of sending a number of packages from one part of the country to another, if the total weight is 3 metric tons 750 Kgm .840 gm .
154. The French Government makes a charge of 2.8 francs per gram on gold mined in certain specified parts of Madagascar. What amount of money should be paid upon 58 gm .5 dgm . 3 cgm . of gold (correct to $\frac{1}{10}$ franc)?
155. Last year a firm in the Errgebirge (Austria) produced

10614 Kilograms of fine tin, valued at 55000 kronen. Taking 1 krone as 10d. and 1 Kilogram as 2.2046 lb ., compare the price of tin in Austria with the price in London, namely, $£ 190$ per ton.
156. In 1912-13 the weight of barley produced in, and exported by sea from, British India was $12,303,532 \mathrm{cwt}$., and was valued at $£ 3,705,457$. If 50 lb . of barley are equal to one bushel, calculate the average price per bushel to the nearest penny (see Question 157 also).
157. If the average price of barley in the United Kingdom was 26 s .2 d . per quarter during 1912-13, find how many times it was cheaper or dearer in the United Kingdom than in India.
158. The great dam at Assouan, on the Nile, holds back 1300 million cubic yards of water. If this were discharged at the rate of 10000 cubic feet per second (i.e., roughly, the rate of the Thames in flood), how long would it take to reduce the volume of water to one-third of its original volume?

## SECTION XVI

## TIME ${ }^{1}$

209. We know that the sun appears to move through the heavens, and, perhaps, that the stars also appear to do so, but we may not realise that the motion of the celestial bodies affords us our fundamental method of measuring time.
210. Let us imagine that the sun is fixed and that the earth is turning round from west to east, then will it be seen at
[^9]Petrograd before London, and at London before New York; or, we may say, that day begins at Petrograd before it does at London, and so on. In the same way the sun reaches its highest point in the sky at Petrograd before it does at London ; and so it is noon at the former earlier than at the latter. This is expressed by saying that the Local Time at Petrograd is earlier than at London. If, then, the clocks showed local time at both places, those at the former would show 12 noon, and those in London some minutes earlier, and those at New York some minutes earlier still.
211. Under the circumstances mentioned each place in the world would have its own time, and no small confusion in catching trains, opening Stock Exchanges, etc., would result.

To obviate this, all places in Great Britain take Greenwich time, as also do France, Belgium, Spain, and Portugal. Ireland, however, keeps to Irish time, and so it is $11.35 \mathrm{a} . \mathrm{m} .{ }^{1}$ in Ireland when it is 12 noon in England and in France.

We may regard the countries mentioned above as forming a belt in which a standard time, i.e. Green wich time, is observed.
212. The sun appears to describe a circle every day, and so it moves through $360^{\circ}$ in twenty-four hours, or $15^{\circ}$ every hour ; consequently we can find the time at any place in the world if we know how many degrees it is east or west of Greenwich-that is to say, the time at any place can be found if we know its longitude and also Greenwich time.

Example 1.-What is the time at Petrograd when it is noon at Greenwich, if the former be $30^{\circ} \mathrm{E}$. ?

Since Petrograd is east, noon there will be before noon at Greenwich, and therefore it will be past noon at Petrograd when it is noon at Greenwich.
$\therefore$ the clocks in Petrograd will be ahead of Greenwich and they are therefore "fast."

Reckoning 1 hour for $15^{\circ}$ we have 2 hours for $30^{\circ}$;
$\therefore$ the time at Petrograd is 2 p.m.

## Example 2.-What is the longitude of Brisbane if the clock is 10 hrs .12 min . fast?

1 hr . fast means $15^{\circ} \mathrm{E}$.
$\therefore 10 \cdot 2 \mathrm{hrs} ., " 153^{\circ} \mathrm{E}$.
${ }^{1}$ This is the time kept on the railways.
213. Now, taking two cities in the same continent, Australia, we find that Adelaide has a different longitude from Brisbane and so a different local time; hence to facilitate business the belt system, in which a standard time is kept, is extended to the whole world.

For this purpose the surface of the earth is divided up into $15^{\circ}$ belts, and places at the middle of each belt differ in time by 1 hour, while every place in one is regarded as different from every place in the other by that same time although they may be only a mile or so apart.
214. The Zone Time is as follows :

| FASt. |  |  |
| :---: | :---: | :---: |
| Country. | Central Meridian. | Fast on Greenwich. |
| England. - . .) |  |  |
| Belgium . - . . |  |  |
| France - . - | Greenwich time. |  |
| Spain . . . . |  |  |
| Portugal. . . .) |  |  |
| Mid-Europe . . . | $15^{\circ} \mathrm{E}$. | 1 hour. |
| East Europe - . . |  |  |
| South Africa . - . $\}$ | $30^{\circ} \mathrm{E}$. | 2 hours. |
| Cgypt . . . . | $90^{\circ} \mathrm{E}$. |  |
| West Australia . | $120^{\circ} \mathrm{E}$. | 8 ", |
| Japan . | $135^{\circ} \mathrm{E}$. | 9 ", |
| South Australia | $1421^{\circ} \mathrm{E}$. | $9 \frac{1}{2}$ ", |
| Other States in Australia | $150^{\circ} \mathrm{E}$. | 10 ", |
| New Zealand . | $172 \frac{1}{2}^{\circ} \mathrm{E}$. | 112 ${ }^{2}$, |


215. Suppose now a boat leaves Holyhead ${ }^{1}$ at 9.30 a.m. and steams over to Dublin, at which place the local time is earlier

1 This paragraph relates to conditions obtaining prior to 1st October 1916, on which date the legal time in Ireland was made to synohronise with that in Great Britain.
than in England (or, the Irish clocks are slow), on landing we must put our watches back 25 minutes. If, on the other hand, we left Liverpool and sailed to New York, and, on arriving there, our watches showed 12 noon, the city clocks would show 7.4 a.m. and we should put our watches back 4 hrs. 56 mins., Not 7 hrs. 4 mins., observe, to agree with the local time.

In crossing the States, however, we should not alter our watches at every place we came to, but every time we crossed from one $15^{\circ}$ zone to the next, and, as will be seen in § 214, there are five such zones.

Zone time is not kept in Holland, and Rotterdam is 18 minutes fast.
216. From the front at Margate it is possible to see the sun set in the sea, and if we were to take a perfectly adjusted chronometer and go down there and observe precisely the time that the sun set on 25 th March, and then, after a year, were to repeat the same experiment, we should find that the interval of time between the two sunsets was 365 days 5 hrs .48 min .45 .51 secs . Julius Cæsar regarded this interval as $365 \frac{1}{4}$ days. We reckon 365 days to a year, and are therefore short by 5 hrs. 48 mins. 45.51 secs., which in four years amounts to 23 hrs .15 min .2 .04 secs . ; we should therefore add on this time every four years, but we really add one day-the 29th February in leap year-and so in 4 years add 44 mins. 57.96 secs. too much.

In 400 years the error is $44.966 \times 100$ minutes, or nearly 75 hours, which is rather over 3 days.
$\therefore$ in 400 years three days must be dropped, so that although every century year, $1600,1700,1800,1900,2000$, would be a leap year we do not call the three, the "hundreds" of which are not divisible by 400 , "leap years." Hence 1600 and 2000 are, with all other years divisible by four, leap years, but 1700, 1800, and 1900 are not, and so the three days are allowed for in 400 years.
217. In offices where bills are drawn or interest calculated (Section XXI. C.) the number of days between two given dates has to be determined, and although tables of days are provided, the student should work the first question in the following examples to familiarise himself with the method of calculation.
218. The student should read $\$ 218$ and 219 before working Questions 62 to 72 of Examples LIX.

Example 1.-A pipe is 3 sq . in. in section, and water flows through it at the rate of 12 ft . per second; calculate the number of gallons delivered per hour.

In 1 second a volume of water 3 sq . in. in sectional area and 12 ft . long is delivered.
$\therefore$ volume delivered per second $=\frac{8}{14} \times 12$ cub. ft .

$$
=\frac{1}{4} \text { cub. } \mathrm{ft} .
$$

$$
\begin{aligned}
\therefore \text { weight " } \quad \text { hour } & =900 \text { cub. ft. } \\
\text { "\# since } 1 \text { gallon } & =900 \times 62.321 \mathrm{lb} .=56088 \cdot 9 \\
\text { and } & =10 \mathrm{lb} . \\
\text { number of gallons delivered } & =56089 \div 10 . \\
& =5609, \text { to the nearest gallon. }
\end{aligned}
$$

219. Example 2.-Three pipes supply oil to a tank and one empties it. The first three can fill it in 3,5 , and 6 hours respectively, and the last empty it in 12 hours. How long does it take to fill the tank with all four pipes open?

The 1st fills it in 3 hrs ; $\therefore$ it fills $\frac{1}{3} \mathrm{rd}$ in 1 hr .

> The 2nd

The 3rd


The 4th empties it in 12 hirs. ; $\therefore$ it empties $\frac{1}{18}$ th in 1 hr . So all four pipes leave $\frac{21}{30}-\frac{1}{12}$ full "

$$
\text { or } \frac{42-5}{60}=\frac{37}{60}
$$

$\therefore$ the whole is full in $\frac{60}{3} \frac{0}{7 r s}$. i.e. $1 \frac{123}{3} \frac{3}{\mathrm{hr}}$. $=1 \mathrm{hr} .37$ mins., to the nearest minute.
220. Read this before working Questions 77 to 79, Examples LIX.

Example 3.-Two trains leave two stations 156 miles apart at the same time, and they travel at 60 miles per hour and 30 miles per hour respectively. How far will the quicker one have travelled before they meet?

They will meet in just the same time as they would if one train travelled at $(60+30)$ miles per hour and the second remained still.

Now a train travelling at 90 miles per hour would take $\frac{156}{80}$ hour to run 156 miles.
$\therefore$ they will meet in $1 \frac{1}{3} \frac{1}{5} \mathrm{hr}$., or in 1 hr .44 mins., and since the quicker one runs at 60 miles per hour they will meet when it has travelled

$$
\begin{aligned}
& 60 \times 1 \frac{11}{15} \text { mile } \\
& =104 \text { miles. }
\end{aligned}
$$

If they had been travelling in the same direction we should have subtracted the speeds and proceeded as above.

## EXAMPLES. LIX.

## Miscellaneous Questions

1. How many days are there between the following dates in an ordinary year? (N.B.-Only one of the two dates given is counted.)

| Jan. 1 to Jan. 18. | May 28 to Sept. 30. |
| :---: | :---: |
| Jan. 3 to Feb. 1. | Mch. 18 to Oct. 3. |
| Jan. 12 to Feb. 27. | June 10 to Nov. 18. |
| Jan. 21 to Mch. 3. | May 16 to Nov. 28. |
| Jan. 29 to Apr. 4. | Apr. 15 to Oct. 29. |
| Feb. 5 to Mch. 29. | Feb. 24 to Nov. 29. |
| Feb. 21 to Apr. 15. | Feb. 20 to Dec. 16. |
| Mch. 28 to Apr. 30. | Jan. 28 to Dec. 10. |
| Mch. 31 to May 30. | Jan. 15 to Nov. 18. |
| Apr. 18 to May 30. | Jan. 17 to Dec. 30. |
| Apr. 29 to June 24. | Jan. 18 to June 25 (leap year). |
| May 15 to July 25. | Feb. 15 to Dec. 26 |
| May 19 to Aug. 29. | Mch. 9 to Nov. 27 |

2. Four motor-cars ran over a given distance in 10 min .36 secs.; 18 min .30 secs. ; 19 min .25 secs. ; and 15 min .2 secs. respectively. What was the average time taken?
3. Four successive trains take 20 min . 18 secs.; 25 min . 20 secs. ; 20 min .20 secs.; and 18 min .30 secs. to run from one station to the next. What length of time must a merchant allow, on the average, from the one to the other?
4. Four of the men employed on building a collier work as follows: (1) 14 days 15 hrs .30 min . ; (2) 12 days 18 hrs .25 min. ; (3) 17 days 16 hrs .20 min . ; (4) 15 days 12 hrs .10 min . What is the total time taken, and what is the average time?
5. Express the result of the last question (1) correct to the nearest day ; (2) correct to the nearest hour.
6. A contractor employs his men on an overtime job so that they actually work 12 hrs .35 min . per day. They take 25 min . for breakfast and 50 min . for dinner. How long do they have for travelling, sleeping, and living?
7. A commercial traveller leaves Leeds at 10.15 a.m., arrives in London at $1.53 \mathrm{p} . \mathrm{m}$., where be transacts his business and
catches the 8.45 p.m. from Victoria and gets to Paris at 6.3 a.m. What length of time did he spend actually travelling?
8. A bricklayer in Queensland works as follows: Monday, 8 hrs .30 min . ; Tuesday, 6 hrs .15 min .; Wednesday, 5 hrs . 45 min . Thursday, 9 hrs .15 min. ; Friday, $10 \mathrm{hrs} .30 \mathrm{~min} . ;$ Saturday, 4 hrs .45 min . What length of time does he work during the week?
9. What does the bricklayer in Question 8 earn per hour to the nearest halfpenny if he is paid $£ 36$ s. per week ? ${ }^{1}$
10. Taking the times in Question 8, and assuming that all time over eight hours per day is paid for at overtime rate, namely, half the ordinary hour rate of 1 s . 4d., extra per hour, find how much the workman earns.
11. Employing the data of Question 5, page 350, and knowing that at certain seasons of the year the water flows in the canal at the rate of 11000 cubic feet a second, find the speed of the water in metres per hour.
12. Find, to the nearest shilling, what a merchant's income per day is if he finds he has made $£ 55615 \mathrm{~s}$. in the year.
13. Find the times occupied on the following journeys (read horizontally) :

|  | Time of Departure. |  | Time of Arrival. | Time on Journey. |
| :---: | :---: | :---: | :---: | :---: |
| London - . | 10.30 a m . | Plymouth | 2.37 p.m. |  |
| Liverpool Street, London | $8.40 \mathrm{p} . \mathrm{m}$. | Antwerp ${ }^{\text {a }}$ | $8 \mathrm{am} . \mathrm{m}$. |  |
| Charing Oross, London . | ${ }_{10}^{2 \mathrm{p} . \mathrm{mm} .}$ |  | 6.11 a.m. <br> 5.20 p.m. |  |
|  |  | Boulogne | 5.20 p.m. |  |
| Charing Cross, London | 4.30 p.m. | Paris, via Dover and | 11 p.m. |  |
| Victoria . | $10 \mathrm{a} . \mathrm{m}$. | Paris, via Newhaven and Dieppe | 5.59 p.m. |  |
| Waterloo. | 9.30 a.m. | Paris, via Havre . | 11.20 p.m. |  |

14. The times taken to run from one station to the next on one of the London tube railways are, in minutes, as follows: $-\frac{1}{4} ; 1 \frac{1}{2} ; 1 \frac{5}{6} ; \frac{9}{10} ; 1 \frac{3}{4} ; 2 \frac{3}{20} ; 1 \frac{1}{6} ; 2 \frac{5}{5}{ }^{5}$. What fraction of an hour is taken on the journey from terminus to terminus?
15. What is the average time between two stations? (Question 14.)
16. The times of trains taken from a time-table are: Waterloo, 9.35 p.m.; Vauxhall, 9.40 p.m.; Clapham Junction, 9.47

[^10]p.m. ; Earlsfield, 9.52 p.m. ; Wimbledon, 9.56 p.m. ; Surbiton, 10.11. What is the longest interval of time between any two stations?
17. In the previous question find the average interval of time between two stations.
18. A contractor at Lille employs men who work as follows in his cotton mills:


For how many hours work has he to pay at the end of the week?
19. What is the amount earned in wages in Question 18 if the average earnings are 1.25 frañc per hour per man?
20. If 1000 labourers earning $10 \frac{1}{2}$ d. an hour work 8 hours a day for $5 \frac{1}{2}$ days a week, what amount is lost to them in wages if they strike from Monday 10th January to 10th April in the year 19163
21. One mason in Newfoundland works $8 \frac{1}{2}$ hours a day for 26 days during June, and another works $12 \frac{1}{2}$ hours a day for the first ten working days and for the last five. Which of the two earns the more, and by how much? (Reckon the wages 35 cents per hour, and that a dollar $=4 \mathrm{~s} .1 \frac{1}{2} \mathrm{~d} . \quad$ Note that 1 cent is reckoned as $\frac{1}{2} \mathrm{~d}$ in Newfoundland.)
22. Employing the data given in Question 107, page 320, calculate the average weight of tinfoil (in ounces) received each month during the three years referred to.
23. Find the weekly income of the hospital (Question 22) derived from the sale.
24. The cost of maintenance of the transporter bridge ${ }^{1}$ over the Wye is $£ 1822$ per annum. What must be the average receipts per day in order that the cost may be covered?
25. If the average price charged for person or vehicle crossing on the bridge mentioned (Question 24) be $1 \cdot 3 \mathrm{~d}$., determine the number of persons or vehicles which must be carried across each week in order that the corporation may not lose money.
26. Women and girls arriving in Winnipeg can get board and lodgings in reliable hostels for a dollar a day. What would be the cost in English money of staying at such a hostel for six weeks? ( 1 dollar $=4 \mathrm{~s} .2 \mathrm{~d}$.)
27. In Victoria, ploughmen engaged on pastoral dairying or agricultural holdings can earn $£ 65$ a year and be provided with rations. Some French emigrants are proposing to go to Australia,

[^11]and wish to know whether their earnings of 4 francs a day without rations leave them better or worse off than they would be in Australia. Reckoning that their rations would cost them 1 fr . 50 c. per day, decide whether they had better emigrate or not.
28. Find, in miles per hour, the average speed of travelling from London to Paris by each of the four routes referred to in Question 13, if the distances are as follows: via Folkestone and Boulogne, 259 miles; via Dover and Calais, 287 miles; via Newhaven and Dieppe, 224 miles; via Havre, 340 miles.
29. What saving in time is there on the sea passage from England to France if one travels via Dover and Calais rather than via Folkestone and Boulogne, if the distances are respectively 22 and $26 \frac{1}{4}$ nautical miles, and the ships can travel at an average speed of 18 knots?
30. By how many days and hours is it quicker to travel from Liverpool to Wellington (New Zealand) via the Panama Canal rather than by the Suez-Aden-Colombo route, if the distances are, respectively, 11425 and 12989 nautical miles, and the average speed of travelling is 17 knots?
31. The grain elevator on the Manchester Ship Canal can (inter alia) discharge 350 tons of grain an hour from vessels at the wharf. If the elevator were to work for 8 hours each working day for one month ( 27 days), what would be the total weight of grain landed?
32. A merchant sets his watch at 10.30 a.m. by St. Paul's Cathedral clock as he takes a taxi, and begins his journey to Venice, where mid-European time ${ }^{1}$ is kept. Must he put his watch back or forward to make it agree with the time shown by the magnificent twenty-four-hour clock ${ }^{2}$ in the Torre dell' Orologio?
33. It is proposed to construct an eastern quay and an approach channel to a port in Spain at an estimated cost of $1,080,247$ pesetas, and the contract must be completed in three years. Calculate the cost per month in English money.
34. Lisbon is $9^{\circ} \mathrm{W}$. What alteration would a wine merchant have to make in the time shown by his watch if he came from Lisbon to London?
35. The time observed in British South Africa is east European time. What is the time at Cape Town when it is 7.30 p.m. in London?

[^12]36. Panama is $80^{\circ} \mathrm{W}$. It is $3.15 \mathrm{p} . \mathrm{m}$. in London. What is the time at Panama?
37. If it takes a ship five days to travel from Plymouth to New York, a distance of 2957 nautical miles, find the speed of the ship in knots.
38. Find the speed of the ship in the last question in statute miles per hour.
39. The distance from Waterloo Station to Oxford Circus is $2 \frac{1}{2}$ miles. It takes 27 minutes to walk up to the Circus and 24 minutes to walk down to Waterloo. Find the difference in miles per hour between the rate of walking up from, and that of walking down to, the station.
40. The Mauretania ran 676 nautical miles in one day, and thereby created a record. Was her speed greater or less than that of an express train travelling 60 miles per hour, and by how much?
41. Burma is $97 \frac{1}{2}^{\circ} \mathrm{E}$. By how much is the time there fast or slow on London time?
42. The eastern States of Australia are ten hours fast. How many degrees is the central moridian for those States east of London?
43. In America, Atlantic time is 4 hours slow and Pacific time 8 hours slow. What is the difference in longitude between the central meridians of the Atlantic and Pacific States?
44. If Havana, which is $83^{\circ} \mathrm{W}$., keeps the eastern American time, namely, 5 hours slow, find the time at Havana when it is $11.30 \mathrm{a} . \mathrm{m}$. in London, and find how much the actual time differs from the eastern time.
45. The distance from St. Pancras, London, to Belfast via Heysham is 407 miles. The train leaves the London terminus at $6 \mathrm{p} . \mathrm{m}$. and passengers land at Belfast at $6.20 \mathrm{a} . \mathrm{m}$. Irish time. Find what length of time is spent on the journey, and the average speed in miles per hour.
46. Hong-Kong is 9785 nautical miles from Liverpool via the Suez Canal, ${ }^{1}$ Colombo, and Singapore, and 13957 nautical miles via Panama, San Francisco, and Yokohama. The time of transit by the former route is 30 days. Calculate (1) the speed in knots, and (2) the time saved by going by the Suez route rather than by the Panama route (to the nearest half a day).
47. It takes 3.75 minutes to raise a steel girder by means of a derrick and to put it in its proper position in the framework

[^13]of a large building. Reckoning that the engine runs on the average $7 \frac{1}{2}$ hours per day, how many girders can be placed in position in five days?
48. A gas fire used for warming an office consumes 30 cubic feet of gas per hour. Find the cost of burning it, on the average, 9 hours a day from 25th December to 29th March, if gas is 3s. per thousand cubic feet.
49. An electric radiator consuming 1.6 units an hour gives as much warnth as the fire referred to in the previous question. If the power costs lid. a unit, what is the amount of the bill for the electrical power supplied for the quarter named? Compare this result with that of the last question.
50. The United States pays $£ 50000$ per annum in respect to its privileges over the Panama Canal; calculate the number ot dollars per day that this annual expenditure represents.
51. If the Suez Canal is 90 miles long and ships require 16 hrs .8 min . to pass through it, calculate the speed of the ships in metres per hour for the benefit of continental captains.
52. A house decorator wishes to quote for putting in a kitchen range; he reckons that he will have to put two men and a boy on the job, and that it will take 4 days of $8 \frac{1}{2}$ hours each to finish. The material will cost $£ 710$ s. all told. The first man must be paid 1 s . $3 \frac{1}{2} \mathrm{~d}$. an hour, the second $11 \frac{1}{2} \mathrm{~d}$. an hour, and the boy 5 s . He also wants to make $£ 2$ for himself. What price must he quote?
53. On some of the London tube stations a small automatic collecting-box informs us that a particular hospital needs a penny a second for its upkeep. What annual income is necessary?
54. Presuming that out of the income referred to in the previous question all but $\frac{1}{1000}$ has to be spent in the course of the first 50 weeks of the year, find the average weekly cost of upkeep of the hospital, and the extra amount necessary to leave no deficit.
55. A modern linotype machine turns out 132000 copies of a newspaper per hour. How many is this per second, and how long must the machine work to produce the whole daily circulation of lit million copies?
56. Bergen is 1018 Km . from Rotterdam. How long would it take a cargo boat travelling at 10 knots to steam from the former port to the latter?
57. A Norwegian firm proposes to inaugurate a boat service between Norway and the Pacific Coast ports, and the steamers, driven by Diesel engines, ${ }^{1}$ will run at 11 knots. What time ${ }^{1}$ Page 351 note.
must be allowed for the following runs: Southampton to New York, 3076 nautical miles; New York to Colon, ${ }^{1} 1980$ nautical miles; Colon to Valparaiso, ${ }^{2} 2650$ nautical miles?
58. The total exports of Spain to Newfoundland have increased in value from $£ 16700$ in 1910 to $£ 25500$ in 1913. Calculate the average monthly rate of increase.
59. The value of the exports from Sierra Leone to Germany in 1912 was $£ 675000$, and in 1913, £822200. Calculate the average monthly rate of increase.
60. The value of the net tonnage of British vessels entered into and cleared from Natal and the Cape of Good Hope in 1900 was respectively $£ 2,547,639$ and $£ 8,538,713$, while for them both in 1913 the value was $£ 8,422,069$. Calculate the average weekly increase or decrease in the period given.
61. Rosario is one of the principal ports in the Argentine and is connected by several railway systems with the Provinces of Santa Fé and Córdoba, which produce maize and wheat, and linseed, respectively. Given that 20000 tons of grain can be loaded in 8 hours at the port, calculate the output if the plant works 8 hours every working day for three months (reckon 365 days to a year, and allow for 13 Sundays).
62. The area of a pipe ${ }^{3}$ is $7 \mathrm{sq} . \mathrm{cm}$., and water flows through it at the rate of 350 cm . per second. How long will it take to fill a cattle trough which will hold 110 litres?
63. One pipe can deliver enough water to fill a tank in $10 \frac{1}{2}$ minutes, another in $15 \frac{1}{2}$ minutes. If they are allowed to supply water together, how long will it take to fill the tank?
64. If one pipe can deliver enough oil to fill a vat in $3 \frac{3}{4}$ hours, another in $2 \frac{1}{2}$ hours, and a third in $1 \frac{1}{4}$ hour, how long will all three of them running together take to fill the vat?
65. If, in the last question, another pipe be provided which can empty the vat in 48 minutes, how long will it take to fill it if all four taps are open?
66. A stone merchant has bought a gravel pit and has five men digging in it. Two of them working separately can each fill a cart in 45 minutes, while the other three, being less experienced workmen, can fill it in 50,55 , and 60 minutes respectively. How long will all five men working together take to load three carts?
67. A labourer can dig up 1 cwt. of clay in $15 \frac{1}{2}$ minutes, how long would it take him (to the nearest hour) to dig 5 tons 16 cwt . 2 qrs.?

[^14]68. The area of cross-section of a pipe is 0.8 sq . in., and oil flows through it at the rate of 10.5 feet per second. How long will it take to fill a tank 10 ft . by 8 ft . by 5 ft .6 in .?
69. If a steel drum be 2 ft .6 in . high and 15 in . in diameter, how long would the pipe of the last question take to deliver enough oil to fill it?
70. A pipe is 3 cm . in diameter and it is used to siphon out wine from a barrel. If the rate of flow be 630 cm . per second, find how long it will require for 500 litres to be drawn out.
71. The envelope of an airship may be regarded as cylindrical in shape, 140 feet long and 20 feet in diameter. After it has risen into the air the pilot discovers that there is a leak, and that the gas is escaping at the rate of 40 cubic feet per second. He knows that the ship cannot remain in the air with less than 12000 cubic feet of gas. How long has he to bring the vessel to anchor safely?
72. A vat of oil containing 15000 gallons is provided with three pipes, one for delivering the oil and two for running it off when it has been heated sufficiently. The bores of the pipes are 1 inch, $\frac{3}{4}$ inch, and $\frac{1}{2}$ inch respectively. The smallest one delivers 5 gallons per minute. If the vat is one-third full, how long may all three pipes be turned on before it is full? (The delivering capacity is proportional to the sectional area.)
73. If the average wages of each man referred to in Question 66 be $10 \frac{1}{2} \mathrm{~d}$. an hour, and gravel be worth 4 s . 6 d . a cart load, what must the merchant charge per load if he makes 3 s .6 d . per load for himself and charges 2 s .6 d . extra for carriage?
74. A contractor has to cut a trench in a road to lay gas mains, and he agrees to do the work in $5 \frac{1}{2}$ days. He puts five men on it and at the end of $2 \frac{1}{2}$ days finds that two-fifths has been done. How many more men must he put on to finish the job in time?
75. It is 1.14 p.m. in Cape Town when it is 4.51 p.m. in Bombay. What is the difference in longitude between these cities?
76. It is 10.12 p.m. in Prisbane (Queensland) when it is 6.59 a.m. in Philadelphia. What is the longitude of Philadelphia if Prisbane is $152 \frac{1}{2}$ E.?
77. The morning express to Fishguard leaves Paddington at 11.30 a.m., and the London express leaves Fishguard at 10.35 a.m. If the distance between the stations is 265 miles, find at what time the trains will meet if they travel at the same rate and take 7 hours on the journey. ${ }^{1}$
78. How far from London will the trains of the last question meet?
79. The distance from Liverpool to Belfast is 135 nautical miles. A cargo boat puts out from Liverpool at $10.30 \mathrm{a} . \mathrm{m}$. and travels at an average speed of 15 knots. The Irish boat leaves Belfast at 12.30 (Irish time) and steams at 20 knots. At what time will the boats be able to speak one another (Greenwich time) ?

## REVISION QUESTIONS. II.

A. (1)

## SECTION XI.

1. A merchant purchases 86.753 mgrms. of radium, but upon weighing the metal he finds he has 0.0865 gram. By what decimal of a gram is the weight he actually receives greater or less than the weight stated on his invoice?
2. A dealer in precious metals bought the following weights of gold: 5 oz. 15 dwt. 18 grs. ; 16 oz. 12 dwt. 12 grs.; 26 oz. 18 dwt. 15 grs. ; $36 \frac{1}{2}$ oz. Find the total weight purchased.
3. If half a bushel of large potatoes is added to $2 \frac{2}{3}$ pecks of small ones, what fraction of the total quantity is $2 \frac{1}{4}$ pecks?
4. What decimal of a pint of ink will an inkpot contain if 234 of them can be filled with $3 \frac{1}{1} \frac{5}{8}$ quarts of ink?
5. A grocer sells the following quantities of vinegar during the first four months of the year: 15 galls. 3 qts. 1 pt.; 18 galls. 1 qt. ; $25 \frac{1}{2}$ galls. ; 68 qts. Find, to the nearest quart, the quantity sold.
6. Calculate the value of the vinegar referred to in the last question at $5 \frac{1}{2} \mathrm{~d}$. a pint.
7. Three casks of petroleum contain respectively 86 gallons, 78 gallons, and 58 gallons. $\frac{3}{4}$ of the first, $\frac{5}{6}$ of the second, and $\frac{1}{2}$ of the third are sold. What is the value of the remainder at $8 \frac{1}{2} \mathrm{~d}$. a gallon?
8. The petrol tank on a motor-car will hold 23 gallons. The owner fills up the tank and subsequently finds that it has been leaking. He therefore drains out the petrol and finds he has only $12 \frac{1}{2}$ pints of the spirit. If the value of a gallon be 1 s .6 d ., how much has the leak cost the motorist?
9. If 1 Kilometre $=0.6213824$ mile, make out a nine-multiple
table for converting Kilometres to miles, and express 562 Kilometres, 530 metres, and 100000 centimetres in miles.
10. From the data given in the last question construct a table for converting metres into yards, and then express 375 metres in yards.
11. Express an acre as the decimal of a Hectare, given that 1 sq. metre $=1 \cdot 19603$ sq. yd., and 4840 sq. yds. $=1$ acre.
12. Captain Absolute purchased a truck of coal containing 8 tons 15 cwt. 2 qrs. at 24 s . 6 d . per ton, and was charged eleven guineas. How much more did he pay than was really due?
13. The present price of copper is $£ 652 \mathrm{~s}$. 6 d . per ton. Calculate the cost of a consignment of 3 tons 18 cwt .1 qr .18 lb . of the metal at the price given.
14. We find by referring to our newspapers that the price of copper yesterday was $£ 6415 \mathrm{~s}$. 6 d . per ton. How much would have been saved if the consignment referred to in the last question had been purchased yesterday? (Answer to the nearest shilling.) Look in your newspaper and find the price of copper to-day.

## A. (2)

1. Prepare an invoice from the following details: 7th Jan. 1914. Messrs. Wilkinson \& Co., 55 George St., Wigan. Bought of Rylands \& Son Ltd., Market St., Manchester-100 pcs. 36 in . $\times 40$ yds. white calico @ 10s. ( $£ 50$ ); 50 pcs. 30 in. $\times 40$ yds. Oxford shirting = 2000 yds. @ 6d. ( $£ 50$ ); 10 pes. $27 \mathrm{in} . \times 10$ yds. fine lawns @ 6s. (£3); 20 pcs. $30 \mathrm{in} . \times 30$ yds. foulard prints $=600$ yds. @ 5d. (£12 10s.). Total, £115 10s. Packing charges, 5s. 6d. Discount, 10 per cent. Per L. and Y. Rly.
2. Make out an invoice for the following items, vendors and purchasers being as in Question 1: 56 yds. calico, $3 \frac{8}{d}$ d. per yd.; 12 yds. unbleached calico, 3d. per yd.; 16 yds. silk, 4s. 6d.; 18 yds. merino, 2s. 3d.; 12 yds. navy serge, 2s. 6d. Receipt this invoice on 30th June 19-, using the name J. Jones, allowing a discount of 1 d . in the 1 s ., and signifying that you merely act for Rylands \& Son Ltd.
3. Prepare an invoice from the following details: The Excell Folding Box Co. Ltd., to Wilkins, James, \& Co. 5th June. Terms, 24 per cent., 1 month. Paid 30 th June. Folding boxes2 dozen $25 \times 17 \times 5 \frac{1}{2}$ at 3 s . 9 d. ; do., $30 \times 18 \times 5 \frac{1}{2}$ at 5 s .; do., $20 \times 10 \times 5 \frac{1}{2}$ at 2 s .9 d .
4. Make out an invoice for the following articles bought from Henry Smith, corn dealer, Ormskirk, by Thomas Jones: 23 trusses of hay at 2 s .6 d . per truss; $\frac{1}{2}$ cwt. mixed corn at $4 \mathrm{~s}, 1 \mathrm{~d}$.
per stone ; 700 lb . of bone meal at $£ 510 \mathrm{~s}$. per ton. Receipt the invoice, and allow ls. in the $£ 1$ discount for cash.
5. Make out an invoice for: 96 lb . tea at $2 \mathrm{~s} .7 \frac{1}{2} \mathrm{~d}$. per lb . ; 20 lb . cheese at 10 d . per lb. ; 3 cwt . sugar at $2 \frac{1}{2} \mathrm{~d}$. por lb . ; 20 lb . steak at 1 s .1 d . per lb. ; 10 lb . lamb at 1s. 3d. per lb. Prepare an adhesive receipt for this account.
6. Prepare a statement, dated 30th June, for accounts as follows: Jan. 10, £6 3s. 4d.; Feb. 6, £2 10s. 4d. ; April 15, $£ 58 \mathrm{~s} .6 \mathrm{~d} . ;$ May 8, £5 3s. 6d.; June 18, £3 5s. 8rl. ; and for which payments were made: Jan. 31 and March 31, 3 guineas each; May 30, 10 guineas.
7. Make out an invoice from the following: James \& Son, bought of Hollsworth \& Co., Golden Square, W.C. Jan. 18, 19-. Goods as under. "Fancy goods cut off to order cannot be received back." No. 5864-3 $\frac{1}{2}$ watered silk at 8 s . 9d. ; disc., 1s. $6 \frac{1}{2} \mathrm{~d}$. No. $15980-6 \frac{1}{8}$, as 6 , white drill at 3s. 9 d .; disc., 1s. 2d. No. 8123-5 dark blue at 9s. 6d. ; disc., 2s. 4 d . Pattern 8134, piece 5624, cashmere $3 \frac{5}{8}$, as $3 \frac{1}{2}$, at 6 s .6 d . ; disc., 10 d . Class No F 513, piece No. 10008, 4 tapestry at 6s. 6d.; disc., 1s.
8. Prepare a complete set of credit documents for the following, from the order being given to the receipt being sent, and make the appropriate entries in the vendor's subsidiary books:

## P. FRAQUELIP,

fisb \$alegman ant berting Curer, 1560 FISH STREET HILL, BILLINGSGATE.

July 8, 191...
Can send.
(1) Lowestoft mackerel . . 4s. 6d. per hundred
(2) Boxes mackerel . . . 5s. 6d. per box
(3) Boxes herrings . . . 4s. 0d. per box
(4) Barrels ditto . . . per barrel
(5) Salmon . . . . 2s. 6d. per $1 b$.
(6) Fresh herrings . . . per
(7) Sprinkled herrings . . per
(8) Smoked haddocks. . . per box
(9) Large boxes best kippers - 3s. 6d. per box
(10) , kippers . . 2s. 6d. per box
(11) Shrimps, red
(12)
(13) Best fillets . . . . per box
(14) Winkles . . . . 12s. per bushel
(15) Whelks

Lobsters and crals, lowest possible market prices.
If requiring, please write or wire at once.
Yours faithfully,
P. FRAQUELIP.

The quantities sent to J. Rogers, 56 Old Street, N.E., 12th July, were: 300 (1); 5 (2) ; 6 (3); $10 \mathrm{lb} .(5) ; 8$ (9); 8 (10); 3 (14). Account settled by order cheque crossed on Roberts' Bank, July 13. Returns valued at $£ 2$.

The student should work through some of the questions in Examples XXXIX. before proceeding to B. (1).
B. (1)

## SECTION XII.

1. If a yard of linen is worth 1s. 11d., and a hank contains 300 yards, find the value of a spindle of linen of 48 hanks.
2. Find the result of the previous question, taking the West of England count of 320 yards to the hank.
3. Find the cost in English money of putting down 599 miles of tram line in Russia at a cost of 500 roubles per verst. ( 1 verst $=0.66$ miles, and 1 rouble $=2 \mathrm{~s} .1 \mathrm{l}$.)
4. How many pieces of calico $3 \frac{1}{2}$ yards long can be cut from a balc $290 \mathrm{yds}$.2 ft in length?
5. How much calico will be left over in the previous question?
6. How many reels of cotton, each containing 400 yards, can be wound from half a mile of cotton?
7. If the width of a railway compartment, from the back of one seat to the back of the opposite one, is 5 ft . 2 in ., how long will a coach be which contains fourteen such compartments and a luggage van $20 \mathrm{ft} .6 \frac{1}{2} \mathrm{in}$. in length?
8. A compartment, as referred to in Question 7, accommodates five people on each seat, the length of which is 7 ft .6 in . How much space is allowed for each person?
9. Fill in the spaces in the following table for the information of continental booksellers. Size of bound books:

| Name. |  | Dimensions in Inches. | Dimensions in Centimetres. |
| :---: | :---: | :---: | :---: |
| Demy 18mo . | - . - | $59 \times 3 \frac{3}{4}$ |  |
| Large crown 8vo | - . . | $8 \times 54$ |  |
| Royal 8vo - | - . ${ }^{\text {- }}$ | $10 \times 6 \frac{1}{4}$ |  |
| Imperial 8vo | - | $11 \times 7 \frac{1}{2}$ |  |
| Crown folio | - | $15 \times 10$ |  |

B. (2)

1. The stroke of a compound locomotive engine is $25_{\frac{1}{16}}^{\frac{3}{6}} \mathrm{in}$. Express this distance in centimetres for a Roumanian railway engineer.
2. What is the diameter, in centimetres, of the cylinder of the most recent type of locomotive, given that the radius is 8.5 inches?
3. The figure shows, in plan and in elevation, a box in which eggs are imported from Denmark; find what length of


ELEVATION.
Scale, $\frac{1}{2}$ inch $=1$ foot. (Thickness is not to scale.)
$\frac{3}{8} \mathrm{in}$. wood and what length of $\frac{3}{4} \mathrm{in}$. wood is required to make the box and the cover. (The transverse pieces A, B, C, D, are in., all the rest is $\frac{3}{8} \mathrm{in}$. wood.)
4. The length from the extremity of the tail-board of a cart to the end of the shafts is $10 \mathrm{ft} .10 \frac{1}{2} \mathrm{in}$.; the length from the extremity of the tail-board to the front of the cart is $\frac{11}{2} 0$ of the whole length. What is the length of the shafts?
5. The front of a wardrobe consists of two plate-glass plates, each 15 inches in width, and they occupy together $\frac{7}{12}$ of the front; find the width of the wardrobe and the width of the woodwork part of the front.
6. The distances from London to Dover and Dover to Ostend are in the ratio of 1.07 to 1 . If the latter is 98 Kilometres, find the former.
7. Express the distances in the previous question in miles.
8. $A B$ is the wall of a house 28 feet high, $B C$ is a ladder 34 feet long. How far must it be placed from the lower part of the house $A$ in order just to reach to the top of the house?

9. $A B$ and $C D$ are two scaffold poles 10 feet apart and 30 ft .6 in . high. What must be the length of the cross pieces AD and BC?

> B. (3)

1. A merchant has five triangular shelves in the corner of his office placed at heights of $25 \frac{1}{2}$ inches above one another. The edges of the shelves next to the walls are 18 inches long. Find the dimensions of a door which has to be put up so as just to reach from the first shelf to the fifth, and cover them all in front.
2. In employing the ferro-concrete method of constructing buildings a large derrick is mounted on a platform supported by three rectangular frames. If $A, B, C$ represent, in plan, the three supports, and the triangle $\triangle B C$ the platform, find the length of $A B$ and $B C$, which are equal, if $A C$ is 85 feet.

3. Estimate the cost of placing chairs 15 inches wide around a bandstand at a seaside resort, given that the bandstand is 30
feet across, that there is a clearance of 10 feet all round between it and the row of chairs, and that each chair costs 7 s .6 d .
4. What length of single track rails will be required for a curve of radius 3765 feet, if its length is $\frac{1}{50}$ th of the circumference of the circle of which it forms part?

Note.-The inner rail will not be quite as long as the outer, but we can regard them as being of equal length for the purpose of this question.
5. What does it cost to make the iron band for a cart wheel $3 \mathrm{ft} .6 \frac{1}{2} \mathrm{in}$. in diameter at $5 \frac{1}{2} \mathrm{~d}$. a foot?
6. A builder finds that he has to use on the average 63 ft . 8 in . of $\frac{8}{8}$-in. gas-pipe in each house he erects. What is the total length of pipe used in building a row of twenty houses?
7. What would the pipe referred to in the previous question cost for the twenty houses at $3 \frac{3}{4} \mathrm{~d}$. per foot?
8. The flexible wires (usually called "flex") by which electric lamps are hung in the ordinary way in houses costs 2 s . 3 d . per dozen yards. If it requires 2 ft .6 in . of flex for each lamp, find the number of lamps which can be hung with 3 dozen yards of wire, and the cost of the flex for each lamp.
9. Allow 2s. 9d. as the cost of the lamp, 4s. 6d. per halfdozen as the cost of shades, and reckoning that an electrician can hang five lamps an hour, earning thereby 1 s . $1 \frac{1}{2} \mathrm{~d}$., calculate the cost of hanging twelve lamps, including cost of material and labour, expressing the result in francs for the convenience of a French customer.

## B. (4)

1. Convert the following distances into Kilometres for a French traveller: London to Brussels, 231 miles; London to Plymouth (rail), 225 miles; London to Cologne (via Harwich), 351 miles. ( 100 Kilometres $=62$ miles.)
2. The Diario Oficial (Santiago) publishes a decree by virtue of which a railway 23 Kilometres long, with a gauge of 1.435 metres, may be built to connect up two iron mines in Chile. What will be the length of the railway in miles and the decimal of a mile, and the gauge in feet and the decimal of a foot?
3. The Tay Bridge, which is the longest in the world, is 2 mi . 73 yds. long. How long would it take the engine of a train travelling 30 miles an hour to cover the length of the bridge?
4. The population of the United States is $91,972,000$, and there are 255 thousand miles of railway. What length of railway is there per thousand of the population in the United States?
5. Taking the population of the United Kingdom as 46 millions, and the total length of its railway system as 23420 miles,
find the length of railway for every thousand of the population. Comment on the results of this question and of the last.
6. Large manufacturers in the north of England sell readymade skirts. If each one requires $3 \frac{5}{8}$ yards of material, how many skirts can be made from half a mile of cloth?
7. If the manufacturer in Question 6 buys the cloth at 13.8 d . per yard, pays 1 ls . for making, and sells each skirt for 6s. 11d., what profit does he make on every gross of skirts that he sells?
8. If a woman takes $3 \frac{3}{4}$ hours to make one of the skirts referred to in the last question, and it costs her $1 \frac{3}{5} \mathrm{~d}$. to provide odds and ends at wholesale price, what does she earn per hour, and what could she earn per week, working 10 hours a day for 6 days?

## C. (1)

## SECTION XIII.

1. What must be the area of a desk in order that it may be prssible to place a drawing-board, $23 \mathrm{in} . \times 16 \mathrm{in}$., upon it and have 2 inches to spare all round?
2. A glazier provides glass, putty, and sprigs, and puts in the glass for $10 \frac{1}{2} \mathrm{~d}$. per square foot, and he also sells glass for 3d. a square foot, always reckoning fractions of an inch as an inch. Supposing the cost of putty, etc., to be $\frac{1}{2} \mathrm{~d}$. per foot of glass, how much does a shopkeeper save by buying the material and putting in a pane of glass $19 \frac{3}{4} \mathrm{in} . \times 29 \frac{1}{2} \mathrm{in}$. for himself, rather than employing the glazier?
3. A piece of land 50 yards by $22 \frac{1}{2}$ yards is purchased by a cinema company. The local rating authority by-laws require that a space of 1 ft .6 in . shall be left on three sides of the building, while the front must be in the same line as the ordinary frontage to the pavement. The walls of the building are to be 9 inches thick ; find the available floor space inside the building.
4. A space 16 inches by 18 inches is allowed for each person in the building described in the last question, and two gangways each 4 feet wide run the whole length of the house. What is its. seating accommodation?
5. If one-eighth of the seating accommodation referred to in Question 4 is set apart for 1 s . seats, one-half for 6 d . seats, and the remainder for 3d. seats, what amount of money is taken when the house is full?
6. The top of a window of the shape shown in the diagram has to be covered with sheet lead 5 lb . per foot super. How many square feet of lead will be required, and what will be the weight of the metal. (Allow $1 \frac{1}{2}$ square feet extra for overlapping.)
7. One of the large parks of London is shown diagrammatically in the figure. Calculate its area in square miles (to two decimal places) from the dimensions given. (Assume both shaded angles to be right angles.)

$1^{15 / 32}$ miles

C. (2)
8. The radius of the bottom of a tin, cylindrical in shape, is 1 inch, and it holds $\frac{1}{4} \mathrm{lb}$. (net) of cocoa. What must be the radius of the bottom of a half-pound tin of the same height ?
9. The circumference of a motor tyre measured over the studs is 990 mm ., and the thickness of the inflated tyre (i.e. the distance between the outer surface of the studs and the rim of the wheel) is 5 cm . What is the radius of the wheel to which the tyre can be fixed?
10. A room is 18 ft .6 in . by 12 ft .9 in ., and it contains a circular table 5 ft . in diameter. What fraction of the available space is occupied by the table?
11. A gardener marks out a garden as shown in diagram. Calculate the cost of gravelling the paths (not shaded) at 1s. 6d. per square yard.

12. The radius of a two-shilling piece is $\frac{9}{18}$ in., and the diameter of a shilling is $\frac{15}{18} \mathrm{in}$. Express the area of the latter as a decimal of that of the former.
13. The diameter of the top of a glass tumbler is 7 cm . and of the bottom 6 cm . What difference is there between the area of the top and that of the bottom of the tumbler in question?
14. What is the average sectional area of the tumbler referred to in the last question?
15. Milk is brought into London from Wiltshire, Hampshire, and other counties, in large cans made of tinned iron. The diameter of the top of one which we measured was 14 inches, and of the bottom 22 inches. Find the average sectional area.

## C. (3)

1. Find the cost of asphalting a road the total area of which is 0.56 of an acre at a cost of 2 s . $5 \frac{1}{2} \mathrm{~d}$. per square yard.
2. How much would it cost to plough 56 ares 50 square metres of land at a cost of 56 francs per are?
3. What would it cost to carpet a hall whose area is 136 sq. m. $50 \mathrm{sq} . \mathrm{dm}$. at $8 \frac{1}{2}$ francs per square metre?
4. What is the value of 25 Hectares 36 ares 58 square metres of forest land in Southern Germany at 350 marks per Hectare?
5. What would be the value of the timber on the land in Question 4, at 5400 marks per Hectare?
6. The area of the City of Westminster is 2555 acres, and its rateable value is $£ 6,619,069$. Find, for the information of the municipal authority at Paris, the rateable value in francs per Hectare. ( 1 Ha . equals $2 \frac{1}{2}$ acres, and 25 francs equal £1.)
7. The area of the main roads of a borough is 128 ac. 5 sq . chs. $325 \mathrm{sq} . \mathrm{yds}$. ; find the cost of watering these roads during the summer months at 5 s . per acre.
8. The area of the forests and plains in Japan Proper is $28,451,434$ chō, and the production of this area was valued at yen $102,342,867$. Determine the average value of the production in shillings per acre. (Yen $1=2 \mathrm{~s} .0 \frac{1}{2} \mathrm{~d}$., and $\operatorname{ch} \bar{\sigma}=2 \cdot 45$ acres.)
9. If $8,592,300 \mathrm{kwan}$ of tea were produced from 30060 chō, find the number of tons per acre. (Kwan $=8.27 \mathrm{lb}$. Av.)
10. The Dominion of Canada, which became a British possession in 1763, has an area of $3,729,700$ square miles ; express this area in Hectares, and find how many times it is larger than France, the area of which is 51 million Hectares.
11. The total yield of grain in Russia last year was $55,167,000$ tons, and the rate of yield was 560 lb . per acre. How many square miles were under grain in Russia last year?
12. There are two large wrought-iron gates, giving entrance to an important building in Westminster. Find the area of each gate from the dimensions given, and calculate the cost at 15 s .9 d . per square foot.


## SECTION XIV.

1. At a particular barracks the soldiers are provided with small steel lockers, 2 ft .6 in . long, 1 ft .6 in . wide, by 15 in . deep. What space will be required to provide locker accommodation for 250 men?
2. A large crucible placed over a furnace contains molten glass. The average dimensions of the crucible are 5 ft .6 in . by 4 ft .3 in . by 2 ft .6 in . If a square foot of glass, $\frac{1}{18}$ inch thick, is retailed at 3 d ., what is the retail value of the contents of the crucible?
3. A steam hammer consists of a block of steel 3 ft .6 in . by 2 ft .6 in . by 2 ft .6 in . Find its weight, if steel is 7.75 times heavier than water, a cubic foot of which weighs 62.32 lb .
4. The specific gravity of indiarubber is 0.95 . Find the weight, in Kilograms, of a piece 25 cm . by 18.5 cm . by 2.5 cm .
5. What would be the weight of a piece of rubber 18 in . by 15 in . by 3 in .? Does it take you longer to work this question than the last, if so, why?
6. What is the value of the rubber of the last question at 2s. 9d. per lb. ?
7. How many ounces (Av.) of benzine are there in a half-pint, if its specific gravity is 0.8 ?
D. (2)
8. A watering-can is circular in plan and its diameter is 1 ft . 2 in ., while its height is 1 ft .9 in . How many cubic feet of water will it hold?
9. How many gallons of water will a nurseryman pour on to some tomato plants if he has to empty the watering-can referred to in the last question twenty-five times in order to water them properly?
10. Water flows through a garden hose-pipe at the rate of five gallons in three minutes. If it is allowed to "sprinkle" a lawn for $8 \frac{3}{4}$ hours, how many gallons of water will have been used?
11. A commercial traveller drives about to his various customers in a carriage, the dimensions of which are 6 ft .6 in . by 4 ft .3 in . by 4 ft .6 in . If he allows $11 \frac{1}{2}$ cubic feet for himself, what space remains for his boxes of samples?
12. A room is 20 ft . by 18 ft . by 14 ft .6 in . What fraction of the whole space is occupied by a case 10 ft . by 5 ft . by 2 ft .6 in. ?
13. A stack of squared timber measures 80 ft . by 30 ft . by 25 ft .6 in . How many loads does it contain, reckoning 50 cubic feet to a load?
14. How many cubic feat of cast-iron are there in a ton if the specific gravity of the iron is $7 \cdot 2$ ?
15. The internal dimensions of a covered rectangular box are 18 in . long by 15 in . wide by 12 in . deep, and the external 20 in . hy 17 in . by 15.6 in . What is the thickness of the wood at the sides and at the top and bottom, and how many cubic feet of wood are there?
16. The average length, width (beam), and draught of a ship are $150 \mathrm{ft} ., 12 \mathrm{ft} .6 \mathrm{in}$., and 10 ft .6 in . respectively. What is its displacement, reckoning 35 cubic feet to the ton?

## D. (3)

1. A cistern is 1.75 m . long and 80 cm . broad. If there are 189 litres of water in it, find the depth of the water.
2. A French merchant wishes to export goods by a British ship, and he knows that a shipping ton is 40 cubic feet (for merchandise). Find what may be the greatest height of a case, 85 cm . long and 75 cm . wide, in order that it may not exceed one shipping ton.
3. How many cubic metres are there in a shipping ton?
4. The average diameter of a particular kind of orange is 6.5 cm ., and the fruit is arranged in a case in six rows of thirty in a row. Find the dimensions of a case which will contain 900 such oranges.
5. The Government of India has undertaken irrigation work In the Punjab for the purpose of developing the land in that
province and of affording peaceful employment for the people. To this end the great Chenab Canal has been constructed. It is 250 feet wide and 11 feet deep. Find how many times the sectional area of the canal is greater than that of the front of an ordinary dwelling-house in England, $25 \frac{1}{2}$ feet long and 30 feet high.
6. A warehouse, the dimensions of which are 55 by 25 by 20 feet, is heated by means of hot water radiators, consisting altogether of thirty-six tubes, ${ }^{1}$ the average surface area of each of which is 400 square inches. Calculate the number of cubic feet in the room for every square foot of heating surface.
7. Using the result of the last question, find the number of radiator tubes necessary to heat (1) an office, $25 \times 28 \times 22$ feet; and (2) the foyer of a theatre, $36 \times 28 \times 25$ feet.
8. A motor bicycle is packed into a skeleton crate for shipment from London to Spain. Calculate from the dimensions given (allowing 2 inches extra on the length, breadth, and height for clearance and packing) the decimal of a shipping
 ton that the crate would occupy, and calculate the cost of shipment (f.o.b.) at 15s. per ton.

## E. (1)

## SECTION XV.

1. A tea merchant buys three chests of tea each containing $80 \mathrm{lb} .$, and he pays $£ 8, £ 10$, and $£ 12$ respectively for them. He wishes to sell the whole quantity at a profit of $2 \frac{1}{2} \mathrm{~d}$. per lb . What must be the selling price per pound?
2. 4 cwt. of Demerara sugar is purchased for 30 s . per cwt., mixed with 128 lb . of sand, and sold at 6d. per $2-\mathrm{lb}$. bag; what is the profit per pound?
3. 56 gallons of spirit, costing 20 s .6 d . a gallon, are mixed

[^15]with 38 gallons at 24 s . 6 d . a gallon; what must be the selling price per pint in order to gain £20 on the whole quantity?
4. Last year the silver production of Queensland was 604979 oz., valued at $£ 68438$; and the figures for the year before were 569181 oz . and $£ 66188$. Did the average value of 1 oz . of silver vary from one year to the next, and if so, by how much?
5. The domestic production of silver in the United States amounted to $67,929,700$ ounces fine in 1914, and the value of this was $37,225,000$ dollars. Calculate the price per ounce in English money, reckoning 4s. ld. to a dollar, and compare with the result of Question 4.
6. The Russian Ministry for Finance is said to be considering a Government monopoly in tea. If the Government carries out its proposals it appears that about 5 million poods of tea would be bought annually by the Government at 10 roubles per pood. English firms can reckon that the retail price would be 1s. 8d., 2 s . 6 d ., or 4 s . 7 d . per Russian pound ( $14 \frac{1}{2} \mathrm{oz}$. Av.). Calculate the net revenue in roubles and in pounds sterling, presuming that the selling price of the tea per pound is the average of the prices given. ( 1 rouble $=2 \mathrm{~s} .1 \frac{1}{3} \mathrm{~d} . ; 1$ pood $=36 \mathrm{lb}$.)

## E. (2)

1. There is a demand in Venezuela (according to consular reports) for cotton knitted goods. Last year 179533 Kgm ., valued at $£ 47710$, were imported. What was the value of the imports per pound in English money?
2. In a month 38576 bars of soap were issued to the Army. If a bar of soap weighs 1 lb ., calculate in tons and hundredweights, correct to 1 cwt., the weight of the soap.
3. Calculate the monthly cost of the soap at 3d. per pound. (Question 2.)
4. The weight of brass in a rifle cartridge is $184 \frac{1}{2}$ grains. If 26 million are fired each day and $\frac{1}{20}$ th of the metal is recovered, find to the nearest ton the weight of metal lost per diem.

5 It is estimated that the consumption of imported sugar in South Africa is 2000 tons per annum. Taking the population as $5,973,000$, find to the nearest pound the consumption per head per annum.
6. Tenders are invited in Egypt for the supply of 12000 okes of oil for Diesel engines. ${ }^{1}$ Taking 1 cubic foot of the oil as weighing

[^16]50 lb. Av., calculate the number of gallons of oil which must be contracted for. ( 1 oke $=2.5 \mathrm{lb}$. Av.)
7. 147.5 tons of tin oxide valued at $£ 16823$ were obtained by crushing 14455 tons of ore. Calculate the number of pounds (to two decimal places) of tin oxide obtained per ton of ore, and the value (to the nearest penny) of 1 cwt . of tin oxide.
8. Naphtha has been discovered in Southern Italy at a depth of 400 metres, and the well appears to be very deep and ahle to yield 2000 litres per day. Express the depth of the well in fathoms, and the monthly yield in gallons, reckoning thirty days to the month. ( 1 litre $=1.761$ pint.)
9. In consequence of the acreage under wheat having been reduced, the New Zealand Government has imported 500000 bushels. What is the retail value of this importation at 40 s . per quarter?
10. France exported to Canada last year 37420 gallons of olive oil (for soap manufacture or for canning fish), which was valued at 53677 dollars. What was the value per pint to the nearest penny? ( 1 dollar $\left.=4 \mathrm{~s} .1 \frac{1}{4} \mathrm{~d}.\right)$
E. (3)

1. In the egg boxes referred to in Question 3, B. (2), page 342, it was found by actual weighing that the average weight of nails per box was 12.75 oz . How many boxes could be nailed up with 1 cwt. of nails?
2. From the data of the last question, find, as the decimal of a Kilogram, what weight of nails is used for each bnx.
3. A particular Cornish mine recently sold $12 \frac{1}{2}$ tons of tin ore for $£ 124617 \mathrm{~s} .6 \mathrm{~d}$.; what was the average price per hundredweight?
4. On the same day (Question 3) $205 \frac{3}{4}$ tons of tin ore were sold for $£ 19892$. Find the average selling price per hundredweight of ore.
5. A "bottle" of mercury contains 84 lb ., and on looking in the paper we find its price is $£ 125 \mathrm{~s}$. a bottle; what is the price per pound?
(The student should look up the price of mercury in his own paper and see whether it has advanced or declined since the question was set.)
6. $£ 1 \mathrm{E}$, i.e. an Egyptian $£ 1$, weighs 8.500 grams, 875 fine; what is the actual value of the coin in English money?
7. The standard coin in use in India is the silver rupee, which is $\frac{11}{17}$ fine and weighs one tola, or 180 grs. Troy, while

1 lac $=100000$ rupees. Find the value of the silver contained in a lac of rupees at $22 \frac{7}{8} \mathrm{~d}$. per ounce.
8. $19,562,549$ centals ( 100 lb .) of wheat were exported from Australia in 1912-13, and the value of this export was $£ 6,403,237$; what was the average price per bushel of 62 lb .?
9. Wheat grown in Japan in the year 1912-13 made 11.28 yen per koku. If 1 koku $=4.96$ bushels, and 1 yen $=2 \mathrm{~s} .0 \cdot 58 \mathrm{~d}$., find the difference in price (in English money) between the average price per bushel of Japanese and of Australian wheat in the year mentioned. (See Question 8.)
10. Last year 623658 acres of land in Ontario were under barley, and produced 29.3 bushels per acre If one bushel weighs 50 lb ., calculate in tons and hundredweights the weight of barley grown in the year.

## E. (4)

1. $1,033,445,264$ kin of salt were produced in Japan in 191213 , and the value was yen $11,690,404$. What is the value of 1 lb . of salt if $1 \mathrm{kin}=1.3228 \mathrm{lb}$. Av., and 1 yen $=2 \mathrm{~s} .0 .582 \mathrm{~d}$.?
2. A 20 -yen piece of Japan weighs $16 \cdot 6665$ grams, and conlains 900 parts in 1000 pure gold ; express the value of the gold in the coin in francs. (See Question 83, page 318.)
3. The gong of a type of table-bell largely used in restaurants is $2 \frac{6}{11}$ inches in external diameter. It is hemispherical in form and made of metal $\frac{5}{22}$ inch thick. Calculate the number of cubic inches of metal used in its construction, and the weight if its specific gravity be 7 .
4. Which is cheaper, 3 -in. nails sold in London at $3 \frac{1}{8} \mathrm{~d}$. per lb., or in France at 80 centimes per Kilogram?
5. The drivers of coal-delivery carts are often furnished with a tube of iron 6 ft .6 in . long, $1 \frac{1}{4} \mathrm{in}$. in external, and $\frac{5}{8} \mathrm{in}$. in internal diameter. Calculate the weight that such a bar adds to the cart if the specific gravity of iron be 7.8 .
6. In the Commonwealth of Australia in 1913 there were $3,216,276$ acres under hay, and the production was $3,936,638$ tons. Find, to the nearest quarter, the weight produced per acre.
7. In the United States in the year 1913, 48,954,000 acres were under hay, and $64,116,000$ short tons were produced. Calculate, to the nearest quarter, the weight produced per acre in the United States, and determine, by making a comparison with the last question, how much more or less per acre the yield was in the United States than in Australia.
8. The total quantity of sea fish caught in two successive years on all Irish coasts, and the value thereof, is:

| Weight (Hundredweights). | Value ( $£$ 's). |
| :---: | :---: |
| 894144 | 306786 |
| 676392 | 294625 |

Find the price per pound in each of the two years given, tabulating the answer.
9. Find the value of the fish referred to in Question 8 in francs per Kilogram.
10. 2107 cwt. of potatoes were imported into the United Kingdom during the week ending Feb. 6, 1915. Find their retail value at 7 lb . for 6 d .
11. What is 7 lb . for 6 d . in marks per Kilogram 9
F. (1)

## SECTION XVI.

1. From the following table calculate the average time taken on a journey from London to Birmingham:

| London : <br> Time of Departure. | Birmingham : <br> Time of Arrival. | Time on Journey. |
| :---: | :---: | :---: |
| $9.10 \mathrm{a} . \mathrm{m}$. | $11.10 \mathrm{a} . \mathrm{m}$. |  |
| $9.50 \mathrm{a.m}$. | $12.48 \mathrm{p.m}$. |  |
| $11.5 \mathrm{a} . \mathrm{m}$. | $1.5 \mathrm{p} . \mathrm{m}$. |  |
| $2.35 \mathrm{p.m}$. | $4.35 \mathrm{p} . \mathrm{m}$. |  |
| $4.55 \mathrm{p} . \mathrm{m}$. | $7.50 \mathrm{p} . \mathrm{m}$. |  |

2. Taking the distance of Birmingham from London as 110 miles, and using the result of Question 1, calculate the average rate of travelling in miles per hour (to one-tenth of a mile).
3. A lift makes fifteen journeys an hour and works for 6 hours a day for 6 days a week, and the cost of running is 2 s .6 d . a day; what is the annual cost of running the lift, and the cost per journey?
4. Seamstresses are said to earn 1s. 6d. a day by making bags for a particular army. Calculate the utmost they can earn per hour, working $15 \frac{1}{2}$ hours a day.
5. A servant's wages are $£ 22$ a year, and her employer may deduct 3d. a week therefrom for her insurance. What are the net weekly wages of the servant concerned?
6. A stone crusher can crush 2 cubic metres of stone in 10 minutes. If it works for $8 \frac{1}{2}$ hours a day and 22 days and 4 half-days in a month, determine the number of cubic metres of stone it would crush.
7. My watch tells me it is 8.30 a.m. ${ }^{1}$ as the ropes are cast off the ship at Holyhead. On arriving at Dublin I find that the time by the city clocks is $12.5 \mathrm{p} . \mathrm{m}$. If Dublin is $64^{\circ}$ west of Greenwich, find the time spent on the voyage and the speed in knots, if the distance from Holyhead to Dublin is 60 nautical miles.

## F. (2)

1. Some time since, one battleship was $2 \frac{1}{2}$ leagues from another, and a torpedo boat destroyer conveyed the Admiral from one to the other. If the T.B.D. made 28 knots, how long did it take the Admiral to transfer his flag from one ship to the other (to the nearest minute)?
2. The distance from Queenborough to Flushing is 114 nautical miles. An English boat leaves Queenborough at 7.45 a.m. and steams at 15 knots. Three hours later the mailboat leaves Queenborough and steams at 20 knots. Which boat will get to Flushing first, and how long will it be there before the other arrives (to the nearest minute)?
3. It takes $2 \frac{1}{2}$ days to put down a rough track, a mile long, for tip wagons. Find to the nearest half-day how long it will take to lay down 12 mi .6 fur. 8 chs .15 yds . of track.
4. The Board of Trade returns show that in Brazil there is a tendency to deal in preserved meat frozen, or otherwise treated. One firm has a "saladero" (slaughter-house) where 50000 head of cattle and 100000 sheep can be dealt with annually. Determine how many cattle and how many sheep can be slaughtered per working day, and find the value of the carcases at 340 milreis per head for cattle and 80 milreis for sheep. (Give the result in English money at 15 milreis to the £1.)
5. Taking the data of Question 4, page 351 E. (2), determine the weight of metal lost between January 1 and April 23, 1915 (to the nearest ton).
6. A reservoir contains 900 million gallons of water and supplies a town of 120000 inhabitants. What must be the daily consumption per person to the nearest gallon in order that the water may hold out from June 24 to September 2 and leave 250000 gallons in the reservoir?

[^17]7. A self-emptying cistern is 2 ft .6 in . by 1 ft . by 10 in ., and the diameter of the section of the siphon pipe within it is $1 \frac{1}{2} \mathrm{in}$. If the water flows out at the rate of 20 ft . a second, how long will it take to empty the tank, presuming no water flows in during the process?
8. A merchant has an electric radiator in his office which costs him $1 \frac{1}{2} \mathrm{~d}$. per hour. It is switched on at 9.30 a.m. and switched off at 6.30 p.m. every day but Saturdays, when it is not run after 1.30. What should be his quarterly account?
9. The pumps on a ship can pump out 2000 gallons a minute, and the ship having been holed has made 5000 gallons of water before the pumps can be got working. The influx of water is at the rate of 150 gallons a second, and the ship will sink when she has 100000 gallons in her. How long have the crew to get their boats out and equipped ?

## SECTION XVII

## PROPORTION

221. In the succeeding pages we shall attempt to show the great variety of uses to which both

> PROPORTION and
> PEROENTAGES (Section XVIII.)
can be put in commercial operations,

## A. (1) a. Direct Proportion

222. The price paid for a consignment of tea depends on the number of chests included therein.

If 1 chest costs $£ 710 \mathrm{~s}$., 2 chests will cost $£ 15$, and so 50 chests will cost $£ 375$.
$\therefore$ the price of the consignment is proportional to the number of chests of tea dispatched.

Example 1.-Two chests are filled with tea in the proportion of 3 lb . in the former to 5 in the latter, which contains 55 lb . How much does the former contain?

The first contains $\frac{8}{6}$ of the weight in the second; or $\frac{8}{8}$ of 55 lb ., which equals 33 lb .

Example 2.-The ratio of lead to tin in a particular kind of solder is as 1 to 2 . How many pounds of tin will be needed if $\mathbf{2 8} \frac{1}{2} \mathbf{~ l b}$. of lead are used?

There is twice as much tin as lead. $\therefore$ if $28 \frac{\mathrm{lb}}{}$. of lead are used, $56 \frac{1}{2} \mathrm{lb}$. of tin will be required.

Example 3.-A coal merchant sells 58 tons of coal for $£ 55$. At what price must he sell 264 tons to make the same profit per ton?

We employ the unitary method, which consists in finding the cost of one ton and then of 264 tons.

58 tons of coal cost $£ 55$

$$
\begin{aligned}
& 1 \text { ton costs } £_{\overline{58}}^{55} \\
& \therefore 264 \text { tons cost } £_{\overline{58}}^{55} \times 264 \\
& = \\
& =£ 250, \text { to the nearest } £ 1 .
\end{aligned}
$$

Example 4.-The ratio of the population of Australia (exclusive of full-blooded aboriginals) in 1912 to that in 1913 was as $1: 1.0296$. The population in 1912 was 4,730,000. Find, to the nearest ten thousand, the population in 1913.

The population in 1913 was 1.0296 times as great as that in 1912;

$$
\begin{aligned}
\therefore \text { the population required } & =4,730,000 \times 1 \cdot 0296 \\
& =4,870,000 .
\end{aligned}
$$

Example 5.-The cost per ton of conveying some agricultural products from Para to Liverpool is 40s. per ton, and the freight charge to Havre bears to that to Liverpool the ratio of 7:8. Calculate the freight per ton from Pará to Havre in French money, at 1 franc $=9.5 \mathrm{~d}$.

Freight per ton, Pará to Liverpool $=40 \mathrm{~s}$.

$$
\begin{aligned}
" \quad \text { Havre } & =\frac{7}{8} \text { of } 40 \mathrm{~s} \\
& =35 \mathrm{~s} \\
& =\frac{35 \times 12}{9.5} \text { francs } \\
& =44.2 \text { francs. }
\end{aligned}
$$

## B. Inverse Proportion

223. The greater the number of men employed in repairing a bridge the shorter will be the time required to do the work. If, for example, 150 men can paint it in 5 days, then 300 men can do it in $2 \frac{1}{2}$ days. We say, then, that the time taken to do a
piece of work is inversely proportional to the number of men employed.

Example 1.-A railway company employs 36 men to repair the permanent way, and they take $2 \frac{1}{4}$ days. How many days will 45 men take?

Employing the unitary method as before, we have:
36 men do the work in $2 \frac{1}{4}$ days
so that 1 man does the work in $2 \downarrow \times 36$ days
$\begin{aligned} \therefore 45 \text { men will do the work in } \frac{2 \frac{1}{4} \times 36}{45} \text { days } & =\frac{9}{4} \times \frac{9 \%}{45} \text { days } \\ & =1 \frac{4}{5} \text { day. }\end{aligned}$
Example 2.-A farmer can feed 50 cows for 3 weeks for £15. He buys 25 cows more. How much does it cost him to keep them for 1 month?

50 cows kept for 3 weeks cost $£ 15$

| 1 cow | " | 3 |  | $£_{50}^{15}=£ \frac{3}{10}$ |
| :---: | :---: | :---: | :---: | :---: |
| 75 cows | " | 3 " |  | $\underset{\substack{2}}{3} \times \frac{15}{\pi / 5}=£_{2}^{45}$ |
| 75 " | " | 1 week |  | $£^{2 \times 3}$ |
| $\therefore 75$ " | " | 4 weeks |  | £30. |

## EXAMPLES. LX.

1. 56 bottles of port cost $£ 114 \mathrm{~s}$., what will 10 dozen cost ?
2. Rice is sold retail at 7 lb . for 1 s ., find the cost of 1 cwt .
3. A french polisher in Cape Town can earn 50s. a week for an eight-hour day and half a day on Saturday. What does he earn per hour to the nearest farthing?
$\not 4$. The ratio of the height of a column to its diameter is $16: 1$. What will be the height of a column the circumference of which we measure and find to be 66 feet?
4. A dairyman purchases daily 28 churns of milk (each of which contains, on the average, 17 gallons), and he pays 3d. a quart. What should he pay for 83 churns of the same capacity?
5. The wholesale price of dried fruit bears to the retail price the ratio of $6: 11$. What is the retail price of a consignment which costs $£ 20$ wholesale?
6. If sugar costs, wholesale, 32 s .6 d . per bag of 112 lb ., what must be the retail price per 14 lb . to gain $\frac{1}{16} \mathrm{~d}$. per lb .?
7. A motor-car costs $£ 600$ and loses value as follows: $\frac{1}{8}$ of its original value the first year, $\frac{1}{2}$ of the reduced value the next, $\frac{1}{6}$ of that value the next, and $\frac{1}{6}$ of that value the next. Express its value at the end of the fourth year as a fraction of its original cost.
8. A contractor puts 15 men on a job and they finish it in 8 days. How many days would 25 men have taken, reckoning that they all work at the same rate?
$\not \subset 10$. The ratio of yen 1 to a United States dollar is as $68 \cdot 055: 137$. If the value of a dollar is $4 \mathrm{~s} .1 \cdot 32 \mathrm{~d}$., find in English money the value of yen 1, to one-tenth of a penny.
X11. The area of the British possessions in the West Indies is to the area of the possessions in Europe as $0 \cdot 10123: 1$. If the former is 12300 square miles, find the latter, to four significant figures.
$x$ 12. If in soldering up the lead over a bay window a plumber uses 9 lb . of solder, how much tin does he use, and what is its value at $£ 142$ per ton, if the solder contain one part of lead to two parts of tin? ${ }^{1}$
9. The value of wool (scoured) exported from Australia in 1913 (eight months) was $£ 2,574,000$, and in $1914 £ 2,624,000$. If the same rate of increase obtains for 1915, estimate the value of the exportation for that year. ${ }^{2}$
×14. In the year 1913 Southern Rhodesia produced 689954 oz. of gold, valued at $£ 2,903,270$. If the same rate held good for 1914, what was the value of the 854480 oz. produced in that year? (The actual value in 1914 was $£ 3,580,210$.)
10. Southern Rhodesia ${ }^{8}$ also produces the thermal insulator,
${ }^{1}$ This is the composition of soft solder. Hard solder contains-copper 40 , zinc 60 : and jeweller's solder-fine gold 5 , copper 2, zinc $1 \frac{1}{2}$, fine silver $1 \frac{1}{2}$.
${ }^{2}$ In all such questions the student must be careful to take a sufficient number of figures in multiplication or division to ensure the degree of accuracy required in commercial operations. Here the answer correct to £1000 would be sufficiently close.
${ }^{8}$ The most important productions of Southern Rhodesia, after gold, are chrome iron ore and coal.
asbestos. The value of the 487 tons produced in 1914 was £8612. What was the value of the 290 tons produced in 1913, supposing the market did not change from 1913-14? (The actual value was $£ 5224$, how was the market going?)
11. The Governor of the Falkland Islands reports that 221930 barrels of oil were produced from 4544 whales caught in 1913-14 off the South Shetlands. If 621 whales were caught off the South Orkneys, what should have been the number of barrels of oil produced if the whales were as productive of oil as those off the South Shetlands? (Actual number of barrels produced by South Orkneys whales was 21750 ; draw conclusions.)
12. If the approximate value of 21750 barrels of whale oil is $£ 87000$, what is the value of 221930 barrels?
13. 654650 cwt. of plumbago valued at $£ 556450$ were exported from Ceylon in 1912-13, and 570810 cwt. in 1913-14. What was the value of the latter if the value per hundredweight was the same as in 1912-13? Is the plumbago market rising or falling if the actual value was $£ 603150$ ?
14. The Commonwealth of Australia imported $2,966,000 \mathrm{lb}$. of coffee and chicory in 1912, valued at $£ 117170$, and $3,174,900 \mathrm{lb}$ in 1913. Find the value of the latter. (Market steady.)
15. Japan produced $2,725,260 \mathrm{kwan}$ of steel in 1911, and $3,309,520 \mathrm{kwan}$ in 1912. If the value of the latter was yen 745800 , find the value of the former.
$\checkmark$ 21. A drum of oil is 14 in . in diameter, 2 ft .6 in . high, and it is worth $£ 715 \mathrm{~s} .6 \mathrm{~d}$. What should a drum 18 in . in diameter and 3 ft . high be worth, to the nearest sixpence?
16. If 10 metres of silk are sold in Paris for 38 francs, how much should be paid in London for 6 yards?
17. France exported to the Dominion 260850 lb . of cheese, valued at 55450 dollars, last year, and 102100 lb ., valued at 22200 dollars, the year before. How is the market moving?
$j 24$. A contractor puts 20 men on to repair a road, reckoning that they will finish it in 15 days. At the end of 10 days he puts 12 more men on. In how many more days will it be finished?
18. If each of the 12 men of the last question were able to work half as quickly again as each of the original 20 , how many days would it have taken to finish the work after they were put on?
19. A builder agrees to finish a hospital by June 1, or to forfeit 50 guineas a day for every day, or part of a day, after that date. On May 15 he reckons that the 85 men he has on it will finish it by June 15. How many more must he put on to finish it in time?
20. If the builder in the last question had put on 8 men more, how much would he have been fined?
21. The Customs revenue of Australia for the first two months of the financial year $1914-15$ was $£ 2,526,000$; estimate the revenue for the year and determine by how much it will be greater or less than the total for 1913-14 if it amounted to $£ 9,114,000$ for the first eight months.
22. A quantity of gas for lighting railway trains occupies 10000 cubic feet at the ordinary atmospheric pressure of 14 lb . per square inch. It has to be compressed into a cylinder 15 feet long and 7 feet in diameter for conveyance by rail. What pressure will it exert on the cylinder if the volume is inversely proportional to the pressure?
23. Hong-Kong is 9834 miles from London, via the Suez Canal, and the time of transit is 29 days. By how many miles per hour would it be necessary to increase the average speed to deliver the mails 12 hours earlier?
24. A ship is crossing the Atlantic and the steam pipe bursts. There are 350 men on board, with food enough to last 11 days. To be on the safe side, the captain cuts down rations so that the food will hold out for 25 days. If the original weight of food was 10 tons, by how much must each man's allowance be cut down?
25. A draper has 25 high-power gas burners outside his shop, and each burns 30 cubic feet of gas in $2 \frac{1}{2}$ hours. He does away with them and installs 8 new ones, the power of each of which is 2.75 times greater than each of the others. In what time will they coysume the same quantity of gas?
26. The caterers on a dining-car train provide food on the assumption that 150 people will take tickets for lunch. As a matter of fact, 196 people take tickets, and the size of the portion given to each is consequently reduced. If the actual value of the lunch was 2 s . per person under ordinary circumstances, what would be the value of the reduced lunch ?
27. If there were 38 boys in the workhouse with Oliver Twist, and each was allowed half a pint of "thin gruel," how much less would Oliver have had if there had been 57 boys there?
28. A battle cruiser can cover 1000 nautical miles in $40 \frac{1}{4}$ hours ; by how many knots must its speed be increased to cover the distance in 38 hours ?
29. If 385 men can turn out $£ 10000$ of munitions of war in $5 \frac{1}{2}$ days, how many men would have to be employed to turn out £35500 worth in 22 days?
30. A mason employs 36 men who build a wall in 10 days of

6 hours each ; how many men would be required to do the work in 7 days of 8 hours each?
$\cup 38$. How many cubic feet of gold of specific gravity 19.32 are equal in weight to 0.58 cubic foot of platinum of sp. gr. 21.45 ?
$\checkmark$ 39. If 28 miners dig 15 metric tons of coal in $8 \frac{1}{2}$ hours, how many metric tons will 100 miners dig in 3 days of $5 \frac{1}{2}$ hours each?
40. If a continental express covers 400 Km . in $4 \frac{1}{2}$ hours, by how much must its speed be increased or decreased so that it may cover 88 feet in 1 second? ( $100 \mathrm{Km} .=62$ miles.)
41. A tank containing 500 litres supplies a house with water, and it is provided with two pipes of diameter 3.5 cm . and 4.5 cm . If the first is used for emptying the cistern it takes 25 minutes. How long would it take using (1) the other pipe alone, (2) both pipes?

## A. (2) Temperature

224. Among the many matters to which a merchant has to give his attention we must include the temperature of his warehouses and offices. There are three scales of temperature, named the Centigrade (C.), the Fahrenheit (F.), and the Reaumur (R.).

The standard temperatures are those of melting ice, FreezingPoint, and of steam, under atmospheric pressure, Boiling-Point, and they are marked $0^{\circ}$ and $100^{\circ} \mathrm{C}$., $32^{\circ}$ and $212^{\circ} \mathrm{F}$., and $0^{\circ}$ and $80^{\circ} \mathrm{R}$.
225. A thermometer was invented by Galileo in 1592, and a greatly im. proved kind of instrument was made by Fahrenheit, 1714. The zero point of the latter was fixed by inumersing the instrument in a mixture of ice, water, and sal-ammoniac : the $32^{\circ}$ point by inmersing it in a mixture of ice and water; a third point, "blood heat," by placing the thermometer in the armpit of a healthy man ; a fourth, by placing it in steam at atmospheric pressure. The interval between the $32^{\circ}$, freezing-point, and the $212^{\circ}$, boiling-point, was divided into $180^{\circ}$ to correspond with the number of degrees in a semicircle !

Celsins, a Swedish astronomer, invented the Centigrade thermometer (c. 1740), and graduated it very conveniently from $0^{\circ}$ to $100^{\circ}$.

Réaumur, a French scientist, made the thermometer which bears his name in 1731. He also performed experiments in artificial incubation and on the making of steel.
226. It is clear that a range of $100^{\circ} \mathrm{C}=a$ range of $80^{\circ} \mathrm{R}$., and that any conversion from one to the other is simply a matter of proportion.

The conversion from, or to, $F$. is more difficult, but it depends upon the fact that $0^{\circ} \mathrm{C}$. and $32^{\circ} \mathrm{F}$., are corresponding temperatures (namely, the freezing-point of water), while $0^{\circ} \mathrm{C}$. and $0^{\circ} \mathrm{F}$. are not. Therefore, in converting say $30^{\circ} \mathrm{C}$. to F ., we proceed as usual, taking a range of $100^{\circ} \mathrm{C} .=$ a range of $180^{\circ} \mathrm{F}$. ; find, by
proportion, the range F . corresponding to a range of $30^{\circ} \mathrm{C}$. and then add $32^{\circ}$.

Thus-
Example 1.-Convert $30^{\circ}$ C. to F.
Here a range of $100^{\circ} \mathrm{C} .=$ a range of $180^{\circ} \mathrm{F}$.
$\therefore$ a range of $30^{\circ} \mathrm{C}$. above freezingpoint $=$ a range of $\frac{180}{100} \times 30$ or $54^{\circ} \mathrm{F}$. above freezing-point F., that is to say, above $32^{\circ} \mathrm{F}$.
 or a range of $30^{\circ} \mathrm{C}$. $=$ a range of $54^{\circ}+32^{\circ}$, or $86^{\circ} \mathrm{F}$. above $0^{\circ} \mathrm{F}$.
227. Example 2.-Express $62^{\circ}$ F. in C. degrees.

In converting $62^{\circ} \mathrm{F}$. to C . we say that $62^{\circ} \mathrm{F}$. is $30^{\circ}$ above the $32^{\circ} \mathrm{F}$., that is, above the freezing-point F ., and, therefore, we convert not $62^{\circ}$ but $62^{\circ}-32^{\circ}$ or $30^{\circ} \mathrm{F}$. to C., since of those $62^{\circ}$, $32^{\circ}$ are Below the freezing-point.

Hence, a range of $180^{\circ} \mathrm{F}$ = a range of $100^{\circ} \mathrm{C}$.
and, ", $30^{\circ} \mathrm{F}=,, 16 \frac{2}{3}^{\circ} \mathrm{C}$.
$\therefore 62^{\circ} \mathrm{F}$. corresponds to $16 \cdot 6^{\circ} \mathrm{C}$.
The following rules are convenient :
To convert any temperature to $F_{\text {., }}$ use the proportion ( $100^{\circ} \mathrm{C}$. or $80^{\circ} \mathrm{R}$. to $180^{\circ} \mathrm{F}$.), and add 32 ; and to convert from F ., subtract 32, and then use the proportion $180^{\circ} \mathrm{F}$. to $100^{\circ} \mathrm{C}$. or $80^{\circ}$ R.
228. The Centigrade thermometer is used universally for scientific purposes, the Fahrenheit for domestic, meteorological, and clinical purposes in this country, while the Réaumur is used in Russia and in some parts of Germany.

## EXAMPLES. LXI. (a)

1. Convert $25^{\circ}, 38^{\circ}, 46^{\circ}, 300^{\circ},-50^{\circ} \mathrm{C}$. to R .
2. Convert $22^{\circ}, 25^{\circ}, 38^{\circ}, 40^{\circ},-20^{\circ}$ R. to C.
3. Express $24^{\circ}, 36^{\circ}, 44^{\circ},-15^{\circ} \mathrm{C}$. in F . degrees.
4. Convert $15^{\circ}, 25^{\circ}, 38^{\circ},-10^{\circ} \mathrm{R}$. to F .
5. Convert $64^{\circ}, 112^{\circ}, 98^{\circ}, 210^{\circ} \mathrm{F}$. to C.
6. Convert $56^{\circ}, 200^{\circ},-36^{\circ}, 32^{\circ} \mathrm{F}$. to R.
7. A doctor finds the temperature of a patient to be $98^{\circ} \mathrm{F}$., what is it C.?
8. If a particular kind of porcelain melts at $1500^{\circ} \mathrm{C}$., what is ite melting-point F. 9
9. The temperature of a storage room for furs is $38^{\circ} \mathrm{F}$., what is the corresponding C . temperature?
10. Express the following melting-points in F. degrees: silver, $962^{\circ} \mathrm{C}$. ; gold, $1064^{\circ} \mathrm{C}$. ; copper, $1085^{\circ} \mathrm{C}$. ; platinum, $1710^{\circ} \mathrm{C}$.
11. The temperature of a particular form of arc lamp is $4000^{\circ} \mathrm{C}$., express this in F . and R .
12. Gunpowder ignites at $550^{\circ} \mathrm{F}$., express this in C. degrees.

## GRAPHICAL METHOD OF CONVERTING TEMPERATURES

229. We divide the horizontal line $O X$ into convenient

lengths to represent C. degrees ( 3 units $=5^{\circ}$ ) and the vertical line $O Y$ into lengths to represent $F$. degrees ( 3 units $=8^{\circ}$ ). Now, $0^{\circ} \mathrm{C}$. is the same temperature as $32^{\circ} \mathrm{F}$., and so the point $A$ is the temperature $0^{\circ} \mathrm{C}$. converted into F . In the same way $100^{\circ} \mathrm{C}$. and $212^{\circ} \mathrm{F}$. represent the same temperature;

## $\therefore B$ represents $100^{\circ} \mathrm{C}$. converted into F .

Join AB; then this line enables us to convert any $C$. temperature into F . or vice versa.

Example 3.-Express $60^{\circ}$ C. in F., using the graph.
The point $C$ represents $60^{\circ} \mathrm{C}$. Follow up the vertical through C till it cuts $A B$ in $D$. Draw a horizontal DE to meet $O Y$ in E. E represents $140^{\circ} \mathrm{F}$.

$$
\therefore 60^{\circ} \mathrm{C} . \text { corresponds to } 140^{\circ} \mathrm{F} .
$$

Example 4.-Express $160^{\circ}$ F. in C., using the graph given.
Draw the horizontal line GH through $160^{\circ} \mathrm{F}$. and drop the perpendicular HK. Then $K$ is the C. temperature corresponding to $160^{\circ} \mathrm{F}$. But K is $71^{\circ} \mathrm{C}$.

$$
\therefore 160^{\circ} \mathrm{F} . \text { corresponds to } 71^{\circ} \mathrm{C} .
$$

230. It will be seen that there is no question of adding or subtracting $32^{\circ}$ in this method, and, by taking the scale sufficiently large, the graph can be made suitable for all commercial purposes. By drawing OX along to the left, it is possible to read off temperatures below $0^{\circ} \mathrm{C}$.

## EXAMPLES. LXI. (b)

1. Construct a graph for reading off R. degrees in terms of C. degrees.
2. Use the graph to confirm the results obtained in Questions 1 and 3. (Examples LXI. (a).)
3. Draw a graph for reading off F . degrees in terms of R. degrees.
4. Employ the graph in Question 3 to test the results of Questions 4 and 6. (Examples LXI. (a).)
5. Construct a graph for reading the temperatures $94^{\circ}$ to $106^{\circ} \mathrm{F}$. in C. degrees, and use it for determining to one place of decimals how many Centigrade degrees the temperature of a patient, namely, $104^{\circ} \mathrm{F}$., is below the boiling point of water on the C. scale.

## B. (1) Capital : Partnership

231. Suppose you want a motor bicycle costing $£ 60$, it may be that you have not managed to save enough money to buy it, and so you will probably go to an intimate friend and ask him to lend you some part of the purchase money. You have in hand now a sum of money with which you do business; we will call it your Capital. ${ }^{1}$ With it you buy the bicycle and take out the necessary licences. Had you gone to any one other than a close friend you would have had to give some written guarantee for the repayment of the money, and you would also have had to pay something for the use of it. This sum we shall call INTEREST.
232. Again, suppose you have been in a business for a number of years and, having saved $£ 500$, wish to start in business for yourself, but find your capital is not enough. You say to Smith, one of your friends, "Look here, you have two hundred pounds; put it with my $£ 500$ and let us open a business for ourselves as estate agents." You and Smith agree upon this course, enter into partnersilip, and are now Partners. Suppose you make $£ 70$ profit in the first year. Since you provided $£ 500$, and Smith $£ 200$, you will take good care that he does not have half the profit, for he did not provide half the capital. You really put $£ 500$ out of $£ 700$, and he put $£ 200$.
$\therefore$ you get $\frac{500}{700}$ of $£ 70$, i.e. $£ 50$; and he gets $\frac{200}{700}$ of $£ 70$, i.e. $£ 20$.

If in the second year you make $£ 560$ profit, then you will have $\frac{5}{7}$ of $£ 560=£ 400$, and he, $\frac{2}{7}$ of $£ 560=£ 160$.
233. Let us imagine that your business has grown so that you feel justified in opening offices in other places. You may need more capital, and can do one of two things to raise it: (1) Take others into partnership with you, arranging to pay them so much a year, or a certain fraction of the profits; or (2) form a limited liability company, which we shall describe on pages 492 and 493.
234. Example 1.-Two merchants put $£ 5000$ and $£ 4000$ into a business, and the profit is $£ 3000$. What amount should each receive if the division of profits is to be in proportion to the capital supplied?

$$
\text { Total capital }=£ 9000 .
$$

The first merchant gets $\frac{5000}{80}$ of $£ 3000=£ 166613 \mathrm{~s} .4 \mathrm{~d}$. and the second $\quad, \quad \frac{4000}{8000}$ of $£ 3000=£ 12336 \mathrm{~s} .8 \mathrm{~d}$. $\therefore$ the amounts received are $£ 166613 \mathrm{~s} .4 \mathrm{~d}$. and $£ 13336 \mathrm{~s} .8 \mathrm{~d}$.
${ }^{1}$ For the means by which a Government may raise capital, aee page 374.

Example 2.-Three merchants put, respectively, £3000, £2500, and £4800 into a business on the understanding that the first shall receive $£ 300$ per annum as manager, and the second one $£ 250$ as secretary, while the balance of the profits shall be divided in proportion to the capital advanced by each. If the profits amount to $£ 1683$, calculate the amount each receives apart from salary.

| Total Profits |  |  | $=£ 1683$ |  |
| :---: | :---: | :---: | :---: | :---: |
| Amount paid in salaries |  |  |  | 550 |
| Net amount available for division $=\underline{\underline{£ 1133}}$. |  |  |  |  |
| Total Capital $=£ 10300$. |  |  |  |  |
| The first partner receives $\frac{3000}{10300}$ of £1133; |  |  |  |  |
| $=£ 330$. |  |  |  |  |
| The second | " | " | $\frac{2500}{10300}$ of £1133 |  |
| The third | " | " | $\begin{aligned} & \frac{4800}{18300} \text { of } £ 1133 \\ &=£ 528 . \end{aligned}$ |  |
|  |  |  |  |  |

$\therefore$ the amounts received apart from salary are $£ 330, £ 275$, and $£ 528$, respectively.

Example 3.-A firm of chemists is controlled by three directors, who agree to divide the profits in the ratio of 1:2:3 (read 1 is to 2 is to 3 ). What amount should each receive out of a profit of $£ 3000$ ?

If the profits were divided into 6 parts (i.e. $1+2+3$ parts) then the first director should have $\frac{1}{6}$, the second $\frac{2}{6}$ or $\frac{1}{3}$, and the third $\frac{3}{6}$ or $\frac{1}{2}$.

$$
\begin{aligned}
& \therefore \text { The first director receives } \frac{1}{6} \text { of } £ 3000=£ 500 ; \\
& \text { The second ", ", } \frac{1}{8} \text { of } £ 3000=£ 1000 ; \\
& \text { The third ", } \quad \text {; of } £ 3000=£ 1500 \text {. }
\end{aligned}
$$

Check the result by adding together the three amounts received, and seeing their sum is equal to the total profit.

Example 4.-Three merchants enter into an arrangement whereby one puts $£ 5000$ into the business for 6 months, the next puts $£ 8000$ in for 12 months, the third $£ 12000$ for 15 months. The first receives $£ 450$ as his share of the profits, what does each of the others receive?

$\therefore$ the first merchant should receive $\frac{30000}{808000}$, or $\frac{5}{51}$ of the profit. But he actually receives $£ 450$.

$$
\therefore \frac{s}{\delta I} \text { of profit }=£ 450 ; \frac{1}{\delta I} \text { of profit }=£ \frac{450}{5}
$$

and $\frac{51}{\delta}$ (i.e. all the profit) $=£ \frac{450}{5} \times 51=£ 4590$.
$\therefore$ the second merchant receives $\frac{98000}{308000}$ of $£ 4590=£ 1440$;
and the third ", $\frac{180000}{308000}$ of $£ 4590=£ 2700$.
The shares of the last two are $£ 1440$ and $£ 2700$ respectively.

## EXAMPLES. LXII.

1. Two merchants enter into partnership ; one puts in $£ 4500$, the other, $£ 3600$. At the end of the year the profit is $£ 1620$. How much should each receive?
2. If three partners agree to advance $£ 5000, £ 8000$, and $£ 7000$ respectively towards the development of a business, and the profit at the end of the first half-year is $£ 4350$, how much more would the second partner receive than either of the others?
3. The profit on a business was $£ 1300$. One partner advanced $£ 2550$, and received $£ 340$ as his share. What amount did the second partner advance?
4. Four business men agree to divide the profits of their business in the ratio of $1: 2: 2 \frac{1}{2}: 3$. If the profits were $£ 3400$ 17 s ., how much should each have?
5. In what ratio should the profits of a business be divided if the partners put money into it as follows : $£ 3000, £ 5700, £ 4500$, £6500?
6. If the profit made from the business of the last question amounted to $£ 2364$, what should be the share of each partner?
7. The profit on a business is $£ 1375$; divide it so that one partner receives twice as much as the second, and four-fifths the share of the third.
8. One partner puts $£ 350$ into a concern for 15 months,

[^18]another puts $£ 580$ into it for 18 months, a third, $£ 375$ for 12 months. Divide the profit of $£ 504 \mathrm{l} 5 \mathrm{~s}$. between them.
9. Thomas Williams advances $£ 5000$ for 3 years. Henry Jones comes into his business after 9 months and advances $£ 3000$, Jacob Joseph comes in with $£ 10000$ after 15 months. In what ratio must the profits be divided at the end of the three years?
10. If the profits of the last question were $£ 2268$, how much should Jacob Joseph receive for his contribution?
11. A landlord has a piece of land which he lets to some farmers on the understanding that they pay him in proportion to the area of their allotments. If he receives $£ 30110 \mathrm{~s}$. per annum in rent, and the areas of the allotments are $3 \frac{1}{2}, 4 \frac{1}{4}, 2 \frac{1}{8}, 5 \frac{1}{6}$ acres, determine the rent each farmer pays.
12. The land agent to a particular prince allows farmers to use some land for grazing purposes. One farmer puts 50 cattle on the land for 180 days; another, 80 cattle for 150 days; a third, 75 cattle for 200 days; and a fourth, 120 cattle for 150 days. The landlord receives $£ 2532 \mathrm{~s}$. 6 d . for his kindness after the land agent has deducted one-tenth for his expenses. How much did each farmer pay?
13. What did it cost each farmer per cow per day? (Question 12.)
14. A commercial traveller takes a ticket from London to Paris and pays 25 s . 9 d . for it. London to Dover is $77 \frac{1}{2}$ miles ; London to Calais is 103 miles; and London to Paris is 287 miles. If the various companies receive an amount proportional to the mileage run over, assign (as if in the Clearing-House) to the English railway company, to the steamboat company, and to the French company its proper amount.
15. Ascertain for the information of the Railway ClearingHouse the proportion in which a charge of 105 s . must be divided among three railway companies for the conveyance of a consignment of fruit, if the mileage on the railways was respectively 85 miles, 120 miles, and $80 \frac{1}{2}$ miles.
16. A butcher pays $£ 80$ per annum for his shop, and puts $£ 580$ capital into his business. After five months he takes in a partner who advances $£ 380$ capital. Find what proportion of the rent the latter should pay, and how much he should receive out of a profit of $£ 240 \mathrm{lOs}$. at the end of the year.
17. A forage dealer employs three men in his business. The first receives three times as much as the third, and the third half as much as the second, while the dealer himself takes as much as all three of them. Divide a profit of 144 s . 6d. a week between them.
18. Three Portuguese planters go to Brazil, where they remain for ten years and develop a vineyard. The record of their prosperity is given below. If they advance the capital of 13620 milreis in the proportion of $9: 20: 40$, and the income is divided at the end of the tenth year, calculate the amount each should receive and the profit each made. ${ }^{1}$ (Observe that no return on the capital expended is received until the fourth year.)
a VINEYARD (SOUTH BRAZIL)

| Year. | Expenses-Items. | Total Amount in Milreis. | Produce per Hectare. |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Labour, 120 ; manure, 500 ; planting, 200 ; plants, 1000 ; stakes, 250 ; administration, 360 | 2430 | - | - |
| 2 | Fencing, 1500; labour, etc., | 2150 | - |  |
| 3 | Total expenses | 1040 | - | - |
| 4 | Including wine-making . | 2000 | 5 pipes of wine of 480 litres each | 1000 |
| 5 | " " | 1000 | 10 pipes | 2000 |
| 6 | " " | 1000 | 20 , | 4000 |
| 7-10 | " " | 4000 | 80 | 16000 |
|  | Total | 13620 | 115 pipes | 23000 |

Net profit per Hectare, $£ 160$.
19. Four partners enter into business together. The first advances $£ 2500$, which he takes out at the end of 15 months; the second advances $£ 560$ for 18 months; the third, $£ 1000$ for 10 months; and the fourth, $£ 3500$ for 2 years. The profit is $£ 696 \mathrm{18s}$. ; divide it among the partners.

## B. (2) Rates

235. We who live in towns know that the Corporation is responsible for providing an efficient sanitary system, sufficient lighting, a suitable number of open spaces, and for keeping the roads clean and in proper repair. The Income necessary to perform these various duties is raised by charging each householder a certain amount of money for the privilege of living in the town. The authorities conclude that if a man can afford to live in a house rented at $£ 80$ a year, he can pay more towards the upkeep of the

[^19]town than the man who lives in a house rented at $£ 30$ a year. They therefore take (usually) $\frac{5}{6}$ of the rental and call that the Rateable Value, thus: Rental, £84; Rateable Value, $\frac{5}{6}$ of $£ 84$ or $£ 70$; and then "demand" each householder to pay a rate varying from 5 s. to 15 s. a year on every $£ 1$ in the rateable value of his house. A demand note and rates receipt are shown on Plates X. and XI. (facing pp. 372 and 373).

The rates vary with the locality, e.g. Westminster, 6s. 10d. in the $£ ;$ Birkenhead, 7 s .10 d . in the $£$.
236. It is important, in opening a business, to ascertain the rateable value of the property and the amount of the rates in the pound. Let us illustrate this:

A merchant has two offers open to him, one for premises rented at $£ 126$ per annum, where rates are 10 s . in the pound, and another at $£ 132$, where the rates are 8 s. in the pound. Which will be the cheaper?

| Cask 1. ${ }^{\text {s. }}$ d. |  | Cask 2. |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Rental | 32 | $\begin{array}{rr}\text { s. } \\ 0 & 0\end{array}$ |
| Rateable value | £105 00 | Raterble value | £110 | 0 |
| Amount of rates | £5210 | Amount of rates | £44 | 00 |
| Rent | £126 00 | Rent | £132 | 00 |
| + Rates | $5210 \quad 0$ | + Rates | 44 | 0 |
| $=$ Total annual cost | $17810 \quad 0$ | $=$ Total annual cost | $£ 176$ |  |

Hence we see that, although the rent in the second case is higher, the rates are lower than in the first, and, other things being equal, it is cheaper to open a business in the latter place.
287. We might say that the rates of a town constitute the income of the Corporation for the purposes of keeping the town in a proper and orderly manner.

It would not be possible out of the rates for one year to meet a large capital expenditure, e.g. $£ 60000$ for a park, but, by borrowing the capital, the rates can be used to pay that back in, say, sixty years, and also to pay the annual interest.

The Corporation may borrow the necessary capital, with the consent of Parliament, either by issuing stock (Section XXII.) or by executing a mortgage deed on the security of the rates, and guaranteeing a certain rate of interest, ${ }^{1}$ usually 3 to 4 per cent

For example, the Corporation of a suburban town issues to the ratepayers the following form :

## BOROUGH OF BENDON.


#### Abstract

The Corporation of Bendon are prepared to receive Loans of $£ 50$ and upwards in multiples of $£ 10$ on security of the Rates, at $£ 310 \mathrm{~s}$. per cent. per annum. Interest will be paid half-yearly on 30 th September and 31st March, and the Loans will be repayable at any time at six months' notice.

Further particulars may be obtained on application to the Borough Treasurer, Town Hall, Bendon. P. JOHNSON HICKS, Town Clerk.


238. All that has to be done in lending to the Corporation is to fill in a proper form saying that you wish to lend (e.g.) $£ 100$, and that the interest is to be paid to you. The borough treasurer then prepares a mortga*e deed on the general district rates, has it properly stamped, ${ }^{1}$ signed by the mayor and town clerk, and embossed with "the seal of the mayor, aldermen, and burgesses" of the town. It is then delivered to you, and when you wish to draw out your money you give notice and, when it is paid over to you, sign the deed declaring you have received the money, and then the Corporation receives the deed back again and oancels it.
239. Example 1.-The rental of a shop is $£ 60$ and its rateable value is $£ 50$; the poor rate is 2 s . and the district rate is 2 s . 3d. in the pound, and the "Inhabited House Duty" (payable not to the local authority but to the Government) is 4 d . in the pound on the rental. How much do the local authority and the Government receive respectively?

Poor rate $=2 \mathrm{~s}$. in the pound ; $\quad \therefore$ rates due $=£ 5$.
District rate $=2 \mathrm{~s} .3 \mathrm{~d}$. in the pound ; $\therefore \quad, \quad=£ 512 \mathrm{~s} .6 \mathrm{~d}$.
$\therefore$ Total payable to local authority $\quad=£ 1012 \mathrm{~s} .6 \mathrm{~d}$.
Inhabited House Duty $=4$ d. in the pound on Rental $=£ 1$
$\therefore$ the Government receives $£ 1$.
Example 2.-If the rates on a house amount to 557 s .6 d . per half-year, and they stand at 3 s .7 d . in the pound for that half-year, calculate the rateable value of the property and its rental if the former is five-sixths the latter.
${ }^{1}$ The amount of all stamp duties can be ascertained from Somerset House.

The problem is simply this: If 3 s . 7 d . is paid upon $£ 1$, upon what sum would $£ 57 \mathrm{~s}$. 6 d. be paid?

$$
\begin{aligned}
\text { The rateable value is } & \frac{£ 57 \mathrm{~s} .6 \mathrm{~d} .}{3 \mathrm{~s} .7 \mathrm{~d} .} \times £ 1 \\
& =£ \frac{1290}{43}=£ 30 . \\
\therefore \text { Rental } & =\frac{6}{5} \text { of } £ 30 \\
& =£ 36 \text { per annum. }
\end{aligned}
$$

## EXAMPLES. LXIII.

Note.-We shall assume rateable value $=\$$ rental, and that the rates are per annum, unless otherwise stated.

1. Calculate the amount payable annually in rates on premises of rental $£ 84$ per annum, if the rates are 8 s .6 d . in the pound.
2. Calculate the result of the last question if the rateable value is eleven-twelfths the rental, and rates 2 s .8 d . per quarter.
3. The rateable value of a warehouse is $£ 2500$. The rates for the first quarter are at 2 s . 1 d . in the pound; for the second, 2 s .; for the third, 2s. 3d. ; and for the fourth, 2 s .4 d . Calculate the amount paid in rates in each quarter and in the year.
4. Which is more remunerative, and by how much-(1) To let a row of forty-eight small houses at 12 s . 6d. a week each, inclusive ; or (2) at $£ 710$ s. a quarter, where the tenant pays the rates at 6 s .4 d . in the pound? Would the difference in the income derived clearly justify the cheaper method?
5. The rent of a store is $£ 120$ per annum, and the rates stand at 7 s .6 d . in the pound. What amount must be paid in rates?
6. The rateable value of the City of Loudon is $£ 5,717,000$ to the nearest $£ 1000$, and the rates stand at 7 s .6 d . in the pound. Find, to the nearest $£ 1000$, the income derived from the rates.
7. The rateable value of Birkenhead is $£ 696660$. What increase, to the nearest penny, must be made in the rate in order to produce $£ 8000$ more income?
8. Taking the population of Birkenhead to be 140000 , determine the average amount contributed by every five persons to the rates if they are 7 s .10 d . in the pound per annum.
9. A landlord owns two houses in different boroughs. The rent he receives is $£ 42$ and $£ 54$, and the rates stand at 7 s .8 d . and 6 s . 9 d . respectively. Determine which house is the cheaper from the tenant's standpoint.
10. If rates are 1 s .8 d . in the pound per quarter, what would
be the rental of a house which was charged $£ 2113$ s. 4 d . per annum in rates?
11. If we take the urban (city and town) population of Australia to be $2,950,000$, determine what amount of money would be produced, reckoning an average rateable value of $£ 28$ per annum per household of five people, and rates at 8 s . in the $£$.
12. A corn merchant has two shops, for which he pays $£ 80$ and $£ 98$ rent per annum. The former is in a town where the rates are 8 s .6 d . in the pound, and the latter in another town where the rates are 8 s . in the pound. Which is the cheaper shop?

13, The rateable value of a suite of offices is raised from fivesixths to eleven-twelfths of the rent at the same time as the rent is raised by one-seventh of its original amount. Calculate the total increase in cost per annum if the first rateable value was $£ 70$ and the rates were 6 s .8 d . in the pound per amum.
14. $\Lambda$ row of thirty-six flats is let at 15 s a week each inclusive of rates. The rateable value is eleven-twelfths of the rental, and rates are at 7 s .6 d . in the pound per annum. Income-tax ${ }^{1}$ is 2 s .2 d . in the pound and is charged on five-sixths of the gross rental. Calculate the net annual income of the landlord.

## B. (3) Taxes

240. Not only does the Corporation of our town require us to pay something towards the upkeep of the town, but the Government also asks for a certain amount, because we occupy a house in the country. The Tax imposed by the Government upon householders is called the Inhabited House Duty, and amounts to 3d. in the pound for houses (not shops) of rental $£ 20$ to $£ 40$ per annum, 6 d . from $£ 40$ to $£ 60$, and 9 d . in the pound for houses of rental over $£ 60$ per annum.

Again, the very fact that we live in this country enables us, if we wish, to enter into business arrangements and to make profits, the Government affording as protection from aggression, from robbery, and from fraud, the while. It is therefore fair that, out of the profits made, or the income earned, we should pay a little to the Government.

The amount paid in the pound is a Tax upon our income, and so is called an "income-tax."
241. For purposes of income-tax assessment incomes are divided into two classes:

[^20](a) Earned Income, which includes our salary, or the profits of out business; and
(b) Unearned Income, which includes interest on money in the bank dividends upon stock (page 480), or rent from property we may have.
242. Income-tax is not charged on incomes below $£ 160$, while all below $£ 700$ are allowed an abatement ranging from $£ 160$ below $£ 400$, to $£ 70$ between $£ 600$ and $£ 700 .^{1}$ A merchant, therefore, making $£ 350$ a year would pay income-tax on $£ 350-£ 160=£ 190$; and one making $£ 650$ would pay on $£ 650-£ 70=£ 580$. An abatement of $£ 10$ is allowed for each child under sixteen years of age, and no tax is charged on insurance premiums (page 380). The tax on carned incomes is lower than on unearned, and it may range from 9 d . to 2 s .6 d . in the pound.
243. The income which the Government derives from this tax is used, as far as it will go, for national purposes, and although last year it amounted to $£ 45,000,000$, and this year will be much more, it is insufficient, and the Government has had to inaugurate (1) Customs tariff, (2) Excise duties, (3) licences, (4) stamp duties, ${ }^{2}$ etc., to provide a sufficient income.

See Question 37, page 15.
The non-tax revenue, i.e. revenue from postal and other services, Crown lands, and Suez Canal shares, amounted to $£ 34,000,000$ in the same year.

If, in an emergency, the Government needs a large amount of money, it appeals for a loan, and issues stock (§354).
244. Example 1.-A clerk's income is $£ 200$ per annum, and the income-tax is 9 d . in the pound. He is not charged any tax upon the first $£ 160$ of his income, nor on $£ 8$ he pays in insurance premiums. What income-tax does he pay?

$$
\begin{aligned}
\text { Total income } & =£ 200 \\
\text { Tax not paid on } & \frac{£ 168}{£ 32} \\
\text { Net income chargeable } & =\frac{\boxed{32}}{32 \times 9} \\
\text { Tax at } 9 \mathrm{~d} . \text { in the pound } & =\frac{12}{12} \mathrm{~s} . \\
& =8 \mathrm{~s} .
\end{aligned}
$$

${ }^{1}$ The remarks in this paragraph refer to normal times. At present the income-tax is much more comprehensive.
${ }^{2}$ The Customs Tariff includes Import duties on beer, playing-cards, ether, spirits, wines, confectionery, etc. The tariff of some other countries is very much more complicated than ours. (See Underwood Tariff Bill, published by Dorland Agency, 1s. ; also Queensland Year-Book, pp. 153170 ; and Whitaker's Almanack, pp. 408-418.)

Exorse Duties are payable on beer, spirits, etc., manufactured in the country.

Lioencrs are payable (e.g.) by auctioneers (£10), hawkers (£2), pawn.

Example 2.-A merchant's net income is £2220, and he has paid an income-tax of 1 s .6 d . in the pound; what was his gross income?

A net income of 18 s .6 d . is derived from gross income of $£ 1$;

| $\cdots \cdot$ | " | " | 1s. | " | " | " | " | $\frac{20}{18 \cdot 5} \mathrm{~s} . ;$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\therefore$ | " | " | $£ 2220$ | " | " | " | $\text { of } \frac{20}{18}$ | £2220 |
|  |  |  | . ${ }^{\text {gros }}$ | $=£ 2400$ |  |  |  |  |

## EXAMPLES. LXIV.

1. If a merchant pays his clerks as follows: Chief clerk, $£ 300$; second clerk, $£ 220$; third clerk, $£ 180$; and each is allowed an abatement of $£ 160$; calculate their net incomes if the tax stands at 10d. in the pound.
2. Income-tax on unearned income is 1 s .2 d . in the pound. If a merchant have property producing an annual income of $£ 550$, and he is allowed to deduct one-sixth for repairs, what amount of tax does he pay?
3. The managing director of a stcel works has an income of $£ 580$ per annum, he is allowed an abatement of $£ 120$, and pays $£ 35$ per annum for his life insurance. What is his net income after income-tax has been deducted at $10 \frac{1}{2} \mathrm{~d}$. in the pound?
4. A timber merchant's net income is $£ 3000$ per annum, and he has paid income-tax at the rate of 1 s . in the pound. What was his gross income?
5. The director of a company receives $£ 500$ a year as salary and derives $£ 250$ from some investments. On the former he is allowed an abatement of $£ 150$, and the income-tax is 8 d . in the pound ; on the unearned part of his income he pays 1s. 2d. in the pound. What is his net income after deducting income-tax ?
6. If one's gross income is $£ 560$ and net income $£ 540$, what is income-tax in the pound if an abatement is allowed on $£ 120$ ?
7. What is the income-tax, when $£ 815 \mathrm{~s}$. is the tax on $£ 335$, the abatement being $£ 160$ ?
brokers ( $£ \mathbf{1 0 s}$.), and by retailers of wines and spirits (from $\mathbf{2 5}$ upwards).

Stamp Duties are imposed on all documents when it is necessary for them to have a legal value--that is, a value in a court of law. For example, if you had a house and letit for $£ 20$ per annum, you would have a 4 s . stamp put on the agreement, and then it would be valid, otherwise it would not.
8. A commercial traveller's net income is $£ 450$. Three-fifths of his gross income pays 9 d . in the pound, and the remainder 1 s . What is his gross income, and how much is "unearned income"?
9. A grocer pays $£ 58$ a year rent, and he may deduct the income-tax paid on the rent. ${ }^{1}$ If it stands at 2 s . 3d. in the pound, what is the net amount he remits to his landlord?
10. A merchant whose income is $£ 450$ per annum is allowed an abatement of $£ 150$. He pays $£ 15$ for life insurance, and he has four children, on each of whom he is allowed an abatement of $£ 10$. Find his net income after the tax at 1 s .3 d . in the pound has been deducted.
11. A banker's income is made up as follows: Salary, £450; rent from property, $£ 220$; dividend from investments, $£ 180$; interest, $£ 150$. He is allowed abatement of $£ 150$ of his earned income, and pays 10d. in the pound on this, and 1 s . 2 d . on the unearned part. What is his net income?
12. Suppose you have saved $£ 180$ and lent it to the Corporation of St. Julius, which agrees to pay you $3 \frac{1}{2}$ per cent. on your money, less income-tax. And suppose still further, that your income is less than $£ 160$ a year. What amount must you reclaim from the State if the tax is 1 s .2 d . in the pound?
13. On November 17, 1914, the British Government raised its great war loan of $£ 350,000,000$, and is paying $3 \frac{1}{2}$ per cent. upon this amount. If the creditors of the Government are paying 2 s . 6 d . in the pound income-tax, calculate the amount derived in income-tax from this immense loan.
14. The area of rural lands included in taxable returns in the Australian Commonwealth was, in thousands of acres, 64028, and the average tax per acre was $3 \cdot 314 \mathrm{~d}$. The tax for Western Australia (the lowest in the Commonwealth) was 0.984 d . last year. What amount of money would the Government have lost if the average tax had been that of Western Australia.
15. From the data of the last question, determine the amount of money the Commonwealth could raise by increasing the average value of the tax on rural lands by $\frac{1}{2} d$. per acre.
16. A merchant pays $£ 1515 \mathrm{~s}$. income-tax one year when it stands at 9 d . in the pound, and $£ 22$ the next year, when it stands

[^21]at lld. in the pound. By how much has his income increased? (Neglect the abatement.)
17. Three merchants enter into partnership with $£ 7000$, $£ 5500$, and $£ 8400$ respectively. At the end of the year the first partner pays $£ 1010$ s. income-tax at 9 d . in the pound. What did each receive out of the profits?
18. In the last question, find the total amount by which the Government benefited through the profits made in the business.

## B. (4) Property

245. Property may be divided historically, rather than logically, into two classes:
(A) Real Property, which includes land and everything annexed to land, such as houses, timber, mines, sporting rights, title-deeds, etc. It is not subject to absolute ownership, but is only the subject of estates ; on intestacy it descends to the heir, and it is always governed by the law of the place where it is situated.
(B) Personal Property consists of all property not included under (A), such as goods, money, and leaschold interests in land. On intestacy it is divided among the next of kin and is governed by the law of the owner's domicile.
246. Real Property may be-
(a) Freehold, when it remains in the hands of the owner until he sells or otherwise disposes of it ; and
(b) Leasehold, when it reverts to the original holder after a given number of years, which is often either 99 or 999 years.

A tenant may take the lease of a house for three, tive, or seven years.
In case (b) the leaseholder has to pay a ground rent to the landlord, which reaches a most princely figure in London and other great cities, but for ordinary houses of rental of $£ 30$ per annum it may be about $£ 5$ to $£ 10$ per annum. At the expiration of the period of the lease the property reverts to the owner. In a large part of the West End of London to-day leases are expiring and houses are being pulled down and rebuilt, to be leased at a much higher figure than before.
247. The Rental of a house or of land is the amount paid for the use of the same, and varies very much from place to place. A house costing $£ 40$ a year in the suburbs of London would cost perhaps $£ 30$ in the Provinces.

If a house were let for $£ 30$ a year, and the landlord asked $£ 510$ for it freehold, then he would require $510 \div 30=$ seventeen years' purchase.
248. Example 1.-What rate per cent. ${ }^{1}$ does a house

[^22]costing $£ 750$ and let for $£ 50$ per annum bring to the owner?
\[

$$
\begin{aligned}
& \text { Income on } £ 750=£ 50 \\
& \quad \Rightarrow \quad \# £ 100=50 \\
& \quad \therefore \text { the rate per cent. }=6 \cdot 6 .
\end{aligned}
$$
\]

Example 2.-A piece of land brings in a ground-rent of $£ 10$ 10s. a year, and the owner wants fifteen years' purchase for the freehold. Find its value.

Value of freehold $=£ 1010$ s. paid for fifteen years

$$
=£ 15710 \mathrm{~s} .
$$

Example 3.-A shop costs $£ 1500$; at what rental must it be let to produce 7 per cent.?

If it cost $£ 100$ its rental would have to be $£ 7$.

| " | $£ 1$ | " | " | $£_{1} \frac{7}{100}$. |
| :---: | :---: | :---: | :---: | :---: |
| " |  | " | " | ${ }_{\text {¢ }}{ }^{100} \times 1500$ |
|  |  |  |  | £105. |

Fxample 4.-What must be the number of years' purchase to obtain 6 per cent.?

If $£ 6$ be paid in rent per annum it will take $100 \div 6=$ or 16.6 years to produce $£ 100$.
$\therefore$ the number of years' purchase $=16.6$.
Example 5.-If a property is sold on a twelve years' purchase basis, what rate per cent. is this?

Now, rent $\times$ number of years $=$ purchase money, and for every $£ 100$ purchase money the rent must be $£ \frac{100}{12}=£ 83 \mathrm{~s}$.
$\therefore$ the rent must be 8.3 per cent. of the purchase money.

## EXAMPLES. LXV.

Find, to two places of decimals, the rate per cent. derived from the following properties, tabulating the answers (Questions 1 to 8):

1. A hotel costing $£ 50000$ and producing $£ 8000$ per annum.
2. A bungalow costing $£ 380$ and producing $£ 40$ per annum.
3. A corner shop costing $£ 8560$ and producing $£ 180$ per annum.
4. A railroad costing $£ 1,500,000$ and producing $£ 78000$ per annum.
5. A line of steamers costing $£ 15,875,000$ and producing $£ 1,000,000$ per annum.
6. A house costing $£ 850$ and producing $£ 42$ per annum.
7. A farm costing $£ 985$ and producing $£ 350$ per annum.
8. A shop costing 5894 dollars and producing 450 dollars per annum.

If the owners of the following properties are prepared to sell at the number of years' purchase given, calculate the selling price (Questions 9 to 15) :

| Annual <br> Rental at |  | Years' <br> Purchase. | Annual <br> Rental at |
| :--- | :--- | :--- | :---: |
| 9. $£ 586$ | - | Years' <br> Purchase. |  |
| 10. $£ 9000$ | - | - 12 | $13 . £ 4210 \mathrm{~s}$. |

At what rental must the following properties be let to produce the percentage required (Questions 16 to 21)?

| Value of Property. | Percentage Required. | Value of Property. | Percentage <br> Required. |
| :---: | :---: | :---: | :---: |
| 16. 5869 francs | 10 | 19. $29,000,000$ lire | 15 |
| 17. 1,000,000 dollars | 121 | 20. $£ 5,633,000$. | $7 \frac{1}{2}$ |
| 18. 89865 gulden | - $8 \frac{1}{2}$ | 21. 3000 guineas | $9 \frac{1}{4}$ |

22. What must be the number of years' purchase to produce -(1) $3 \frac{1}{2}$; (2) $7 \frac{1}{4}$; (3) $8 \frac{1}{8}$; (4) $15 \frac{1}{2}$; (5) $20 \frac{1}{8}$; (6) 25 per cent.?
23. What percentage of the purchase money must the rent of a property be if it is reckoned at (1) 7 ; (2) 8 ; (3) 15 ; (4) $12 \frac{1}{2}$; (5) $18 \frac{1}{2}$; (6) 25 years' purchase?

## B. (5) Insurance

249. In a particular town there are forty thousand houses, and in the course of the last five years not twenty of them have been destroyed by fire. In the same time the actual loss sustained by burglary has been, perhaps, slightly higher, while the number of people who have died would be very considerable. We may say, then, that the risk of fire is small and of burglary slightly greater, while it is highly probable that all of us will die.

Now, it is easy to see that representatives of the forty thousand householders can meet together and agree that the average value of the contents of their houses is $£ 200$, and decide that they will each pay 18. 6d. per cent. on that value, pool the proceeds, and, if any house is burnt down, replace the contents
out of the pool. It is clear that if the owner of any house does not enter into the arrangement he may lose a great deal of money, and possibly become a bankrupt, if his house is burnt.
250. Now the householders will contribute altogether $1 \mathrm{~s} .6 \mathrm{~d} . \times$ 40000 or $£ 3000$. If three houses are completely burnt down, the pool of $£ 3000$ will have to pay $£ 600$, and leave balance in hand of $£ 2400$ for the next year. If fifteen houses were destroyed, nothing would be left for the next year.

Now, instead of the householders doing this among themselves, insurance companies exist, and we apply to them for a policy-that is, an agreement to the effect that if we pay them, say, 1 s . 6 d . per cent. on the value of our property, they will replace the same, up to a value stated if fire destroys it.

Inasmuch as the elaborate system of fire-calls reduces the chances of complete destruction to a minimum, it is obvious that fire insurance companies can make very large profits, which they can invest and increase still further, and so it pays to invest money in the shares of such companies (page 491).
251. The Greeks virtually applied the principle of insurance to their shipping ventures, and, indeed, if Antonio had but insured his argosies he would never have had to run the gauntlet of Shylock's revenge.

Risks of every kind are covered by insurance, such as the fall of a chimney-pot, a crop of wheat being injured by hail, or a ship sinking. By paying 2s. 6d. per annum an employer can be covered against his servant (say) cutting her hand, whereas if he did not insure he might have to pay $£ 200$ or $£ 300$ damages. By paying a small premium he throws his responsibility on to the shoulders of the company, which can afford to pay the damages because, of the large number insured, only a few suffer injury.

## LIFE INSURANCE

252. In the case of life insurance, the Premium (that is, the amount paid annually to secure any required cover) must be high, for the risk of dying is very much higher than that of fire.

The best insurance offices require the Proposer (the one who seeks insurance) to be examined medically, and upon the report of the doctor being good, they "accept" his life. After he has paid the premium they issue a policy (Plate XII., p. 382).
253. A whole life policy is payable at death.

An endowment policy is payable at the age of $50,55,60$, etc., or previous death, and involves a slightly higher premium.

A Bonus is an amount added to a policy as a result of the company's investing its premium income and making a profit.

If you, aged 20 , had a policy for $£ 500$ payable to you in 30 years, and at the end of 20 years did not wish to pay any further premium but wanted a cash payment, the office would call upon you to surrender the policy and offer you, say, £250, which would be called the Surrender Value, and it would represent the total amount you had paid in premiums together with the interest earned, less a certain amount for the risk the company had taken in insuring your life.
254. Tables, called Mortality Tables, have been compiled in which we find recorded the Expectation of Life both of men and of women. With the help of such tables, and a knowledge of other matters which enter into the question, insurance offices determine the premium to be paid at any age of entry. The following is a part of such a table:

| Age. | General Male Population. | Life Offices' Experience. | Abstainers' Experience. | Females. |
| :---: | :---: | :---: | :---: | :---: |
|  | Years. | Years. | Years. | Years. |
| 15 | $45 \cdot 2$ | $47 \cdot 8$ | 51.5 | $47 \cdot 6$ |
| 20 | 41.0 | $43 \cdot 7$ | $47 \cdot 4$ | $43 \cdot 4$ |
| 25 | $37 \cdot 0$ | $39 \cdot 6$ | $43 \cdot 5$ | $39 \cdot 4$ |
| 30 | $33 \cdot 1$ | $35 \cdot 6$ | $39 \cdot 3$ | $35 \cdot 4$ |
| 35 | $29 \cdot 2$ | $31 \cdot 7$ | $35 \cdot 1$ | 31.5 |
| 40 | $25 \cdot 6$ | $27 \cdot 9$ | $30 \cdot 8$ | $27 \cdot 8$ |
| 45 | $22 \cdot 2$ | $24 \cdot 2$ | $26 \cdot 6$ | $24 \cdot 2$ |
| 50 | $18 \cdot 9$ | $20 \cdot 6$ | $22 \cdot 5$ | $20 \cdot 6$ |
| 55 | $15 \cdot 8$ | $17 \cdot 2$ | $18 \cdot 6$ | $17 \cdot 2$ |
| 60 | $12 \cdot 9$ | $14 \cdot 1$ | $15 \cdot 1$ | $14 \cdot 1$ |
| 65 | $10 \cdot 3$ | $11 \cdot 2$ | 11.8 | $11 \cdot 3$ |
| 70 | $8 \cdot 1$ | $8 \cdot 7$ | $9 \cdot 0$ | $8 \cdot 8$ |

255. Typical rates for various kinds of insurance are:

Fire.-Buildings of private residences, 1 s .6 d . per cent.
" " business premises, 1s. 6d. to 2s. 6d. per cent.
Employers Liability.-2s. 6d. to 20s. per servant.
Whole Life Assurance-

| Without profits. |  | Age at entry, 20. | Annual Premium, |  | 1 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| With | " | " , | " | " | 2 |  |  |
| " | " | 30. | " | " | 2 |  |  |
| " | " | " $\quad 40$. | " | " | 3 |  |  |
| " | " | 60. | " |  |  |  |  |

Insurance of parcels sent abroad by Post, 4d. for $£ 12$, and 2 d for each additional $£ 12$ up to 5 s. 10 d. for $£ 400$ (maximum).

Accident Insurance, $£ 1$ to $£ 8$ per annum according to benefita required and nature of employment.
Marine Insurance depends entirely on the character of the goods, port of shipment, and destination, and upon international relationships. It may range from a few shillings to four or five guineas per cont. A merchant in the Midlands tells us that he paid 20 per cent. in the early part of the year 1915.
Underwriters are those who guarantee the amount of the policy if and when it becomes due-that is, they take the risk.
256. Lloyd's.-Edward Lloyd was a Welshman who, at the close of the seventeenth century, opened a coffec-house in Tower Street, London, where underwriters and shippers dropped in for a chat. A little later, Lloyd moved to the corner of Lombard street, where his coffee-house business was rapidly subordinated to all sorts of shipping transactions, at which the auction "pulpit" now in the Cajtain's Room was used.
1726. Lloyd's list was issued.
1774. Lloyd's moved to the Royal Exchange, where it still finds its home.
1850. There were 200 underwriters, now there are more than three times as many.
It has agents in every port, and intelligence stations everywhere. It is, in fact, the centre and soul of the shipping world.

25\%. Example 1.-What is the value of a warehouse which is insured at 1 s . 6 d . per cent., the owner paying 22 s . 6 d . per annum premium?

Owner pays 1 5ัs. on $£ 100$

$$
\begin{array}{r}
\therefore \text { he pays } 22 \mathrm{~s} .5 \mathrm{~d} . \text { on } \frac{100}{1 \cdot 5} \times 22.5 \\
=£ 1500 .
\end{array}
$$

Exampie 2.-A merchant has goods to the value of £99750, which he insures at the rate of 5 s . per cent. What must be paid per annum in order to cover both stock and premium?

A policy for $£ 100$ covers goods valued at $£ 9915 \mathrm{~s}$., and premium, 5s.

$\therefore$ value of policy is $£ 100000$.
Proof.--Policy is for $£ 100000$. Premium on that amount is $£ 250$. $\therefore$ value of goods covered $=£ 100000-£ 250=£ 99750$.

## EXAMPLES. LXVI.

1. The value of a certain property is $£ 380$. What is the premium to insure it against fire at 1 s .6 d . per cent.?
2. A merchant wishes to insure his furniture and effects at his private house against fire and burglary to the extent of $£ 750$ fire and $£ 550$ burglary. The premiums are 1s. 9d. and 1s. 6 d . per cent. respectively. What is the total amount he must pay?
3. The life insurance premium for a clerk aged 32 is £2 11s. 4d. per cent. What is the annual premium for a policy of $£ 450$ (with profits)? ?
4. A company has 250 branches in the United Kingdom, the average value of which, for fire insurance purposes, is $£ 485$. What is the total premium to be paid, reckoning 1 s .9 d . per cent.?
5. A draper pays $£ 2815 \mathrm{~s} .9 \mathrm{~d}$. per annum in fire insurance premiums. Two-thirds of this amount is payable on his ordinary stock and one-third on a particularly inflammable part (e.g. celluloid combs, cotton wool, flannelette, etc.). If his stock is valued at $£ 35700$ for insurance purposes, what is the rate per cent. for his ordinary stock and for the inflammable part of it, if the value of the latter is one-seventh of the whole?
6. A jeweller has a valuable stock which is insured as follows (when placed in a safe at night): Precious stones-premium, $£ 258$; value of stock, $£ 34400$. Gold articles-premium, $£ 375$; value of stock, $£ 60000$. Silver articles-rate, 5s. per cent.; value of stock, $£ 1000$. Find (1) the total premium paid; (2) the rate per cent. for precious stones and for gold articles.
7. From the following details make out a statement for the total insurance premium due to the Beadle Insurance Corporation from Stoop \& Co. :

Fire.-Value of premises, $£ 1500$; rate per cont., 1 s .6 d .

Bứglary. "-Value of goods, £8000; rate per cent., 2 s .
Ingurance of Employees. - Total, $£ 10000$; av. rate per cent., 3 s. ,, ,", Machinery.-Value, $£ 12500$; ,, 48.
Fidelity Güarantee on £8500; av. rate por cent., bs. 6 d.
8. If a clerk insures his life for $£ 500$ when he is 20 years old,

[^23]and pays a premium of $£ 217 \mathrm{~s} .4 \mathrm{~d}$. per cent., he will receive, in an office with which we are acquainted, at the age of $55, £ 974$ (at present rates). Does he gain or lose money over the matter, and if so, how much? (Remember, in estimating the position, that we are excluding the interest which could be obtained by investing the premiums year by year, and that he had $£ 500$ cover, at least, all those 35 years. See Part III. for further information.)
9. A junior clerk comes to me saying that he can insure his life for $£ 250$, at the rate of $£ 216 \mathrm{~s} .4 \mathrm{~d}$. per cent. with profits, or for $£ 24 \mathrm{~s} .6 \mathrm{~d}$. per cent. without profits, the insurance being an endowment insurance payable in 35 years. The profits will amount to $£ 200$. In which of the two ways shall I advise him to insure, and how much will he benefit by following my advice?
10. The captain of a liner insures his life for $£ 1500$, and pays at the rate of $£ 49 \mathrm{~s}$. 1d. per cent. for an endowment insurance payable in 25 years (his age is 40 years). He is drowned after he has paid 18 premiums. What does the company lose if the bonuses in the 18 years amount to $£ 550$ ?
11. Three merchants consign goods to the value of $£ 825$ from Leeds to Suez, and effect an insurance for $£ 960$ upon the same. On delivery they receive a (code) cablegram saying that $\frac{7}{15}$ of the goods have been spoiled. The value sent by each of them was ${ }_{2}^{2}$ by the first, ${ }^{4} 5$ by the second, and the residue by the third. If the rate of insurance was $£ 25 \mathrm{~s}$. per cent., find how much each merchant should pay for the insurance, and how much each should receive in compensation for damage, which is to be taken in proportion to the value consigned by each.
12. How much did the first merchant of the last question gain or lose by the device of over-insuring his goods?
13. What would it cost a West End firm to insure its Paris " magazin" for 15500 francs at 3 francs per cent.?
14. A firm of cotton manufacturers in Manchester happens to have a clerk who has taken the trouble to learn Russian, and they send him as their manager of a new branch at Moscow. What premium must he pay to insure the offices there for 3580 roubles at 1.25 rouble per cent.?
15. It is possible to insure a consignment of cloth valued at $£ 3685$ from Southampton to Cape Town for $£ 4$ 12s. 1d. Determine the rate per cent., to the nearest penny.
16. A quantity of goods is worth $£ 8560$, and the insurancepremium upon it is 5s. per cent. For how much must an insurance policy be taken out to cover both goods and premium?
17. What will it cost in English money to insure my wine vaults in Italy for 6200 lire at 3 lire per cent.?
18. A cargo of cotton goods (valued at $£ 9560$ ) is consigned from Manchester to Bermuda (where the value of the importation of these goods was in 1913-14 greater than that of any other goods imported), and it is insured against all risks with the British Government at $£ 44 \mathrm{~s}$. per cent. Calculate, for the consignee, the amount of a policy to cover the value of the goods and the premium.
19. A merchant has coffee to the value of $£ 1850$ in store. What must he pay to insure his stock and the premium at the rate of 2 s .9 d . per cent. ?

## B. (6) Bankruptey

258. In the course of your business career you may find, particularly at certain periods of the year, that the profits are not as high as at others, or, indeed, that the business is being conducted at a loss. If this continues for any length of time it may become serious, and you may find it impossible to pay your way. One of the most frequent causes of this state of affairs is injudicious, or perhaps unfortunate, buying. ${ }^{1}$

For example, suppose the dried fruit market is slowly rising and you buy in rather largely, and immediately afterwards a slump oocurs. You are compelled to sell at the current price, and so lose, it may be very heavily.
259. Sometimes it is impossible to recover from the loss sustained, and you may then fail to meet your just debts. If this be so, then one of your creditors will send in his account as usual, and if it be not met at one month he may ask for a threemonths' bill, and upon your failing to meet that he may obtain judgment against you in a court of law-that is to say, he may have a notice served on you demanding payment within seven days. If you then fail to comply with the order of the Court, you have committed an act of bankruptcy, ${ }^{2}$ and your creditor may call upon you to appear before the registrar of the Court where a Bankruptcy Petition ${ }^{3}$ has been lodged. (See Bill of Exchange, Plate XIII., p. 468, for " Bill.")
260. On appearing before the Court mentioned, the creditor

[^24]will establish the fact that you are his debtor for an unsecured debt exceeding $£ 50$, whereupon the registrar, after having heard your views, will issue a Receiving Order ${ }^{1}$ and will then become merely a trustee of the debtor's property on behalf of the creditors. The fact that a receiving order has been issued must be advertised in The London Gazette and also in a local paper, while the Board of Trade must be notified by the registrar. But the debtor is not yet a bankrupt. Some claims, such as those for rent, rates, taxes, and servants' wages, are called Preferential Claims, and must be paid in full, if possible, before any other claims are considered, while the landlord may distrain goods to recover rent due to him.
261. After you have prepared a statement of affairs, the first meeting of creditors is held, at which the possibility of coming to terms is considered, so as to avoid the extreme course of making you a bankrupt. It should be observed that if you could offer the legal minimum of 5 s . in the pound the creditors would be wiser to accept it, ${ }^{2}$ generally speaking, than to make you a bankrupt, for the proceedings cost a great deal and the legal expenses incurred constitute a Preferential Claim, while, from your standpoint, your credit is saved.

If, however, the case is pursued to the end and you are "adjudicated" a bankrupt, it is a criminal offence for you to obtain credit for over $£ 20$ unless you declare that you are an undischarged bankrupt, and you are prohibited from becoming a Member of Parliament or from taking up any municipal office.
262. Example 1.-A debtor pays 6s. 8d. in the pound; what does a creditor receive for a debt of $£ 3000$ ?

On $£ 1$ the debtor pays 6 s. 8 d. ; $\therefore$ on $£ 3000$ he pays $£ 1000$. So the creditor receives $£ 1000$ and loses $£ 2000$.

[^25][^26]Exampie 2.-A bankrupt's assets are $£ 5000$, and he can pay 12 s .6 d . in the pound; what are his liabilities?

$$
\begin{aligned}
& \text { He pays } 12 \mathrm{~s} .6 \mathrm{~d} \text {. on } £ 1 ; \\
& \therefore \quad £ 5000 \text { on } \frac{£ 5000 \times 20}{12 \cdot 5}=£ 8000 ; \\
& \therefore \text { his liabilities are } £ 8000 .
\end{aligned}
$$

## EXAMPLES. LXVII.

1. If a bankrupt pays 3 s . 6 d . in the pound on a debt of $£ 356$, how much does the creditor actually receive?
2. If the assets of a bankrupt are $£ 78612 \mathrm{~s}$., and his liabilities $£ 1368$, what dividend can he pay?
3. What are a bankrupt's assets if he can pay 5 s .9 d . in the pound on liabilities amounting to $£ 1200$ ?
4. If a bankrupt's assets amount to $£ 53815$ s., and he pays a dividend of 7 s .6 d . in the pound, what are his liabilities?
5. What dividend can assets amounting to $£ 511119 \mathrm{~s} .7 \mathrm{~d}$. pay on liabilities amounting to $£ 835410$ s. ?
6. One of my customers who owes me $£ 35810 \mathrm{~s}$. becomes a bankrupt, and pays 15 s .6 d . in the pound. How much do I lose?
7. A bankrupt has four creditors to whom he owes respectively $£ 300, £ 450, £ 560$, and $£ 80$. If he pays $12 \frac{1}{2}$ per cent. dividend, find how much he pays in the pound, and how much each of the creditors actually receives.
8. If a creditor receive from a bankrupt $£ 2697 \mathrm{~s}$. 6 d . on a debt of $£ 7186$ s. 8 d., what dividend does he pay?
9. A bankrupt's assets are $£ 6375$, what are his lialilities if he pays a dividend of 12 s .9 d . in the pound?
10. How much would one of the creditors of the bankrupt of the last question receive on a debt of $£ 35010$ s. ?
11. A bankrupt has four creditors, to the first three of whom he owes 3000 francs, 10000 francs, and 15500 francs. If his total liabilities are a quarter of a million francs and his assets 100000 francs, what amount of money will be distributed among his creditors other than the three mentioned above, and what dividend does he pay?
12. Three merchants are in partnership and they agree to bear all bad debts in the ratio of $1: 3: 5$. If a debtor becomes a bankrupt and pays 12 s . in the pound on a debt of $£ 10555 \mathrm{~s}$., find the amount each loses.
13. A bankrupt finds he can pay 3s. 6 d .. in the pound on debts amounting to $£ 855315$ s. 4d. What are his assets, and what would be the average loss to each of his fifty creditors?
14. The lawyer who conducts the case for a bankrupt charges $2 \frac{1}{2}$ per cent. on the total assets, which are $£ 800$. What should creditors whose debts amount to $£ 250$ and $£ 480$ receive if the sum of the debtor's other liabilities amounts to $£ 1610$ ?
15. A bankrupt owes $£ 7202$ and he has assets valued at $£ 2060$ 1ls. He owes $£ 80$ for rent. What dividend can he pay?
16. A merchant has real property valued at 50000 dollars; goods valued at 125500 dollars; outstanding debts valued at 18500 dollars ; and owes rent of 1000 dollars. The lawyer who takes up his case in bankruptcy charges 4500 dollars. If the debts amount to 250000 dollars, what dividend can be paid?
17. A bankrupt's cash in hand and at bank amounts to $£ 350$, his other property is valued at $£ 300$, and a creditor owes him $£ 26$, but is himself able to pay only 7 s . 6 d . in the pound. Allow legal charges 15 guineas, and find the liabilities if a dividend of 15 s .6 d . is paid.
18. What assets will meet a dividend of 16 s . 3 d . on liabilities amounting to $£ 7324$ ?
19. What assets would be required to pay a dividend of 17 s . 6d. on liabilities amounting to $£ 5800$, after deducting preferential claims as follows:

Legal expenses, $£ 25$; one year's rent, $£ 90$; six months' rates at 6 s .8 d . in the pound on five-sixths of rental ; incometax, 1 s . in the pound on $£ 400$; wages due, $£ 80$.
20. What dividend can be paid under the following circumstances:

Assets: Eighteen houses valued at $£ 250$ each; goods valued at $£ 12500$; plant valued at $£ 8360$; outstanding debts valued at $£ 1250$.
Liabilities: Preferential claims, $£ 850$; other claims, $£ 30000$. Of the outstanding debts, one for $£ 300$ realises 12 s . 6 d. in the pound; one for $£ 100,8 \mathrm{~s} .4 \mathrm{~d}$. in the pound; one for $£ 50,5 \mathrm{~s}$. in the pound; the remainder producing the full amount.
21. A bankrupt's assets were declared to be $£ 1093$ 10s., but the receiver ruled that an amount of $£ 21814 \mathrm{~s}$. must rank as a preferential claim. If the liabilities were $£ 5832$, what difference would the receiver's ruling make to the dividend?
22. Among a bankrupt's assets, which amount to $£ 8500$, is a debt for $£ 1500$ which is written off entirely as a bad debt, and a dividend of 12 s . 8d. is declared. Find what his liabilities amounted to, and then determine by what amount the dividend can be increased if the bad debt referred to realises 18 s . in the pound.
23. A bankrupt's liabilities amounted to $£ 104000$, and a dividend of 15 s . was probable; but the landlord put in a preferential claim for a year's rent, and the dividend was finally declared to be 14s. $4 \frac{1}{2} \mathrm{~d}$. in the pound. What was the rental claimed, and to what dill the remaining assets amount?
24. One of the creditors of a bankrupt learns that his liabilities are $£ 58300$ and his assets $£ 24977$ 10s., and that a dividend of 8 s .6 d . in the pound will be paid. On working this out he finds that the figures given do not agree with one another, and concludes that preferential claims have been allowed. To what did they amount?

## C. Chain Rule

263. The so-called Chain Rule is really nothing more than Proportion disguised; but, since it is useful in exchange problems particularly, we shall deal with it.

The student should work Examples LXVIII. both by Proportion and by Chain Rule.
264. Example 1.-If 1 mile $=1.6093$ Kilometre, evaluate a yard in metres.
(i) By Proportion-

$$
\begin{aligned}
1 \mathrm{mi} . & =1.6093 \mathrm{Km} . \\
\therefore 1760 \mathrm{yds} & =1.6093 \mathrm{Km} . \\
& =1.6093 \times 1000 \mathrm{~m} . \\
\therefore 1 \mathrm{yd} . & =\frac{1.6093 \times 1000}{1760} \mathrm{~m} . \\
& =0.9144 \mathrm{~m} .
\end{aligned}
$$

(ii) By Chatn Rule-

To work this question by Chain Rule we write it down thus:

$$
\begin{aligned}
1760 \mathrm{yds} .\left(\begin{array}{l}
\text { (NOT } 1 \mathrm{mi} .)
\end{array}\right. & =1.6093 \mathrm{Km} . \\
1 \mathrm{Km} . & =1000 \mathrm{~m} . \\
x \mathrm{~m} . & =1 \mathrm{yd} .
\end{aligned}
$$

Where $x$ is the number of metres in 1 yd .
Now, the value of $x$ is, from part (i)-

$$
\frac{1.6093 \times 1000 \times 1}{1760 \times 1}
$$

or, $x=\frac{\text { numbers on the side without the } x \text { multiplied together }}{\text { numbers on the side with the } x \text { multiplied together }}$, and each number constitutes one link in the chain, while one link
is unknown. Hence we have the following (neglecting the numbers):


Where we pass from yards to Kilometres and then from Kilometres to metres, and from metres back to yards; and

$$
E=\frac{B \times D \times F}{A \times C} .
$$

It is possible to show that the chain is right thus:

$$
\mathrm{ms}=\frac{\mathrm{Kes} . \times \mathrm{ms} . \times \mathrm{yds}}{\mathrm{Kmss} \times \mathrm{yds}}
$$

and since, on the right, Kilometres and yards cancel, and we inave metres $=$ metres.

If we had found that

$$
\mathrm{ms} .=\frac{\mathrm{Kras} . \times \mathrm{ms}, \times \mathrm{yds} .}{\mathrm{Kms}_{\mathrm{m}} \times \mathrm{mg}}
$$

then Kilometres and metres would cancel on the right, and leave metres equal to yards, which is impossible, and would show the chain to be wrong.
265. Example 2.-If $1 \mathrm{gm} .=15.43235$ grs., evaluate a Kilogram in pounds.


$$
\begin{aligned}
\therefore x & =\frac{15.43235 \mathrm{grs} \times 1 \mathrm{lb} . \times 1000 \mathrm{gms}}{7000 \mathrm{grs} . \times 1 \mathrm{gm}} \\
& =2.2046 \mathrm{lb} .
\end{aligned}
$$

$\therefore 2.2 \mathrm{lb}=1000 \mathrm{gms}=1 \mathrm{Kgm}$.

## EXAMPLES. LXVIII.

1. What is the constant for converting English tons to metric tons, if $1 \mathrm{Kgm} .=2 \cdot 2046213 \mathrm{lb}$. ?
2. Find, from the value of the Kilogram given in Question 1, the constant for converting grams to grains.
3. Express 250 English tons in metric tons, and 5 Kgm . in grains.
4. If $1 \mathrm{lb} . \mathrm{Av} .=0.45359265 \mathrm{Kgm}$., find the constant for converting metric tons to English tons. Make out a nine-multiple table for this conversion, and thence express 15.86 metric tons and 3586 Kgm . in English tons.
5. Use the results of Question 4 to find how many Kilograms make 1 stone.
6. Using the result of Question 1, reduce 10 tons 2 cwt. 1 qr. to Kilograms.
7. If 1 foot $=3.047945 \mathrm{dm}$., show that 1 cubic foot contains 28.3 c.dm. nearly.
8. If 1 pint $=0.567932$ litre, and 1 cubic foot $=6.231$ gallons, show that 1 cubic foot contains 28.3 litres.
9. If 1 ounce $\operatorname{Tr} .=3 \cdot 11035 \mathrm{Dgm}$. , and $1 \mathrm{lb} . \mathrm{Av} .=14 \frac{7}{12}$ or. Tr., express 1 oz . Av. in grams and 10 lb . (Av.) in Kilograms.
10. If 1 gram $=15 \cdot 43235$ grains, and 7000 grains $=1 \mathrm{lb}$. Av., find the weight of 1 stone Av. and $3 \frac{1}{2}$ stone of dead meat in Kilograms.
11. If $£ 1=25.22$ francs or 20.43 marks, express 1 franc in marks, and thence prepare a nine-multiple table for converting francs to marks, and determine the value of 5863 francs.
12. If 1 cubic foot $=28.32$ c.dm., calculate approximately the constant multiplier for converting quarts to litres, and thence express 80 pecks in litres and 350 bushels in Hectolitres.
13. What is the constant multiplier for converting litres to quarts? Express 5 l. 6 dl. in pints.
(Questions 14 to 16 are obviously proportion sums, but they can be worked by the Chain Rule.)
14. Three salesmen, R, S, T, take money as follows: R takes $£ 50$ while $\mathbf{S}$ takes $£ 45$, and $\mathbf{S}$ takes $£ 25$ while $\mathbf{T}$ takes $£ 100$. How much will R take when $T$ takes $£ 150$ ?
15. A milkman employs four men on particular rounds-the first sells 40 gallons and the second 28 ; the third sells 50 while the second sells 30 ; and the fourth sells 60 while the third sells 80. What does the first sell when the fourth sells 100 gallons?
16. Three plasterers are employed on a particular job; the
first can do in 8 hours what the second can do in 5 hours, and the third can do in 10 hours what the second can do in 15 hours. How long does the third need to do what the first can do in 16 hours?
17. If a United States dollar is worth $4 \mathrm{~s} .1 \cdot 32 \mathrm{~d}$. , and 1 frane 9.513 d ., calculate the amount that must be paid in Paris to settle an account for 562 dollars 85 cents.
18. A gold Krone (Denmark) is worth 1 s .15 d ., a rupee is worth 1s. 4d., and a Canadian dollar $4 \mathrm{~s} .1 \cdot 33 \mathrm{~d}$. Settle the following accounts : 150 Kroner in rupees, 1000 rupees in dollars, 500 dollars in Kroner.

## SECTION XVIII

## PERCENTAGES, COMMISSION AND BROKERAGE, PROFIT AND LOSS

## A. Percentages

266. The real meaning of the word per cent. (L., centum) is per hundred, and we use 100 because of its great convenience in making comparisons. The following examples will illustrate the application of percentages:

Example 1.-What is $\mathbf{1 5} \%$ of $£ 150$ ?

$$
\begin{aligned}
& 15 \% \text { means } 15 \text { per cent. or } \frac{15}{100} \\
& \therefore 15 \% \text { of } £ 150=\frac{15}{100} \text { of } 150 \\
&=£ 2210 \mathrm{~s} .
\end{aligned}
$$

Example 2.-A grocer buys rice which costs him £200. A quarter of it is spoiled by rats. What percentage does he lose?

$$
\begin{aligned}
& \quad \frac{\frac{1}{2} \text { of the rice is obviously } \frac{25}{100}}{\therefore \frac{1}{2}=25 \%} \text {. }
\end{aligned}
$$

267. Example 1.-The population of New Zealand increased from $3,425,160$ in 1912 to $3,448,190$ in 1913. Calculate the increase per cent. to two places.

The populations were $\bumpeq 3,425,000$ and $3,448,000$.
$\therefore$ the increase was $\bumpeq 23000$ on $3,425,000$
i.e. 1 on 150
or $\frac{2}{3}=0.66$ on 100.
Increase on 3,425,160 was 23030

$$
\begin{aligned}
\therefore \text { percentage increase was } & \frac{23030 \times 100}{3,425,160} \\
& =0 \cdot 67, \text { to two places. }
\end{aligned}
$$

Example 2.-If $28 \frac{1}{2} \%$ of a merchant's annual income is £171, what is his average monthly salary?

$$
£ 28.5 \text { is } 28 \frac{1}{2} \% \text { of } £ 100
$$

$$
\begin{array}{rlll}
£ 1 \quad, & " & £ \frac{100}{28 \cdot 5} \\
\therefore £ 171 \quad, \quad & & £ \frac{100 \times 171}{28 \cdot 5} \\
& =£ 600 \\
\therefore \text { average monthly salary } & =£ 50 .
\end{array}
$$

Example 3.-A motor costs £564 new, and is worth $£ 376$ at the end of the first year. What is the percentage depreciation?

Original value, $£ 564$.
Value at end of one year, $£ 376$.
The depreciation on $£ 564$ is $£ 188$

$$
\begin{array}{r}
\therefore \quad " \quad \text { on } £ 100 \text { is } £ \frac{188 \times 100}{564} \\
=£ 336 \mathrm{~s} .8 \mathrm{~d} .
\end{array}
$$

$\therefore$ the depreciation is $33 \frac{1}{3} \%$.
Example 4.-The mean maximum temperature for February is $42^{\circ}$ and the minimum $35 \cdot 6^{\circ}$, and the corresponding figures for March are $52^{\circ}$ and $38.3^{\circ}$. By how much per cent. does the maximum exceed the minimum in the two cases, and by how much per cent. is the mean temperature for March above or below that of February?

February, max., $42^{\circ}$; min., $35.6^{\circ}$; diff. $=6.4^{\circ}$
$\therefore$ with min. $35.6^{\circ}$, max. is $6.4^{\circ}$ higher,

$$
\begin{aligned}
& \text { or } \frac{64}{356} \times 100 \\
& =17.97 \%
\end{aligned}
$$

March in the same way gives $\frac{13 \cdot 7}{38 \cdot 3} \times 100$

$$
=35.77 \%
$$

Mean temperature for February $=\frac{42+35 \cdot 6}{2}=38.8^{\circ}$
" " March $=\frac{52+38.3}{2}=45.15^{\circ}$
March exceeds that for February by $6.35^{\circ}$
$\therefore$ mean March temperature is higher than that of February

$$
\begin{aligned}
& \text { by } \frac{6.35}{38.8} \times 100 \\
& =16.36 \%
\end{aligned}
$$

Example 5.-The population of the town increases by $3 \%$ in one year, and that of another decreases by $1 \%$ in the same time; also the population of the former was 100000, and that of the second $18 \%$ more than this number. Calculate the difference in the populations at the end of the year.

$$
\begin{aligned}
& \text { Original population, town }(1)=100000 \\
& \text { " " } \\
& (2)=\frac{11}{10} \mathrm{~B}_{0}^{\circ} \text { of } 100000 \\
& =118000 \\
& \text { Increase in } 1 \text { year on (1) }=3000 \\
& \text { Decrease in } 1 \\
& \text { (2) }=1180 \\
& \therefore \text { Population at end of yearfor }(1)=103000 \\
& (2)=116820
\end{aligned}
$$

$\therefore$ difference of population at end of year $=13820$.
Example 6.-A piece of gold wire is drawn so that its diameter is 0.05 cm ., and its length 15 cm ., instead of being drawn 0.06 cm . in diameter and 20 cm . long as ordered. What percentage error is there in the volume of gold, to one place of decimals?

The student should note the method adopted here.

$$
\begin{aligned}
\text { Volume ordered } & =\pi \times(0.03)^{2} \times 20 \text { c.c. } \\
& =\pi \times 0.018 \text { c.c. } \\
\text { Volume received } & =\pi \times(0.025)^{2} \times 15 \\
& =\pi \times 0.009375 \text { c.c. } \\
\text { Volume is too small by } & =\pi(0.018-0.009375) \\
& =\pi(0.008625)
\end{aligned}
$$

Percentage error on volume ordered $=\frac{\pi(0.008625)}{\pi(0.018)} \times 100$

$$
\begin{aligned}
& =\frac{0.8625}{0.018} \\
& =47.9 \%
\end{aligned}
$$

268. The student should observe that percentages may or may not involve time.

Simple and Compound Interest, the Discounting of Bills, etc., will be dependent on time, but Brokerage, Cash Discount, Rates, Taxes, Premiums, and the like, are largely independent of it, and yet the last three may be called periodic.

It is convenient to remember, for business purposes, that-
$. \pi \%=1 \mathrm{~s}$. in the pound, for $\frac{\mathrm{s}}{100}$ of $£ 1=1 \mathrm{~s}$.;
$2 \frac{1}{2} \%=6 \mathrm{~d}$. in the pound;
and that $12 \frac{1}{2} \%=2 \mathrm{~s} .6 \mathrm{~d}$. in the pound.

## EXAMPLES. LXIX.

1. Express the following rates per cent. in fractional form :
(l) 25.
(2) 5.
(3) 10 .
(4) 50.
(5) 20 .
(6) 65 .
(7) 72 .
(8) 88.
(9) 43.
(10) $2 \frac{1}{2}$.
(11) 3.
(12) $3 \frac{1}{2}$.
(13) $4 \frac{1}{2}$.
(14) $12 \frac{1}{2}$.
(15) 16.
(16) $23 \frac{1}{2}$.
(17) $33 \frac{1}{3}$.
(18) 45.
(19) 28.
(20) $18 \frac{1}{2}$.
2. Reduce the following to percentages, to two places of decimals:
(1) $\frac{1}{8}$.
(2) $\frac{1}{2}$.
(3) 4.
(4) $\frac{1}{8}$.
(5) $\frac{1}{10}$.
(6) $\frac{1}{20}$.
(7) $\frac{1}{2} \frac{1}{25}$.
(8) $\frac{8}{5}$.
(9) $\frac{5}{8}$.
(13) $\frac{21}{2} \frac{1}{3}$.
(10) $\frac{4}{4}$.
(14) $\frac{18}{5} 8$
(11) $\frac{16}{16}$.
(15) $\frac{27}{31}$
(19) $\frac{8}{80}$.
(12) $\frac{\pi}{2}$.
(17) $\frac{3}{200}$.
(18) ${ }_{75}^{45}$.
(20) $100^{1} 00$.
3. Write down the value of:
(1) $5 \%$ of $£ 250$; of $£ 300$; of $£ 550$; of $£ 760$.
(2) $2 \frac{1}{2} \%$ of 10 s. ; of 15 s. ; of 80 s. ; of $£ 5$.
(3) $10 \%$ of $£ 450$; of $£ 80010 \mathrm{~s}$. ; of $£ 775$.
(4) $12 \frac{1}{2} \%$ of $£ 88 \mathrm{~s}$. ; of $£ 9600$; of $£ 928 \mathrm{~s}$.
(5) $8 \frac{1}{2} \%$ of 12 s . ; of 12 guineas; of $£ 312 \mathrm{~s}$.
4. What is $5 \%$ of $£ 150 ; 16 \frac{2}{3} \%$ of 5 miles; $7 \frac{1}{4} \%$ of 180 acres ; $5 \frac{1}{2} \%$ of 40 gallons?
5. What is $6 \frac{1}{2} \%$ of 1050 francs; $3 \frac{1}{2} \%$ of yen $1575 ; 3 \frac{1}{2} \%$ of 350 dollars $+84 \%$ of 50 cents ; $12 \frac{1}{2} \%$ of 786 metres; $10 \frac{1}{2} \%$ of 388 litres?
6. What is $7 \frac{1}{2} \%$ of 1 mile; $8 \%$ of $150 \mathrm{~cm} . ; 12 \frac{1}{2} \%$ of 10 sq. chs. ; $5 \%$ of 3 Hectares in ares; $15 \%$ of 58 lire; $20 \%$ of 25 tons 3 cwt . $?$
7. If a man drinks one-cighth whisky and seven-eighths water, what percentage of his restorative draught is whisky?
8. Show that $8 亡 \%$ of $£ 8$ is the same as $4 \frac{1}{8} \%$ of $£ 16$.
9. Of what amount is $5 \frac{1}{2} \%$ the same as $10 \frac{1}{2} \%$ of $£ 1100$ ?
10. What fraction of an acre is $0.01 \%$ of a square mile?
11. What is $15 \%$ of 8 tons 3 cwt .2 qrs.?
12. $£ 315 \mathrm{~s}$. is $2 \frac{1}{2} \%$ of a certain sum, what is that sum, to the nearest pound?
13. Of what area is 10 acres $12 \frac{1}{2} \%$ ?
14. If $15 \%$ of a clerk's salary is $£ 45$, what is that salary?

The list prices of a number of articles are given in Questions 15 to 24. Allow the percentage discount marked from each of them:

> 15. An occasional table, £3 $10 \mathrm{~s} . ; 5 \%$.
> 16. A bag of cocoa, £2 16 s . ; $2 \frac{1}{2} \%$.
> 17. A bag of walnuts, $£ 315 \mathrm{~s}$; $7 \frac{1}{2} \%$.
> 18. A fur coat, $£ 88 \mathrm{~s}$. ; $3 \frac{1}{2} \%$.
> 19. Black wolf stole, $£ 66 \mathrm{~s} . ; 10 \%$.
> 20. Pearl necklace, 100 guineas; $15 \%$.
> 21. Linen hamper, 28s. 6d. ; $3 \%$.
> 22. Field service greatcoat, £3 $10 \mathrm{~s} . ; 5 \%$.
> 23. Straw "boater," 4s. 6d. ; $2 \frac{1}{2} \%$.
> 24. Soft felt hat, $8 \mathrm{~s} .6 \mathrm{~d} . ; 4 \frac{1}{2} \%$.
$25.35 \%$, of the area of a piece of land is 5 ac .2 rds .20 sq. po. Find the area of the land.
26. What is $28 \%$ of a piece of gold weighing 540.864 grams?
27. What percentage is 1 sq. iv. of 1 sq. ft.?
28. Express the volume of a box 5 in . by 8 in . by 10 in . as a percentage of the volume of one 8 in . by 9 in . by 10 in .
29. What percentage is 1 d . of $£ 1$ ?
30. £5 can be borrowed and repaid at the rate of 2 s .4 d . a week for 52 weeks. What percentage is the amount paid for the loan of the amount borrowed?
31. A railway company has 8000 Km . of line open and it opens 85 Km . more. By how much per cent. has the length of line open been increased?
32. 5 tons is $3 \frac{1}{2} \%$ of the load a crane will lift. What is the load $\}$
33. The value of money orders issued in India in 1911-12 was $£ 32,475,933$, and in $1912-13, £ 34,854,327$. Calculate the increase per cent. in value.
34. The United Kingdom exported goods to the value of $£ 67,622,616$, and France to the value of $£ 1,452,674$, to India in 1913. What percentage is the value of goods exported from France of that exported from the United Kingdom?
35. The value of the silk imported ${ }^{1}$ into Russia through the European frontier increased from 2,211,000 roubles to $2,473,000$ roubles for the first half of the years 1912 and 1913. Calculate the percentage increase in value.
36. During one year the Bank rate ${ }^{1}$ was $4 \%, 3 \frac{1}{2} \%, 3 \%, 4 \%$, on four different dates. Find the percentage fall or rise, in each of the three intervals, on the rate at the beginning of that interval, and determine the greatest percentage variation.
37. A piece of "Crown" size printing paper is $20 \times 15 \mathrm{in}$., and a piece of "Royal," $25 \times 20 \mathrm{in}$. What must be the width of a piece of paper 40 in . long so that its area may be as much per cent. greater than the "Royal" as the "Royal" is greater than the "Crown"?
38. If one is 10 ft . above the ground in a large open ex panse of country he can see 4 miles; if he is 20 ft . he can see $5 \frac{3}{4}$ miles. Find how far he can see when 35 ft . above the ground, if the radius of vision is as much per cent. above $5 \frac{8}{4}$ miles as $5 \frac{8}{4}$ is above 4 miles.
39. Last year 23655 tons of copper were produced in Queensland, and the year before 23120 tons. Calculate the percentage increase from one year to the next.
40. In the same Colony (Question 39) for the same years 626 tons and 359 tons of wolfram ${ }^{2}$ were produced. Calculate the percentage decrease in the year.
41. In the year 1914 the coal production of the Donetz Basin (Russia) was $1,399,670,000$ poods, and in 1913, 1,252,310,000 poods. Calculate the percentage increase in production from 1913 to 1914.
42. In January 1915, 2576 tons of rubber were produced in the Straits Settlements, and this weight was $118.12 \%$ more than (not of) the weight produced in January 1914. Calculate the latter weight.
43. The duty on spirits imported into Nigeria has been raised recently from 6s. 3d. to 7 s . 6d. per imperial gallon. Calculate the percentage increase in the duty.
44. Last year the production of flax in Russia was $11 \frac{1}{2}$ poods per dessiatine ( 2.7 acres), and in the previous year it was $160.87 \%$ of this weight per dessiatine. What was the production in that year?
45. The price of British wheat in the week ending 27th November was 54 s .2 d ., and for the corresponding week last year 41s. 11d. per bushel. Calculate the average monthly percentage change in price for the year given.
46. A particular kind of perfumery imported into the United

[^27]States has to pay $48 \frac{1}{2} \%$ duty. An importer pays 500 dollars duty. What was the value of the importation?
47. The population of England and Wales was as follows:
(From WHITAKER'S ALMANACK.)

| Year. |  |  | Population. |  |
| :---: | :---: | :---: | :---: | :---: |
| 1811 | $\cdot$ | . | . | 10164256 <br> 12000236 |
| 1821 | $\cdot$ | . | . |  |
| 1901 | $\cdot$ | . | . | 32527843 <br> 1911 |

Calculate the increase per cent. in each decade, and draw some conclusions from Questions 47 to 50 and from their results.
48. The population of Scotland was $1,805,864$ in 1811 and $4,760,904$ in 1911. Calculate the average percentage increase per annum in the period given.
49. If the population of Ireland was $4,704,750$ in 1891, $4,458,755$ in 1901, and $4,390,219$ in 1911, calculate the decrease per cent. in each decade, and state whether there is any indication that the decrease is becoming more or less marked.
50. From the following data find the difference between the percentage decennial increase in the population of England and Wales for the periods 1891-1901 and 1901-1911, tabulating the results:

| Year. |  | Population of England and Wales. |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total. | Decennial Increase. |
| Porcentage. |  |  |  |  |
| 1891 | . | . | . | 29002525 <br> 32527853 <br> 1901 |
| 1911 | . | . | . |  |

## B. Commission and Brokerage

## I. COMMISSION

269. Jacobs \& Sons of Leeds (say) are large machinery manufacturers, and they wish to extend their business by opening up a market in South America. They therefore advertise for a man who has a practical knowledge of the trade and who can
speak Portuguese, and they tell him what they want and propose that they shall pay him just a nominal salary to cover his expenses perhaps, and then, let us say, $15 \%$ on the value of all the machinery he sells for them. On accepting the post he becomes one of Messrs. Jacobs \& Sons' travellers, and the amount he receives on his sales is called his Commission, and he himself might therefore be called a Traveller on Commission.

He then sets out for South America, furnished with catalogues and, if necessary, samples of steel, and sets about his business. If he sells $£ 5000$ worth of machinery he will get $\frac{10}{100}$ of $£ 5000$, or $£ 750$ commission.
270. Again, if we take an insurance company, the same thing happens, only it may have, and frequently does have, a representative in every town of any size, and it is the business of this Agent, as he is called, to get in touch with people and endeavour to get them to insure their houses, or furniture, or lives. Now suppose he gets a client to insure his house for $£ 1000$ and the premium is 24 s ., he will receive $15 \%$ commission on the 24 s ., and if he induced his client to insure his life for $£ 1000$ he would get $2 \frac{1}{2} \%$ commission on the $£ 1000$ and then $2 \frac{1}{2} \%$ on every premium paid afterwards.

## II. BROKERAGE

271. Mr. Whitefoot has received a large consignment of fruit from the West Indies, and he knows that he cannot transfer it to his stores and sell it quickly enough to prevent considerable loss through its becoming overripe. He therefore rings up Brown \& Sons, who, he knows, undertake the sale of such cargoes, and instructs them to sell for him immediately, agreeing to pay them perhaps $5 \%$ on the amount for which they sell the cargo. Brown \& Sons are called Brokers, and the percentage they are paid is called Brokerage. The difference between a commission agent and a broker is simply this, that the former sells goods, samples of which he often carries with him, while the latter need not even see the things he is going to sell, and may dispose of them 20 miles or 2000 miles from where they are, but the purchaser will, of course, see what he is buying beforehand.

Huge sales of property, for example, are held at Tokenhouse Yard, London, although the property may be anywhere.

Two of the chief classes of brokers are Stock Brokers and Bill Brokers, who are intermediaries between the buyer and seller, and who meet at the Stock Exchange and the Royal Exchange
respectively. The Ship Brokers also meet at the latter place, while Corn Brokers assemble in Mark Lane, and Brokers, who deal with Eastern and Colonial products, in Mincing Lane. There are also Corn, Coal, and other Exchanges in most of our large towns.
272. A broker usually charges $\frac{1}{8} \%$, and this constitutes his source of income. Not infrequently he charges both buyer and seller, and so gets $\frac{1}{4} \%$ on the deal.

It is necessary to distinguish between the two methods of paying brokerage or commission. We may say that we will pay $5 \mathrm{~s} . \%$, or $5 \%$. The former means 5 shillings on every $£ 100$, the latter $£ 5$ on every $£ 100$.
273. We now illustrate these points:

Example 1.-If an agent is paid $10 \%$ on sales, what should he receive if he sells $£ 25000$ worth of goods?

$$
\begin{aligned}
\text { Commission } & =10 \% \text { of } £ 25000 \\
& =£ 2500 .
\end{aligned}
$$

Example 2.-A commission agent is paid $2 \frac{1}{2} \%$ on sales, and makes $£ 300$ a year. To what do his sales amount?

$$
\begin{aligned}
& \text { He gets } £ 2 \frac{1}{2} \text { on } £ 100 \\
& " \quad \text { " } £ 1 \text { " } £ \frac{100}{2 \frac{1}{2}} \\
& ">£^{\prime 300} \mathfrak{L}_{2 \frac{1}{2}}^{100} \times 300 \\
& =£ 12000 \text {. }
\end{aligned}
$$

Example 3.-A broker sold a cargo for $2 \mathrm{~s} .6 \mathrm{~d} . \%$, and handed over $£ 799$ to the merchant. What was the value of the cargo, and what did the broker make?

With actual S.P., i.e. selling price, $£ 100$ the amount handed over would be £99 17s. 6d. ;
$\therefore$ the actual S.P., when $£ 799$ is handed over, is $\frac{799 \times 100}{99.875}$ $=£ 800$; and the broker gets $£ 1$.

## EXAMPLES. LXX.

1. An agent is paid $2 \frac{1}{2} \%$ on his sales, which amount to $£ 1000$ per annum. What is his income?
2. A traveller's income is $£ 500$, and it is $8 \frac{1}{2} \%$ of the value of the goods sold by him. What is that value?
3. If a commercial traveller sells 3586 francs' worth of silk
goods for his firm at Lyons, and receives 305 francs commission, at what rate per cent. is he paid, to one decimal place?
4. What should an agent receive in commission at the rate of $15 \%$, if his sales amount to 59863 dollars?
5. A commercial traveller receives $3 \frac{1}{2} \%$ on the value of the goods he sells, and his income is 75000 francs a year. What is the value of the goods sold?
6. An insurance company pays its agents $2 \frac{1}{2} \%$ on the value of the policies they secure. If an agent gets insurances to the value of $£ 350, £ 760, £ 1050$, and $£ 800$ in one year, what amount does he receive in commission?
7. If a broker is paid $\frac{1}{10} \%$ on the value of the business done for his client, what should he get on 85640 marks ?
8. A stock broker ${ }^{1}$ charges $2 \mathrm{~s} .6 \mathrm{~d} . \%$ on the value of the stock sold by him. What amount must he sell to give him an uncome of $£ 300$ per annum?
9. An estate agent lets a flat for seven years at a rental of £58 10s. a year. He receives $5 \%$ on the first year's rent and $2 \frac{1}{2} \%$ on that of each subsequent year for the term mentioned. What amount does he receive for his services?
10. A merchant purchases 36 small houses which are let at a weekly rent of 15 s . 9 d . each. An agent looks after the property, collects the rent for the owner, and reccives $7 \frac{1}{2} \%$ on the gross annual income. Find the amount the agent receives per annum, presuming all the houses are occupied during the whole year.
11. If in the last question an average of $2 \%$ of the houses were unoccupied during the whole year, find what the income would be both of the landlord and of the agent.
12. The agent for an insurance company does the following business in a year: (1) new life policies, $£ 10000$; (2) renewal premiums, $£ 73810 \mathrm{~s}$.; (3) fire insurance premiums, $£ 30015 \mathrm{~s}$. Calculate his commission at $2 \frac{1}{2} \%$ on (1) and (2), and $15 \%$ on (3).
13. A firm paid $£ 31919$ as commission to its agents, at the rate of $4 \%$. What value of goods was sold?
14. A company pays its agent $5 \frac{1}{2} \%$, and his account amounts to $£ 268814$ in a year. Upon what sum was this commission paid?
15. A firm pays brokerage on $£ 5194$ at the rate of $1 \mathrm{~s} .6 \mathrm{~d} . \%$. What amount is paid in brokerage?

## C. Profit and Loss

274. Wills \& Wills are cloth workers who, having conducted their business with care, find at the close of the year, when all ${ }^{1}$ See page 483,
their expenses are paid, bad debts allowed for, and a certain amount set aside to allow for depreciation of goods, machinery, etc., that they have $£ 3000$ more than they had last year. They have made then £3000 Profit. If trade had been bad, or they had been careless, they might have been $£ 500$ worse off than they were last year, in which case there would have been a Loss of $£ 500$.
275. Suppose now that the merchants referred to spent $£ 10000$ this year and made $£ 3000$ profit, and $£ 18000$ last year and made $£ 3600$ profit, they would of course wish to compare the results in order to see whether the profit made on the amount spent was improving or not. To do this they would reckon the profit made in each year on $£ 100$, simply because that sum is convenient to work with.

Now, $£ 3000$ profit on $£ 10000$ spent is $£ \frac{300}{0} \times 100$ on $£ 100$ spent.
$\therefore$ the profit per cent. is $£ 30$ this year.
Also the profit per cent. last year was $£ \frac{3600}{180} \overline{000} \times 100$, or $£ 20$.
It is now easy to see that the profit has increased from $\mathbf{£} 20 \%$ last year to $£ 30 \%$ this year, a fact which would have been very much more difficult to see if we had not reduced the profits to a percentage.

Few things are more helpful than to observe the percentage profits over a number of years and construct a graph for the same (see Part III.).
276. In many trades the profit is calculated on the cost price, but in some, such as the tea trade, it is usual to calculate the profit on the selling price, not on the buying price, for this reason: taking the retail tea trade year in and year out, the retail price is kept fairly constant, 1s. $4 \mathrm{~d} ., 1 \mathrm{~s} .6 \mathrm{~d} ., 1 \mathrm{ls} .8 \mathrm{~d} .$, etc., per lb. ; but the wholesale price varies, and consequently the tea is blended so that when sold for, say, 2 s . per lb . it will yield a profit of $15 \%$ or $17 \frac{1}{2} \%$, as the case may be.

In America, too, the profit is reckoned on the selling price (S.P.), and there are very good reasons for doing this, for when once an article has been listed, say, at $£ 10$, its selling price then becomes well known, and discounts, commissions, etc., are usually allowed upon that price, while the cost price (C.P.) can only be known by referring to the Purchases Book ( $\$ 171$ ). Again, if a merchant sells to make $10 \%$ on the cost price
and then subsequently deducts $10 \%$ from the selling price, he loses money (see Example 3, § 277).

We shall always reckon protit on the C.I., unless otherwiso stated.

2'ry. Exampie 1.-I buy a quantity of coal for $£ 50$ and sell it for $£ 70$; what is my profit per cent.?

Coal is bought for $£ 50$ and sold for $£ 70$
$\therefore$ profit on $£ 50$ is $£ 20$
and „ $£ 100$ is $£ 40$
$\therefore$ profit is $40 \%$.
Example 2.-A gentlemen's outfitter marks pyjamas at 23s. a suit and makes $15 \%$ on what he pays. Find the wholesale price per dozen suits.

We want the buying price, so we write-
He sells for $£ 115$ what he buys for $£ 100$

$$
\begin{aligned}
& \therefore \quad, \quad, 23 \mathrm{~s} \text {. } \quad, \quad \frac{100}{115} \times 23 \mathrm{~s} \text {. } \\
& \therefore \text { buying price }=20 \mathrm{~s} \text {. each, or } 240 \mathrm{~s} \text {. per dozen. }
\end{aligned}
$$

Example 3.-A merchant buys a canteen of cutlery for $\mathbf{£ 2 0}$ and lists it for sale at an increase of $20 \%$ on that price. He subsequently has it marked at $20 \%$ below the selling price to clear. What is his proflt or loss?
(1) If he buys it for $£ 100$ he lists it at $£ 120$
$\therefore \quad, \quad, \quad £ 20 \quad, \quad, \quad £ 20 \times \frac{120}{100}=£ 24$.
(2) If he lists it for $£ 100$ and reduces it to $£ 80$ to clear $\therefore \quad, \quad$, $\quad 244, \quad, \quad £ 24 \times \frac{80}{100}=£ 194 \mathrm{~s}$. $\therefore$ he buys it for $£ 20$ and sells it for $£ 194 \mathrm{~s}$., and so loses 16 s .

Example 4.-Mark biscuits which cost 3s. per 5-lb. tin to gain $20 \%$ in selling, and find the profit per pound.

We want selling price.
Biscuits bought for 100 s . are sold for 120 s .

$$
\begin{aligned}
& \quad \text { selling price is } 3 \mathrm{~s} .7 \mathrm{~d} . \text { per } 5-\mathrm{lb} \text {. tin. } \frac{120}{100} \times 3 \mathrm{~s},=3 \cdot 6 \mathrm{~s} . \\
& \quad \text { C.P. of } 5 \mathrm{lb} .
\end{aligned}=3 \mathrm{~s} . \quad \begin{aligned}
\text { S.P. of } 5 \mathrm{lb} & =3 \cdot 6 \mathrm{~s} . \\
\therefore \text { profit on } 5 \mathrm{lb} . & =0 \cdot 6 \mathrm{~s} .=7 \cdot 2 \mathrm{~d} . \\
\therefore \text { profit per lb. } & =\frac{72}{5}=1 \cdot 44 \mathrm{~d} . \\
& =1 \frac{1}{2} \mathrm{~d} . \text { nearly. }
\end{aligned}
$$

Example 5.-A merchant made a certain profit last year
and finds that this year's profit is $10 \%$ less than last year's. Find what loss he has sustained if the profit this year is £350.

We want last year's profit.
A profit of $£ 90$ this year means a profit $£ 100$ last year

$\therefore$ last year's profit was $£ 38817 \mathrm{~s} .9 \mathrm{~d}$.
$\therefore$ the loss is $£ 3817 \mathrm{~s} .9 \mathrm{~d}$.

## EXAMPLES. LXXI.

Calculate the percentage gain or loss on the Selling Pricr in each of the following transactions (Questions 1 to 10 ):

| Cost Price. | Selling Price. | Cost Price. | Selling Price. |
| :---: | :---: | :---: | :---: |
| 1. £3 6s. 6 d . | $£ 310 \mathrm{~s}$. | 6. $£ 895 \mathrm{~s}$. | 100 guineas. |
| 2. £2 14s. 7 d . | $£ 2 \mathrm{l}$ 16. | 7. £30 4s. 6d. | 25 guineas. |
| £3 9s. 4 drd. | $£ 315 \mathrm{~s}$. | 8. $4277 \cdot 8$ francs. | 5860 francs. |
| 4. $£ 82 \mathrm{~s} .1 \frac{1}{2} \mathrm{~d}$. | £88s. | 9. 13600 lire. | 10000 lire. |
| 5. $£ 517 \mathrm{~s}$. | $£ 610 \mathrm{~s}$. | 10. $4389 \cdot 6$ dollars. | 3720 dollar |

What percentage depreciation has taken place in the following sases (Questions 11 to 20):

Article. Cost Price.
11. A motor-cycle
12. A clock f5 15s 6d
13. A garden hose
14. A gramophone
15. A warship.
16. A cargo of timber
17. 10 tons of iron
18. 50 gallons of oil
19. 75 Kgm . of sugar
20. 80 tins of salmon

40 guineas.
む5 15. 6 d .
$£ 1$ 2s. 6d.
$£ 10 \mathrm{l} 5 \mathrm{~s}$.
£980000.
£8350.
$£ 18 \mathrm{l} 5 \mathrm{~s}$.
$£ 15$ 12s.
75 francs.
12 dollars.

## Second-hand

 Selling Price.
## $£ 25$.

£3 12s. 6d.
12s. 9d.
$£ 55 \mathrm{~s}$.
£5800.
£7480.
$£ 1510 \mathrm{~s}$.
$£ 12 \mathrm{l}$ s.
68 francs.
10 dollars 25 cents.
21. What would you gain per cent. by buying meat in Smithfield Market for 9 s .6 d . a stone and selling it at 1 s .3 d . per lb .?
22. A dozen pairs of ladies' hose cost 12 s . 8 d . ; what must they be sold at per pair to gain $15 \%$ ?
23. If penholders cost half a guinea a gross, what percentage profit is made by selling them at 1d. each?
24. What is the wholesale cost of gentlemen's " boaters" if a S.P. of 4 s .6 d . allows for a profit of $12 \frac{1}{2} \%$ on the C.P.?
25. A grocer sells $£ 150$ worth of sugar at a profit of $5 \%$, $£ 180$ worth of dried fruit at $7 \frac{1}{2} \%$, and $£ 350$ worth of tea and coffee at $8 \%$. What is his total profit, and what is his average profit per $£ 100$ received?
26. The profits on a business are 9750 dollars. One partner is to receive 950 dollars and then $10 \%$ of the remaining profits, while the other two are to have $40 \%$ and $50 \%$ respectively. By how much is the greatest amount received more than each of the other two?
27. A gain of $5 \%$ is made by selling apples for three a penny. Find the gain or loss per cent. by selling them at twenty-five for 6 d .
28. Find the profit made by buying 3 tons 6 cwt . of butter at $£ 514 \mathrm{~s}$. per cwt., and selling it at 1 s . $3 \frac{1}{2} \mathrm{~d}$. per lb .
29. A merchant finds that his turnover for the year is $£ 56500$, and that his profit is $15.55 \%$ of that amount. Calculate his net profit if he pays 2 s .6 d . in the pound income-tax upon his gross profit.
30. A silversmith has a perforated silver basket for which he has paid £10. If he reckons that $5 \%$ of the selling price must be absorbed in expenses, at what figure must he mark the article so as to make a clear profit of $15 \%$ on that price?
31. A farmer bought 50 cattle for $£ 850$. At what average price per head must he sell them to make a gross profit of $17 \frac{1}{2} \%$ ?
32. Coffee can be bought wholesale at 84 s . per cwt., and then has to pay duty at $1 \frac{1}{2} \mathrm{~d}$. per lb . If retailed at 1 s .3 d . per lb ., what percentage of the selling price is profit?
33. If a greengrocer, selling apples at three a penny, gains $5 \%$ on what they cost him, what will he gain per cent. if he sells five apples for 2 d .?
34. What would be a merchant's profit per cent. on his turnover if the former is $£ 1563$ and the latter is made up of : Cost of goods, $£ 5000$; wages, $\mathbf{3 0} \%$ of the cost of goods and the profit?

## EXAMPLES. LXXII.

## Miscellaneous Questions

1. During the attempted construction of a Panama Canal by M. de Lesseps, the owners of some land, valued at 75000 francs, are said to have received 800000 francs for the freehold.

Presuming this to be true, calculate the percentage profit made by the vendors of the land.
2. The average width of the ordinary channel of the Nile is $3 \frac{1}{2}$ miles, but when the inundation is at its height the channel is $20 \frac{1}{2}$ miles wide. By how much per cent. does the inundation increase the width of the channel?
3. A barrel of wine contains 36 gallons; 15 are drawn off, and the barrel filled up with water. What is the percentage strength of the mixture now?
4. A greengrocer made $£ 500$ profit on his businsss this year, and finds that this amount is $12 \%$ less than last year's profit. By how much does the profit this year differ from that of last year?
5. We find from our newspapers that South American chilled forequarters of beef sold at Smithfield at 3s. 10d. per stone, and English beef at 5 s . 1d. per stone. What percentage profit does a butcher make by selling Argentine meat as English?
6. Our butcher is selling us beef at 1 s . 1d. per lb. What percentage profit is he making when he bought it for 58.2 d . a stone. (Scotch long sides)?
7. Instead of taking 1 Kgm . as 2.2046 lb ., a merchant takes it as 2.2 lb . What percentage errur does he make, to three places of decimals, and what would be the total error made in converting 1 metric ton into pounds? (Give the answer in pounds.)
8. The foreign trade of Saffi (Morocco) amounted to $£ 537823$ in 1914, and $£ 972432$ in 1913. Calculate the percentage decrease in the year. ${ }^{1}$
9. The cotton production of India is estimated at $17,674,000$ cwt. for the present year, or $99.9 \%$ of last year's production. How many tons (to the nearest 10 tons) were grown last year?
10. The wheat production of the southern hemisphereArgentina, Chile, Australia, and New Zealand-is estimated at $134,234,000 \mathrm{cwt}$. for $1914-15$, as compared with $126,246,000 \mathrm{cwt}$. for 1913-14. What will be the increase per cent. if the production is in accordance with the estimate?
11. $675 \cdot 5$ million Kgm . of coffee were exported from Brazil ${ }^{2}$ in the year before last, and 724.8 million Kgm . last year. What was the percentage increase in the exportation in the year given?

[^28]12. Mark coffee bought at $£ 6$ per cwt. so as to gain $8 \%$, and find the profit per pound?
13. A merchant has premises in Liverpool and also at Bordeaux. At the former he sells ladies' stockings at $2 \mathrm{~s} .6 \frac{1}{2} \mathrm{~d}$. per pair, and at the latter 3 fr. 30 c. per pair. By how much per cent. does the higher price exceed the lower, and which is higher?
14. In the early part of the present year the prices for a $4-\mathrm{lb}$. wheaten loaf were stated to be: New York, $11 \frac{1}{2}$ d. to $1 \mathrm{~s} .5 \frac{1}{2} \mathrm{~d}$.; London, 8d. ; Paris, $7 \frac{1}{2}$ d. Find by how much per cent. the cost of a loaf in Paris was less than that in London, and by how much per cent. the average price of a loaf in New York exceeded that charged in London.
15. Flour cost $5 \frac{1}{3} \mathrm{~d}$. per $3 \frac{1}{2}-\mathrm{lb}$. bag (retail) last year, and 9 d . this year (1916). What is the percentage profit in the two cases if the wholesale prices were $4 \frac{1}{2} \mathrm{~d}$. and $7 \frac{1}{2} \mathrm{~d}$. respectively?
16. What percentage increase is 1 d . per lb . on soap which cost 1 fr. 25 c. per Kgm.?
17. $85,050,300$ acres out of $221,983,200$ acres were under winter sowings in Russia last year. What percentage of the whole was thus under winter sowings?
18. Taking the data of the last question, $136,932,900$ acres were under spring crops. What percentage was this?
19. The total yield of all grains in Russia last year was $55,167,000$ tons, which was $23.8 \%$ less than in the previous year. What was the grain yield of the previous year?
20. A signet ring costs a jeweller 17 s .6 d . He marks it 25 s., but ultimately disposes of it to a customer at $5 \%$ less than the marked price. What is his gain per cent. on the amount he paid for it and on the selling price?
21. If a pair of antique candlesticks is bought for 15 guineas and sold by auction for $£ 1210$ s., what is the loss per cent. on the original cost and on the selling price?
22. In the ten years 1901-11 the rural population of the Maritime Provinces, Ontario and Quebec, decreased from 2,903,470 to $2,864,647$. Determine the percentage decrease in population for the ten years given, and also the average annual percentage decrease.
23. A grocer sells sugar at $2 \frac{3}{4}$ d. per lb. and makes 2 d . profit on every 7 lb . he sells. At what price per hundredweight did he buy the sugar?
24. The population of Japan on 31st December 1913 was $52,985,423$, and on 31st December 1914, 53,596,858. What was the average increase per hundred inhabitants in the year given ?
25. The price of everyday household commodities has gone up $60 \%$ between 1899 and 1915 . How much have we to pay now for what we could get for 15 s . 9 d . in 1899? (Answer to nearest penny.)
26. Our papers tell us that the Clyde shipbuilders claim that the purchasing power of a sovereign has gone down to 14 s .9 d . What percentage drop has befallen the sovereign if this is true?
27. It is proposed to lease a particular area in Spain for the construction of a railway. The cost is estimated at 24,717,920 pesctas, and the Government guarantees (not more than) $5 \%$ per annum interest. If the full $5 \%$ is paid, what would this amount to in English money? (A silver peseta $=9.513 \mathrm{~d}$.)
28. If gas has gone up from 2 s . 8 d . to 3 s . 2d. per thousand, and we burn, on the average, 950 cubic feet a week in our office, how much per cent. will the bill be higher this quarter than it was last, and what will be the actual amount extra?
29. If beef costs 6 s .6 d . a stone at Smithfield Market, at what price per pound must it be sold so that the profit is $22 \%$ on the selling price?
$$
\text { Hint. -Selling price }-22 \% \text { of selling price }=\text { cost price. }
$$
30. In Japan Proper the value of the production of the forests was yen $102,342,867$ in 1912-13, and the output of chemical products of wood (charcoal, acetic acid, lime, pine black, pulp, camphor, and camphor oil) was valued at yen $26,047,873$. What percentage of the total value was derived from the chemical products of wood?
31. A furniture dealer buys an antique sideboard for $£ 286 \mathrm{~s} .8$ d., and marks it to gain his usual $15 \%$ on the selling price. What is the selling price?
32. If books are sold to retail dealers at thirteen to the dozen and $25 \%$ off the published price, what profit per cent. does a bookseller make in selling thirteen copies of a half-crown book for 2s. each?
33. In two successive years the United Kingdom exported to Norway motors, for petroleum, steam, etc., and transformers (electrical), to the value of 88400 and 108500 kronen respectively. Find the percentage increase from the first year to the second and its value in English money. ( 1 krone $=1 \mathrm{~s} .1 \frac{1}{2} \mathrm{~d}$.)
34. It is proposed to build 144 workmen's dwellings in one of the cities of the Netherlands at a cost of 340000 gulden. At what price must an English contractor be able to do the work in order to gain $15 \%$ on the amount it costs him? (1 gold florin or gulden $=1 \mathrm{~s} .7 .824 \mathrm{~d}$.)
35. The price of British wheat at Canterbury (Kent) rose from 30 s . 7 d . to 56 s . 11d. per quarter in the year ending 6th February 1915. What is the percentage increase on the price at the beginning of the year?
36. In the previous question find the average monthly percentage increase in the price of British wheat for the period given.
37. The wholesale price of coal was 24 s .6 d ., the retail price 26 s .6 d . a ton. What was the percentage profit both on the wholesale and on the retail price?
38. If the retail price of Canadian Cheddar cheese rose from $£ 415 \mathrm{~s}$. per cwt. to $10 \frac{1}{2} \mathrm{~d}$. per lb . in a month, find the percentage increase in profit if the wholesale price was 8 d . per lb . all the time.
39. A Japanese merchant dies worth yen 75600 , and his son, who succeeds to his property, has to pay a succession duty of $5 \%$; what is the amount of the duty in English money? (Yen 1 $=2 \mathrm{~s}$. $0 \frac{1}{2} \mathrm{~d}$.)
40. Taking a yen as 2 s ., what difference does this make to the succession duty in the last question?
41. A stock jobber ${ }^{1}$ dies worth $£ 350680$, and estates between $£ 200000$ and $£ 400000$ pay an estate duty of $12 \%$ in the United Kingdom. Calculate the amount the Government receives (to the nearest pound).
42. The Deputy Postmaster-General of Melbourne invites tenders to supply (1) 22 miles of paper-insulated lead-covered cable, and (2) 100 automatic recording registers. A deposit of $2 \%$ on the first $£ 500$ and $1 \%$ above that amount must be made with each tender. An English firm quotes £1375 12s. for part of the contract, what deposit must be paid?
43. What deposit in English money would a French firm pay if it tendered for the same part of the contract as that referred to in Question 42, if it quoted the cost as 33756 francs?
44. Which tender is the higher, and by how much, in English money (Questions 42 and 43)?
45. The total ordinary revenue of Japan for the present year is estimated at yen $534,065,000$, of which the monopolies in salt, camphor, ${ }^{2}$ and tobacco are expected to produce, respectively, yen $8,323,300,37300$, and $45,791,000$. What percentage of the total revenue is derived from each of these three sources?

[^29]46. The population of Chōsen (Korea) in 1913 was $15,164,066$, and the average increase in the ensuing year was $2 \cdot 27$ per hundred inhabitants. Calculate the population in 1914.
47. It is estimated that an army of $1,300,000$ men uses 687578 lb . of brass per day in the form of cartridges when on active service. If $5 \frac{1}{2} \%$ of this metal is recoverable, what weight is lost per day per man?
48. The price of copper is $£ 6215 \mathrm{~s}$. per ton for cash, and $£ 635 \mathrm{~s}$. at three months' credit. If the former is sold at a profit of $10 \%$ and the latter at $12 \frac{1}{2} \%$, find the total profit made by the vendor on 6 tons of the former and 4 of the latter.
49. On entering into partnership four merchants agree that the first shall have $£ 200$, the second $£ 100$ and $5 \%$ of the remaining profits, the third $£ 80$ and $30 \%$ of the profits remaining after the first two have been paid and the third has received his $£ 80$, while the fourth shall have the residue. If the profits are $25 \%$ of the capital, which is $£ 12000$, calculate the amount each partner receives. (Check the result.)
50. The price of tea goes up $3 \%$ and the consumption goes down $2 \%$. By what percentage is the original amount spent on tea increased or diminished?
51. The revenue derived from the Excise duties in the United Kingdom amounted to 38 million pounds last year. If the consumption increases so that the revenue is $38 \frac{1}{4}$ million pounds, by what percentage may the duty be diminished so that there may be no loss to the State on last year's figures (to two places of decimals)?
52. Tea valued at 2 s . 6 d . per lb . is mixed with an inferior sort at ls. per lb . in the ratio of 2 lb . of the former to 6 lb . of the latter. At what price per pound must the mixture be sold to gain $10 \%$ ?
53. $34,224,700 \mathrm{Kgm}$. of zinc ore were dug in Austria in 1913, a decrease of $1.3 \%$ in quantity on the 1912 production. How many Kilograms of zinc ore were produced in $1912 ?$
54. The value of the ore referred to in the last question was $2,073,820$ kronen in 1913, a decrease of $28.2 \%$ in value compared with 1912. Find the value of the ore in 1912.
55. Taking the result of the last two questions, find the value of 1 Kgm . of ore in each of the years given (to two significant figures), and the percentage decrease in the value of 1 Kgm . in the second year given.
56. In the year 1912-13 the Government of India spent $£ 3,301,928$ on irrigation and received $£ 1,109,289$. What percentage return did the Government receive on the money spent ?
57. In 1903-4, 48000 chests of opium were sold for export, and the average price per chest was 1462 rupees. In 1912-13 the figures were 17890 chests at 2784 rupees each. Calculate the percentage decrease in the quantity sold, and the percentage rise in the price per chest. Comment upon the figures given in this question and upon the results obtained.
58. The paid-up capital of a company is $£ 585000$, and the dividend declared is $3 \frac{1}{2} \%$ per annum. What is the amount of the dividend?
59. If there are 3000 shareholders in the company of the last question and the payments to each are the same, what would a shareholder receive in a year by investing his dividend at $4 \frac{1}{2} \%$ per annum?
60. A railway company in the United Kingdom paid compensation in a year as follows: (1) To passengers, £4037 9s. 7d. ; (2) to workmen, £9318 18s. 9d.; (3) for damage and loss of goods, $£ 19785 \mathrm{5s} .7 \mathrm{~d}$. What percentage of the whole compensation paid fell under each of the three heads (1), (2), (3) ?
61. The owner of a cotton mill has a house for which he paid $£ 575$ and which he lets at a rental of $£ 45$ per annum. The cost of repairs averages $£ 6$ a year, and, in the course of ten years, he has had it empty in all three quarters (of a year, of course). What has been his average percentage return per annum?
62. If the Norwegian Government allows a preference of $12 \frac{1}{2} \%$ on Norwegian manufactures, what amount would be allowed on domestic manufactures introduced into a contract and valued at $£ 565816 \mathrm{~s} .8$ d. ?
63. We find from our newspapers that a sovereign was worth $25 \cdot 35$ francs on a particular day and $25 \cdot 45$ the next day. Calculate the percentage change in value.
(Look in your newspapers to-day and to-morrow and find the value of $£ 1$ in francs, and compare with the figures given.)
64. The traffic receipts of a railway company were $£ 5,250,433$ 8 s. 6d., and $£ 2501577$ s. was spent on the renewal and maintenance of locomotives. What percentage of the traffic receipts was spent in this way?
65. If the rates paid by the company referred to in the previous question were $£ 263999$ 6s. 2d., find what percentage this amount was of the total traffic receipts.
66. In 1903, 42.05 men per thousand in the British Army in India were lost through sickness, death, or invaliding, and 11.34 per thousand in 1912. By what percentage of the 1903 figure has the loss diminished on the average in each year?
67. The returns of a railway company show the season ticket receipts to have heen: First class, £103104 9s. 5d.; total receipts, $£ 2929416 \mathrm{~s} .8 \mathrm{~d}$. What percentage of the total receipts was derived from the second and third classes taken together?
68. If, in the last question, the second class receipts were $£ 629127 \mathrm{~s} .10 \mathrm{~d}$., find what percentage of the total was derived from third class season ticket-holders.
69. The tolls received on a canal in England amounted to $£ 2567 \mathrm{~s}$. in a year, and the cost of maintenance was $48.6 \%$ of this amount. Find the cost of maintenance, and hence the profit.
70. The working expenses of a steamship company were $£ 2773065 \mathrm{~s} .9 \mathrm{~d} .$, and the cost of fuel $£ 66182 \mathrm{ls}$. What percentage of the expenses is due to the cost of fuel?
71. If the cost of stores, lubricants, and water (see Question 70) had been $4 \%$ of the working expenses, how much would the company have expended on this item?
72. A company owning and working a number of docks, harbours, and wharves finds its income is $£ 3761572 \mathrm{~s}$., and that $2 \%$ of this has to be spent on dredging. What amount is spent in this way?
73. If in the previous question $12 \%$ of the income is spent on "maintenance," what is the amount so spent?
74. An electric lighting company supplies power as follows: (1) For traction, 750100 units, producing $£ 28278 \mathrm{~s}$. 2d. ; (2) for power, 95130 units, producing $£ 6269$ s. 5 d . ; (3) for lighting, 688500 units, producing $£ 401110$ s. 3d. With a view to the next question, find the cost per thousand units in parts (1), (2), and (3).
75. Employ the result of Question 74 to find by how much per cent. the highest charge per thousand units exceeds the lowest.
76. Taking the result of Question 74, find by how much per cent. the second largest charge per thousand units exceeds the lowest. Comment upon the charges made.

## SECTION XIX

## DOUBLE ENTRY IN ACCOUNTS

278. Before proceeding to this section the student must revise thoroughly §§ 171-182.

In § 171 we saw that William Towney bought cloth from John Nelson, so that the former bought goods while the latter sold them; it is clear then that the transaction involved two items-(1) receiving cloth, (2) selling it, and it is easy to see that this is true for all commercial transactions. Hence every firm
will make two entries for each transaction, and this is the fundamental principle of Double-entry Book-keeping.
279. Double-entry book-keeping is not double the work of Single Entry, for a number of items, such as discounts (§ 181, note), can be entered into the Ledger as one item.

By a Ledger ${ }^{1}$ we mean a book into which all the items from the Subsidiary Books are posted, and one which enables the counting-house manager to determine the financial position of the firm and the condition of each separate account.

Never put any item into the ledger except it has first appeared in one of the subsidiary books, and always put in the proper Ledger column the number of the page of the Subsidiary Book upon which the item can be found.
280. There are three kinds of accounts-(1) Personal Accounts, which we shall denote by ( P ) ; (2) Real Accounts, consisting of the Cash Accounts, Bank Accounts, Machinery, Plant, and Property Accounts, marked (R); and (3) Nominal Accounts, which include all accounts concerned with the profits and losses of the business, marked (N).

All N Accounts are therefore Profit and Loss Accounts.
281. We shall now proceed as follows:
I. Explain how to post very simple items into the Ledger, presuming that we have taken them from the Subsidiary Books.
II. Post into the Ledger direct from those books.

## I.

The student must, if he wishes to learn bookkeeping, take a piece of properly ruled Ledger paper and put down item by item for himself as we proceed, and not rely upon the model Ledger which we have put at the end of this exercise so that the student may not consult it until he has completed his work.
282. Example 1.-John Brown begins business with Cash, £50; he buys a horse for $£ 20$, and sells it for $£ 30$. How does he stand ?

[^30]Item 1.-Jan. 1. John Brown begins business with Cash, £50; $\therefore$ J. B.'s capital is $£ 50$, so we open a Personal Ledger Account, "John Brown: Capital Account," and have to decide whether the $£ 50$ is a $D r$. or Cr. entry, and we always look at it from the point of view of "the business." J. B. puts $£ 50$ into the business, $\therefore$ the latter owes J. B. £50; . J. B.'s account is one of its creditors; $\therefore$ the $£ 50$ is a credit entry, "Jan. 1. By Cash, £50."

If the business owes a person money we credit his account, but if he owes the firm money we debit his account.

Now, the cashier receives that $£ 50$; $\therefore$ he makes a $D r$. entry in his Cash Account ${ }^{1}$ (§ 178): "To John Brown, £50," and thus completes the double entry.

Item 2.-Jan. 2. He buys a horse for $£ 20$, and presumably pays for it in cash, so we open a Horse Account (Nominal Account), and that is $D r$. to the business for the value of the horse, hence we make a Dr. entry, "Jan. 4. To Cash, £20," and since the cashier has paid that money out he enters, "Jan. 4. By horse, $£ 20$," in the Cash Account, and thus completes the double entry.

Item 3.-Jan. 5. He sells the horse for $£ 30$, so we credit the Horse Account (N), "Jan. 5. By Cash, £30," and write "Jan. 5. To Horse, $£ 30$," in the Cash Account, since the cashier receives $£ 30$ cash, and thus complete the double entry.
283. In order to see whether our entries are probably correct we add up the $D r$. and $C r$. totals and see whether they agree-that is to say, we make a Trial Balance, from which we see that the $D r$. and $C r$. totals are $£ 100$.

TRIAL BALANCE.


[^31]In practice, accountants usually take the Balances of the various accounts and find whether the total Dr. Balances equal the total $C r$. Balances, but we must clearly understand what a Balance is.

If the $D r$. side of the Cash Account is heavier than the Or. side we have cash in hand (§ 179), or we have a Debit Balance, so that qhe Balange is the difierenof between the amounts on the two sides, and is always brought down on the heavier side, except in Nominal Accounts. ${ }^{1}$ Hence we have: Balance of Capital Account is £50 on the Cr. side, of the Cash Account $£ 60$ on the $1 r$. side, and of the Horse Account $£ 10$ on the $D r$. side, whence the usual form of Trial Balance:

TRIAL BALANCE.

again suggesting that our work is correct (see § 288).
(If the student finds his work wrong he may compare with the model at this point.)
284. Now if we look at the Horse Account we shall see that it is the only one upon which profit or loss could be made in this case, but if J. B. had bought a cow, or paid wages as well, we should have had other accounts which could well involve, in one way or another, profit and loss. All such accounts are Nominal Accounts, and therefore all Nominal Accounts involve Profit or Loss.

Again, if J. B. makes a profit, he increases his capital, for he has more money to go on with, and in this case he made $£ 10$ profit, which is shown as a Cr . balance in the Horse Account, hence a credit balance in a Nominal Account means a profit, or, more simply, if the Cr. side of a Nominal Account is the heavier, the balance shows the profit, ${ }^{2}$ and since the profit

## ${ }^{1}$ See $\S \S 285$ and 286.

2 If the student remembers this he will have no further trouble with nominal accounts, for a $D r$. balance clearly means a loss.
increases the Capital Account we ought to close all Nominal Accounts and transfer their balances to the Capital Account, instead of bringing them down and leaving them ready for the next trading period.
285. Instead of transferring all nominal balances directiy to the Capital Account, we draw up one account called a Profit and Loss Account (P. and L. Account) and transfer all Nominal Account balances to that account, balance ir, transfer its balance to the Capital Account, and by working in this way we are able (1) to see all the items contributing to profit or loss in one account, the P. and L. Account, (2) to transfer one balance and one only to the Capital Account, (3) to see in a moment from that account the net profit or loss.

We now total and balance the Cash Accounts ( R ) by writing "Jan. 6. By balance c/d, £60," total the account, and then carry down the balance to the heavier (Dr.) side, and learn that we have cash in hand, £60, which can be used for future transactions.

Now balance the Horse Account (N) or, as we may call it, the $P$. and L. Account ( N ), and learn that since the Cr. side is heavier there is a profit, which we put on the $C r$. side of Capital Account, and then balance the latter and so find the new capital, $£ 60$, with which to continue business.
286. One step more has to be taken. We have closed the Horse Account or P. and L. Account, and with it all Nominal Accounts, however many there may be ; the Capital and Cash Accounts remain, and the former tells us that the business owes J. B. £60, while the latter gives us the comforting information that we have just $£ 60$ in hand to pay Mr. Brown the amount due to him. The Liabilities are $£ 60$ but the Assets are $£ 60$ too, so that the firm is solvent. We represent this all-important fact in a Balance Sheet thus:

Balance sheet, January 6, 191-.

(The student can now compare his Ledger with the model, if his Trial Balance or Balance Sheet is wrong.)
287. In speaking of the Trial Balance (§ 283) we said that the agreement of the Balance totals "suggested" that the
work was correct, but the books are not necessarily right because the Trial Balance is correct, for-
3. All the transactions may not have been recorded, while a fictitious entry might have been inserted, and yet the Trial Balance would still appear correct if equal amounts had been left out from or inserted upon fach side.
2. Entries might be made in wrong accounts hit on the right sides.
3. The clerk who makes out the Trial Balance might have had inaccurate entries handed to him by other clerks.

On the other hand, the Trial Balance does indicate that the accounts are tolerably accurate, and it also gives a very conveniently arranged summary as to the condition of outstanding accounts.
288. MODEL LEDGER ${ }^{1}$ (L).
(The $D r$. and $C r$. items composing the double entry of any one transaction are in similar type.)


| Dr. |  | ( ASH ACCOUNT (R). |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\lvert\, \begin{aligned} & \text { Jan. } 1 . \\ & \text { Jan. } 5 . \end{aligned}\right.$ | To John Brown <br> To Horse | ¢ <br> 50 <br> 30 | s. | d. | Jan. 4. <br> Jan. 6. |  | ¢£ <br> 20 <br> 60 <br> 10 | 8. | d $\begin{aligned} & \text { d } \\ & 0 \\ & 0\end{aligned}$ |
| Jan. 6. | To Balance b/d (Cash in hand) | $\frac{80}{60}$ | - | $\frac{\square}{n}$ |  |  | 80 | 0 | $0$ |

(as it would appear in the cash columns of the Cash Book).

${ }^{1}$ We omit the folio numbers here (see § 281, I).

## EXAMPLES. LXXIII. (a)

1. What good purposes does a Ledger serve?
2. What is the fundamental reason for Double-entry Bookkeeping? Why is it not twice the work of Single Entry?
3. What kinds of accounts are there? Classify : Capital Account, Cash Account, Bank Account, Horse Account, Sheep Account, Ink Account, Silk Account.

Post into the Ledger the following entries presumed to be taken from the Subsidiary Books, take out a Trial Balance and a Balance Sheet (Questions 4 to 6).
4. J. Tree opens business, July 1, Cash in hand, £30; he buys a cart for £5, July 8, and sells it for $£ \&$, July 15.
5. T. Brown begins business, April 1, Cash in hand, $£ 40$; he buys cloth for $£ 8$ and sells it for $£ 16$ on $A_{\text {pril }} 12$.
6. E. Wilson begins business, May 3, Cash in hand, $£ 60$; he buys woollens, $£ 30$, and sells them for $£ 35$ on May 10.
7. Is the balance of an account on the heavier or lighter side?
8. If there were a loss, which side of the $P$. and $L$. Account would be the heavier?
9. What does (1) a Cr. balance, (2) a $D r$. balance in the Capital Account mean?
10. T. Hill puts $£ 50$ into the business and draws out $£ 60$. Show the Capital $\Lambda$ cocount supposing that there are no other items.
11. Why is the balance of a Nominal Account carried to the Capital Account?
12. In our Silks Account we have £20 Dr., £30 Cr. What does that mean? On which side does the balance fall? What do you do with it? Is it a gain or a loss?
13. In our Cash Account we have "Dr. Jan. 1. To satins, $£ 40$ "; "Cr. Jan. 8. By Cash, $£ 60$," and all the satin is sold. How do we stand?
14. T. Wills' Capital Account shows a debit balance, $£ 10$; what does this mean?
15. J. Brown opens business, Jan. 1, with £400; on Jan. 8 he buys iron goods for $£ 200$, and on Jan. 15 sells them for $£ 150$. Prepare the Ledger Accounts, Trial Balance and Balance Sheet, and comment on the position, explaining the meaning of all the balances.

## II.

289. In the following exercise we shall again presume that we have taken the entries from the Subsidiary Books and shall also keep the Cash and Bank Accounts separate, although they
would appear in the Cash Book in the ordinary way-in other words, in everyday business the Cash Book includes two Ledger Accounts, namely, Cash Account and Bank Account, but we separate them here to emphasise the principles of posting into the Ledger.
290. Example 2.-Henry Wills began business with: Cash in hand, $£ 100$; Cash in Bank, $£ 100$; he purchases boots for $£ 90$ and sells them for $£ 135$, pays $£ 5$ in wages and $£ 1$ in rent. Draw up the Ledger Accounts and Balance Sheet.

The student will please write down the items in his Ledger as before.

Item 1.-Cash in hand, $£ 100 ; \therefore$ the cashier on receiving the money enters on the Debit side of the Cash Account, "To H. Wills' Capital Account, £100," and we credit Henry Wills' Capital Account, " By Cash, £100," as in Example 1.

Item 2.-Cash in Bank, £100, which is also H. W.'s capital ; so we open a Bank Account ( R ), and since the Bank receives the money it is debtor to the firm for the amount, so we have in the Bank Account a Dr. entry, "To H. W.'s Capital Account, £100," and the corresponding Cr. entry in HI. W.'s Capital Account, "By Bank, £100," thereby showing that the Bank owes H. W. that amount, and completing the double entry.

Item $3 .-\mathrm{He}$ purchases ${ }^{1}$ boots for $£ 90 ; \therefore$ we open a Ledger Account and call it "Purchases Account (N)," which is now $D r$. to the business for $£ 90$, while the cashier records the payment in his Cash Account, "By Purchases, $£ 90$," and so completes the double entry.

Item 4.-He sells the boots for $£ 135 ; \therefore$ we open a Sales Account (N) ; the cashier receives $£ 135$ and enters in the Cash Account, "To Sales, $£ 135$ "; and since the Sales Account has parted with the goods, as it were, we credit that account and enter in it, "By Cash, $£ 135$," and so complete the double entry.

Item 5.-Pays wages by cash; so we open a Wages Account (N) and make a debit entry ("Debit losses, Credit gains," the wages are a "loss" to the business), "To Cash, £5," and the Cr . entry in the Cash Account, "By Wages, $£ 5$," completes the double entry.

Item 6.-He pays rent, $£ 1 ; \therefore$ we open a Rent Account (N) and make the Dr. entry "To Cash, $£ 1$ "; and then the Cr. entry

[^32]in the Cash Accuunt, "By Rent, $£ 1$," again completes the double entry.

The student should have made his own ledger entries and should continue to do each item for himself and not rely upon our models.
291. We now procced to make out a Trial Balanoe, and first of all jot down the balances in order thus :

Capital Account : Cr. side heavier, $\therefore$ there is a Cr. balance which amounts to $£ 200 .{ }^{1}$

Cash Account: Dr. side heavier, $\therefore$ there is a $D r$. balance, $\therefore$ there is cash in hand which amounts to $£ 139$.

Bank Account: Dr. Side heavier, $\therefore$ there is Cash at Bank amounting to $£ 100$.

Purchases Account, Wages Account, Rent Account: Dr. balances of $£ 90$, $£ 5$, and $£ 1$ respectively ; Sales Account: Cr . balance, $£ 135$.

TRIAL BALANCE.

|  | Balances. |  |
| :---: | :---: | :---: |
|  | Dr. | Cr. |
| Capital Account (P) | £ s. $d$. | $\begin{array}{ccc} f & s . & d . \\ 200 & 0 & 0 \end{array}$ |
| Cash Account (R) . - | 13900 |  |
| Bank Account (R) ${ }^{\text {a }}$ | $\begin{array}{lll}100 \\ & 0 & 0\end{array}$ |  |
| Purchases Account ( N ) | 90 50 0 |  |
| Rent Account (N) | 10 |  |
| Sales Account (N) |  | 1350 |
|  | 3350 | 33500 |

From the above we conclude that our Ledger is probably correct. (The student will now draw up a Trial Balance, using the totals.)
292. We now (1) balance the Nominal Accounts ; (2) transfer their balances to the P. and L. Account ; (3) balance the P. and L. Account and find the profit or loss; (4) transfer that balance to the Capital Account.

Taking the Purchases Account we write on the Cr. side, "Jan. 31. By balance carried forward to P. and L. Account $£ 90$," or more shortly, "Jan. 31. By I'. and L. Account, £90,"

[^33]and then transfer that to the $D r$. side of the $P$. and $L$. Account, for the Purchases Account has a debit balance as the Dr. side is the heavier. Treating all the Nominal Accounts similarly, we make nut and balance the P. and L. Account thus:


We now transfer the net profit to the Capital Account, balance it and the two Real Accounts, and then make out the Balance Sheet. Be very careful not to touch the Nominal Accounts again now, for they have all been included in the P. and L. Account and so transferred to the Capital Account, which therefore includes them all and represents them on the Balance Sheet:
293.

BALANCE SHEET, January 31, 191-.

which proves that our books are correct.
294. MODEL LEDGER (II).


[^34]

| Dr. |  | BANK ACCOUN'T (R). |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 1. | To Henry Wills, Capital a/c | $\left\lvert\, \begin{gathered}\text { £ } \\ 100\end{gathered}\right.$ | 8. $d$. <br> 0 0 | Jan. 1. | By Balance c/d | $\stackrel{£}{100}$ | $\stackrel{8}{8}$ | ${ }_{0}$ |
|  |  |  | 0 |  |  | 101 | 0 | 0 |
| Feb. 1. | To Balance b/d (Cash in Bank) | 100 | $0{ }_{0} 0$ |  |  |  |  |  |






## EXAMPLES. LXXIII. (b)

1. To what extent can we rely upon a Trial Balance?
2. What items are entered (a) in the P. and L. Account, (b) in the Balance Sheet?
3. Where would you expect to find : (a) a net loss; (b) a net gain; (c) the amount of capital for the ensuing month; (d) whether J. Lee owed us money or we owed him ; (e) what wages had been paid in the month; $(f)$ what cash there was in hand ; and (g) in the Bank?

Post into the Ledger, make out the Trial Balance and Balance Sheet, decide the net profit or loss, and the amount of capital for the next month (Questions 4 to 6 ):
4. Henry James began business, Jan. 1, with $£ 300$ cash in hand; he bought some bicycles for $£ 75$ on Jan. 10, and sold them for $£ 100$ on Jan. 18; paid wages, $£ 10$; and rent, $£ 2$, Jan. 30.
5. T. Nett began business, June 1, with $£ 180$ in hand; he bought furniture for $£ 75$, sold it for $£ 100$ on June 18 ; paid wages, June 29, £15, and rates, £5, on June 30.
6. Wm. Johns has cash in hand, July 1, £100; in Bank, $£ 500$; he bought 10 loads of timber for $£ 60$ each, sold 8 for $£ 80$ each on July 15, and 2 for $£ 50$ each on July 28. He paid cartage, $£ 2$, and his gas bill, $£ 3$.

## III.

295. There is one Subsidiary Book, The Journal, which must be considered in addition to those referred to in $\$ 171$ to 182.

The Journal was originally the only book of first entry, and the early Italians used it for every transaction prior to posting to the Ledger ; but now other books scrve for sales, purchases, cash, Bank, and discount items, and the Journal includes the Following entries only :

1. The opening entries (§297).
2. Such entries as the purchase of machinery, plant, etc., which are not for sale and so do not appear in Purchases or Sales Books.
3. The closing entries ( $\$ 307$ ).

In the following exercise we trace the operations through all the Subsidiary Books and then post into the Ledger and complete the Balance Sheet.
296. Example 3.-Record the following transactions of Henry James in the Subsidiary Books, post to Ledger, take out a Trial Balance, prepare a Profit and Loss Account and Balance Sheet.

He began business, Jan. 1, with cash in hand, $£ 10$; in Bank, $£ 700$; goods on hand, £50. A. Bell owed him $£ 40$; J. Hudson owed him £30; he owed E. Brown £28. The transactions were:


## THE JOURNAL-OPENING ENTRIES

297. (1) Henry James had been conducting his business prior to Jan. 1, and the Journal entries are made to ascertain what capital he has on that date, but his capital is the excess of his assets over his liabilities; $\therefore$ we find, from the data given, (1) his assets, (2) his liabilities, subtract, and so arrive at his capital.
(Note that no transaction that takes place after Jan. 1 enters into this matter at all. We want the capital on Jan. 1.)

The student will make out the Journal.

## 298.

THE JOURNAL.
10.

|  | Opening Entries. Henfy James. Asscts- | $\begin{aligned} & \text { Ledger } \\ & \text { Folio. } \end{aligned}$ |  | £ | 8. $d$. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Cash in hand . | 8 | 1000 |  |  |
| 2 3 3 | Cash in Bank. | 8 | 7000 |  |  |
| 4 | Value of goods on hand | 15 15 | 50 40 40 |  |  |
| 5 | J. Hudson's (delt) . | 15 | 3000 |  |  |
| 7 | Lialilities- <br> To E. Brown <br> To Heury James' net eapital | 15 |  | 28 802 | $\begin{array}{ll}0 & 0 \\ 0 & 0\end{array}$ |
|  |  |  | 8300 | 830 | 0 |

Items 1 and 2 should be carried forward at once to the Cash Book, Dr. side, Cash and Bank columns respectively :
"Jan. 1. To Balance brought forward, $£ 10$ " (Cash column), and " £700" (Bank column).

The others will be posted into the Ledger later on (§303).
299. (2) It is now necessary to take the business transactions during the month and enter each of them into the appropriate book of first entry; to avoid mistakes they mUST always be taken in order, just as they stand.

The student will now rule up pages for Purchases, Sales, and Cash Books, and make the following entries:

Item 1. Sales Book Entry as shown.
2. Cash Book Entry, Cr. side, Bank column, "Jan. 2. By E. Brown, $£ 27$ "; Discount is a gain, and $\therefore$ a Cr. entry ; Discount column, £l.
3. Cash Book Entry, Cash column, Dr. side, as it is Cash Recd., "Jan. 4. To J. Hudson, £20."
4. Purchasks Book Entrry as shown.
"
5. Cash Book Entry, Cash column, Dr. side, "Jan. 9. To A. Bell, £50, which amount is accepted in full settlement of his account," but he owed $£ 40$ on Dec. 31 last, and received goods valued £25 on Jan. 1, $\therefore$ he owed $£ 65$, and since he pays only $£ 50$, he had received $£ 15$ as a discount, which is a loss to Henry James and $\therefore$ a Dr. entry in the Discount Column of his Cash Book.

Item 6. Casi Boor Entry, Bank Column, Dr. entry, "Jai. 11. To Cash, $£ 75, "$ and since this amount is also received by the Bank and the cashier records such a fact, we must write in the Cr. side, Cash column, "Jan. 11. By Bank, £75."
7. Cash Book Entry, a payment, and $\therefore$ a $C r$. entry in Cash column, "Jan. 12. By sundry expenses, £4."
8. Casin Book Entry, Bank Column, and being a payment from the firm's funds it is a Cr. entry, "Jan. 15. By Henry James, drawings, £100."
9. Casi Book Entriy, Bank Column, and a Cr. entry, as it is a payment, "Jan. 16. By E. Brown, £75." 10. Casil Book Entry, Bank Column, being a payment to the Bank Account, it is a Dr. entry, "Jan. 27. To sales, £150."
" 11. Cash Book Entry, Bank Column, Cr, side, "Jan. 28. Jiy salaries, £10."
12. Journal Entry just as $3, \$ 298$, hut see $\S 307$.

Now compare your records in the Subsidiary Books with the models given and see whether they agree.
300.

| Number of Invoice. | Date. | Particulars. | $\begin{aligned} & \text { Ledyer } \\ & \text { Folio. } \end{aligned}$ |  | tails. |  |  | als. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 51 | $\stackrel{191-}{\operatorname{Jan} .} 7 .$ | E. BrownSilks Satins . | 15 | $\pm$ | s. | d. | £ | $s$. | $d$. |
|  |  |  |  | 100 | $0$ | 0 |  |  |  |
|  |  |  |  | 50 | 0 | 0 | 150 | 0 | 0 |
|  |  |  |  | 150 | 0 | 0 | 150 | 0 | 1 |

THE SALES BOOK.
6.


302. It is now necessary to post-1. From the Journal, and 2, from the other Subsidiary Books into the Ledger, and we emphasise two points:

1. We shall not open Cash and Bank Accounts in the Ledger, but regard the Cash Book as a Ledger Account which will, at the end of the month, tell us at once our cash in hand, cash in Pank, and the amount of discount allowed to us and by us.
2. The student mUS' now take some sheets of paper ruled as a Ledger, and make the entries upon them item by item as we procced, ignoring our model until he has finished, and then compare his record with that in the book. We cannot make too much of this point.
3. I. Posting the opening entries from the Journal into the Ledger (of which the Cash Book forms a part).

Journal Items 1 and 2 have already been dealt with ( $\$ 298$ ), and since it is usual to open the Capital Account first we take Item 7 and open H. J.'s Capital Account with a Cr. entry: "Jan. 1. By Balance, $£ 802$ " (i.e. By Balance due to H. J. from the business).

Next, taking Item 3, we open a Stock Aocount with a $D r$. entry: "Jan. 1. To Balance from December, £50." This is a Dr. entry, since we regard the Stock Account as a Dr. to the business, and the stock-keeper is responsible to the business for that value.

Items 4 and 5 are similarly entered to the $D r$. side of $A$. Bell's and J. Hudson's Accounts.

Item 6 is a Cr. entry in E. Brown's Account: "Jan. 1. By Balance, $£ 28$," for we owe him that amount and he is therefore one of our creditors.

## 304. 2. Posting from Purchases and Sales ${ }^{1}$ Books into the Ledger.

1. Open Purchases and Sales Accounts in the Ledger.
2. Open accounts for every person named in those accounts.
3. It is not necessary to enter every item from the Purchases and Sales Books into the Purchases and Sales Ledger Accounts, but to enter the monthly totals, provided that
4. The separate items are entered in the various accounts opened under 2 (above), for if we have bought goods valued at $£ 100, £ 200, £ 300$, and $£ 400$ from A, B, C, and D, and we credit

[^35]each of their accounts with the goods sent by them, then the total credit amounts will be $£ 1000$, and if we debit the Purchases Account with that total we have, to all intents and purposes, completed the double entry but without doing twice the work of single entry.

## (a) Posting from Purchases Book

Since E. Drown is one of H. .J.'s creditors, we make a credit entry in E. B.'s Account: "Jan. 7. By goods, £150"; and since the total fur the month is, in this case, $£ 150$ also, we make a $D_{i}$. entry in the Purchases Account: "Jan. 31. To total for the month, $£ 150, "$ thus completing the double entry.

This transaction leads us to the following rule: "The accounts of all persons whose names appear in the Purchases Book must be credited with the respective amounts and the Purchases Account debited with the total of them."

## (b) Posting from the Sales Book

Since $\Lambda$. Bell is one of II. J.'s dehtors, we write on the Dr. side of A. B.'s Account: "Jan 1. To goods, £25"; and then on the Cr. side of the Sales Account write: "Jan 1. By total for the month, $£ 25, "$ thus completing the double entry.

From this we have the rule: "The accounts of all persons whose names appear in the Sales Book must be debited with the respective amounts and the Sales Account credited with the total."

## 305. 3. Posting from the Cash Book ${ }^{1}$ into the Ledger.

I. Taking the Dr. side first, item by item, we see that one entry of each has been made in the Cash Book and that one more has to be made, unless it has already been done.
(1) This was entered in the Cash Book from the Journal (§ 298), and at the same time the remaining Journal entries were posted to the Ledger, but, since the net capital was also credited to MI. J.'s Capital Account, the two items, "Cash in hand, $£ 10$," and "Bank, £700," were clearly included in that posting, for the $£ 802$ net capital $=£ 10+£ 700+£ 92$ (the difference between Assets 3, 4, 5 (£120), and Liabilities 6 (£28)). Hence the net capital entry, "Jan 1. By balance, £802," completes the double entry of Cash, $£ 10$, and Bank, $£ 700$, and also includes balance of Assets 3, 4, and 5 against Liability 6.

[^36](2) J. Hudson's Account: Cr. entry, "Jan. 4. By Cash, $£ 20, "$ completes the double entry.
(3) A. Bell's Account: Cr. entry, "Jan. 9. By Cash, £50," and also "Jan. 9. By Discount, £15," where the former completes the Cash look entry and the latter is completed, together with all other discounts on the Dr. side of the Cash Book, by entering the total discounts in the Discomit Account later (see (6) and (13) below).
(4) "Jan. 11. To Cash (paid into Bank), £75," has its corresponding double entry already made on the Cr. side of the Cash Book, "Jan. 11. By Bank, £i5" (Bank received Cash, . Cash column), so that we make no further Ledger entry.
(5) Sales Account, Cr. entry : "Jan. 27. By Bank, £150," thus completing the double entry.
(6) Open Discounts Account (N), Dr. untry: "Jan. 31. To Total discounts allowed, £15" (the corresponding C'r. entry will be found in A. Bell's Account).

## II. Taking the Cr. side, item by item :

(7) E. Brown's Account: "Jan. 2. To Bank, £27," Dr. entry, and also "Jan. 2. To Discount, £1." All disecount entries are completed by carrying the rotals to the Discounts Account.
(8) "Jan. 11. By Bank, $£ 75$," has been completed under "Jan. 11. To Cash, $\mathfrak{£} 75$," on Dr: side of Cash Book, and so need not appear any more in the Ledger (see (4) above).
(9) Open Sundry Expenses Account and make Debit entry : "Jan. 12. To Cash, £4."
(10) Henry James' Capital Account, Debit entry (for H. J. has withdrawn £100 of his capital): "Jan. 15. To Dank (Drawings), £100."
(11) E. Brown's Account, Debit entry: "Jan. 16. To Bank, £75."
(12) Salarics Account, Debit entry: "Jan. 28. To Bank, £10."
(13) Discounts Account, Credit entry: "Jan. 31. By Discounts received, £1."
(Note that this appeared as a Dr. entry in E. Brown's Account.)

## TRIAL BALANCE

306. We take the balances, leaving the totals to the student to check.
H. J.'s Capital Account, Cr'. balance, £702. Stock Account, Dr. balance, $£ 50$. A. Bell's Account, nil. J. Hudson's Account,

Dr. balance, £10. E. Brown's Account, Cr. balance, £75. Purchases Account, Dr. balance, £150. Sales Account, Cr. balance, £175. Sundry Expenses Account, Dr. balance, £4. Salaries Account, Dr. balance, £10. Discounts Account, Dr. balance, £14. Cash Book-Cash Account, Dr. balance, £l. Bank Account, Dr. balance, £713.

TRIAL BALANCE.

showing that the books are probably correct.
30\%. We may now balance the Personal Accounts and Nominal Accounts, and then make the

Closing Entrifs in tue Journal,
which embody all our Profits and Losses, and therefore deal with Nominal Accounts only, and prepare for the P. and L. Account.

1. Take the balances of the Nominal Accounts from the Trial Balance.
2. Transfer the balances througi, the Journal to the P. and L. Account.
3. And then make out the P. and L. Account.
4. Determine the net gain or loss to be transferred to Capital Account.
[^37]JOURNAL (CLOSING ENTRIES).

| Jan.$31$ | Profit and Loss Account, Dr. ${ }^{1}$ <br> To Stock at beginning <br> ,"Purchases <br> ", Salaries <br> ", Sundry Expenses <br> ," Discounts. | $\begin{aligned} & 18 \\ & 10 \\ & 16 \\ & 16 \\ & 16 \\ & 16 \end{aligned}$ | $\begin{array}{ccc}\text { ¢ } & \text { s. } & \text { d. } \\ 228 & 0 & 0\end{array}$ | $\begin{array}{rcc} \boldsymbol{£} & \boldsymbol{s .} & d . \\ 50 & 0 & 0 \\ 150 & 0 & 0 \\ 10 & 0 & 0 \\ 4 & 0 & 0 \\ 14 & 0 & 0 \end{array}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | SAles, Dr. . <br> Stock at the end of period To P. and L. Account, Cr | 16 15 18 | $\begin{array}{lll} 175 & 0 & 0 \\ 100 & 0 & 0 \end{array}$ | 27 |  |  |
|  | P. and L. Account, Dr. ${ }^{2}$. <br> To Capital Account | $\begin{aligned} & 18 \\ & 15 \end{aligned}$ | $47 \quad 0 \quad 0$ |  |  |  |

whence we see at once that the net profit is $£ 47$.
308. Let us now make out our P. and L. Account from the closing entries in the Journal :
18.


In the above account the "Stock at the end of the month, $£ 100$," has to be debited now to the Stock Account to show that on Feb. 1 we have $£ 100$ worth of goods in hand, while the net profit is carried to the Cr. side of the Capital Account, thus completing the double entry of the only two items in the Account for which it has not been completed.
309. Finally, we come to the Balance Sheet, which, as before, will include all the Assets and Liabilities of the firm and will not include the accounts dealt with under Profit and Loss - that

[^38]is to say, no Nominal Accounts are entered into the Balance Sheet.

Hence we have-
Capital Account, $£ 749$, as a Liability, for the business owes that amount to the capitalist, Henry James.
Cash, £1: Asset.
Bank, £713: Asset.
Stock on Hand, $£ 100$ : Asset.
A. Bell owes nothing to us, nor do we owe him anything.
J. Hudson owes us $£ 10$ : Asset.
E. Brown is one of our creditors to whom we owe £75: Liability.
The other accounts are nominal, but the student should be very careful to include Cash in hand and in Bank from the Cash Book.

BaLaNCE SHEET, Jandary 31, 19-.

(We hope that the student has taken our advice and has made a complete set of Ledger Accounts, which he can now compare with the following model.)
310. MODEL LEDGER (III).
15.


[^39]Sec. xix] DOUBLE ENTRY IN ACCOUNTS




16.


I When stock is stored in a warehouse, at the end of a period, we regard the Stock Account as a Real Account, but when the Stock Account relntes to goods at the beginning of a period of working, as here, we shall regard it as a Nominal Account, and hence ite balance goes to P. and I. Account.



| Dr. |  | SALARIES |  |  | ACCOUNT (N). |  |  |  | Cr. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 28. | To Bank . |  | 8 | $10 \left\lvert\, \begin{aligned} & s \\ & 0\end{aligned}\right.$ | $\begin{array}{ll}\text { s. } \\ 0 \\ 0 & \\ 0\end{array}$ | Jan. 31. | $\begin{gathered} \mathrm{By} \\ \mathrm{P} . \end{gathered}$ | Balance $\mathrm{c} / \mathrm{d}$ to and L. a/c . | 18 |  | £ 10 | 8. $\begin{aligned} & \text { d. } \\ & 0 \\ & 0\end{aligned}$ |


311. The order of procedure in Book-keeping is-

1. Opening entries made in Journal.
2. Entries made in Subsidiary Books.
3. Subsidiary Books closed at end of month.
4. Entries in Subsidiary Books posted to Ledger.
b. Trial Balance.
5. Closing entries made in Journal.
6. Nominal and Real Accounts balanced.
7. P. and L. Account prepared.
8. Capital and Personal Accounts balanced.
9. Balance Sheet prepared.
10. Conclusions drawn.
11. In posting such an item as "H. James returned to us goods valued at $£ 5$; we sent him a credit note," enter in our Returns Inwards Book as usual and then open Ledger Accounts for H. James and "Returns Inwards." Credit the former, "By

Returns, $£ 5$," and debit the latter, "To Total, £-"-that is, the total amount for the month. In a similar way treat " We returned goods to R. Tall, $£ 10, "$ only use the Returns Outwards Book.

## EXAMPLES. LXXIII. (c)

1. What purpose does the Journal serve?
2. Write a short essay on the use of the Subsidiary Books.
3. If John Bell owes us $£ 20$ at the close of the month, on which side of his account does the balance fall?
4. We have overdrawn our Bank Account by $£ 100$; how does the Cash Book show this?
5. There is a Dr. balance in our Discounts Account. What does it mean?
6. We have "Stock valued at $£ 100$ " on hand on June 1 . In what accounts will that appear in our June Ledger Accounts, and where shall we put the amount for July 1?
7. Give, in order, the data necessary for completing a set of accounts from the Subsidiary Book entries to the Balance Sheet.
8. What is the use of a P. and L. Account?

Journalise the following and find the net capital (Questions 9 to 11):
9. T. Williams has on Jan. 1, cash in hand, $£ 50$; goods valued $£ 100$; T. Jones owes him $£ 60$; and he owes R. Brown $£ 50$.
10. On Jan. 1, 19-, John Smith had cash in hand, $£ 510 \mathrm{~s}$. ; cash at Bank, $£ 6010 \mathrm{~s}$. ; goods on hand, $£ 125$; and William Alton owed him £7. He owed to Arthur Roberts $£ 27$ 10s.
11. H. Thomas has cash in hand, $£ 50$; in Bank, $£ 70$; $£ 100$ due from T. Nell ; and $£ 60$ due from R. Brown; stock valued $£ 500$; he owes T. Felling £70, and P. Roberts $£ 100$.
12. Post from Wm. Towney's Purchases Book, $\S 171$ (latter part), into the Ledger.
13. Post into the Ledger from Walter Ralegh's (a) Purchases and (b) Sales Books, § 173 and § 174.
14. Take Wm. Towney's Returns Outwards Book, open in his Ledger a Returns Outwards Account and an account for John Nelson, and post from § 177 into the Ledger.

Post into the Ledger Questions 15 to 17 :
15. The Cash Book entries in $\S 178$.
16. The Cash Book entries in $\S 180$.
17. The Cash Book entries in § 181.
18. Post into the proper Ledger Accounts: "Jan. 10. Paid for furniture and fittings by cheque $£ 200 . "$ "Jan. 12. Lent

Tom Brown £50." "Paid £100 in full settlement of H. Jago's account for $£ 150$."
19. Prepare a Trial Balance from the following Ledger balances: Cash, Dr., £40; John Smith, Dr., £10 15s.; capital, Cr., £41 8s. ; F. Clarkson, Dr., £4 4s. 6d. ; T. C. Jackson, Cr., $£ 10$ 10s. ; R. T. Nicholls, Dr., £5 6s. 6d.; R. S. James, Cr., $£ 68 \mathrm{~s}$. ; F. H. Somerset, Cr., £12; goods, Dr., £10; and explain what the effect on a Trial Balance is $(\alpha)$ if an entry for $£ 10$ is posted to the Dr. instead of to the Cr. side of an account, and (b) if an amount of $£ 1$ is posted in error as 1 s., but on the correct side.
20. The following is a statement of a trader's Credit Sales and Credit Purchases and Returns (Inward and Outwards). You are required to enter the transactions in the proper books of original entry and post to the Ledger Accounts: Fcb. 3, 191-, bought from F. Grace, 2 doz. pocket knives at 4 s .6 d . each ; Feb. 3, sold to J. Abel, 1 doz. photo frames at 1s. each ; Feb. 3, sold to J. Shrewsbury, 6 doz. dessert knives at 20s. per doz., less $5 \%$ trade discount ; Feb. 3, received from 3. Briggs, 1 case of carvers, 25 s ., returned damaged; Feb. 4, bought from G. Mead, 2 doz. silver photo frames at 5 s .6 d . each, less $10 \%$ trado discount; Feb. 4, returned to N. Hurst, 1 doz. pairs of scissors at 18 s . per doz., being the wrong size ; Feb. 5, sold to W. Humphreys, $\frac{1}{2}$ doz. razors at 3s. each, and charged him carriage on same, 6d. ; Fel. 5, sold to L. Townsend, 2 cases of fish knives and forks at $£ 2$ per case ; Feb. 5, returned to F. Grace, $\frac{1}{2}$ doz. pocket knives at 4s. 6 d . each, being of poor quality ; Feb. 6, bought from B. Lilley, 2 doz. glass match-stands, silver-mouuted, at 6s. each ; Feb. 6, J. Abel returned $\frac{1}{2}$ doz. photo frames at 1 s . each, not ordered ; Feb. 7, sold to J. Hearne, 3 doz. pocket knives at 30s. per doz., less $5 \%$ trade discount ; Feb. 7, sold to V. Gunn, $\frac{1}{2}$ loz. glass match-stands, silver mounted, at 8 s . 3d. each ; Feb. 8, bought from L. Spooner, 6 cases of fish knives and forks at $£ 3$ per case, less $10 \%$ trade discount.
21. Enter the following transactions into the Ledger: Feb. 1, 191-, Charles Dugmore began business with cash amounting to £120; Feb. 3, bought goods from R. Russell, $£ 75$ 6s. 8d. ; Feb. 5, bought goods for cash, £22 3s. 4d. ; Feb. 6, sold goods to F. Shepherd, £21 2s. 6d. ; Feb. 8, paid R. Russell on account, $£ 20$; Feb. 10, sold goods for cash, $£ 30$; Feb. 15, bought goods from C. Oliver, $£ 10$ 12s. 5d.; Feb. 25, received cash from F. Shepherd, $£ 20$, and allowed him discount, $£ 12$ s. 6 d .; Feb. 28, paid trade expenses, $£ 410 \mathrm{~s} .6 \mathrm{~d}$. Balance your Ledger and prepare a Trial Balance (both of totals and balances), also the P . and L. Account and Balance Sheet, valuing the final stock at £90.
22. Enter the following transactions in the Subsidiary Books
and then post to the Ledger Accounts: Feb. 1, 191-, John Thomas had a capital in cash of $£ 100$; Feb. 3, bought goods from R. Taylor, $£ 40$; Feb. 4, sold goods to F. Peters, £25; Feb. 8, sold goods to C. Griffin, $£ 10$; Feb. 9, paid R. Taylor on account, $£ 20$; Feb. 12, roceived cash from F. Peters, £25; Feb. 15, bought goods for cash, £16 8s. 6d.; Feb. 17, sold goods to C. Gritfin, £11 10s.; Feb. 20, sold goods for cash, £5 5s.; Feb. 27, sold goods to C. Griffin, £5 10s.; Feb. 28, reccived cash from C. Griffin, £20, and allowed him discount, £110s. Balance the accounts in your Ledger and prepare a Trial Balance.
23. Make out a P. and L. Account and Balance Sheet for the accounts of Question 22, valuing the stock at $£ 4010 \mathrm{~s}$. 6d.
24. On December 1, 191-, Richard Morton's books showed the following balances: Assets-Cash at llank, £85 17s. 6d.; stock of goods, $£ 12715 \mathrm{~s} .3 \mathrm{~d}$. ; owing by W. Watson, $£ 366 \mathrm{~s} .3 \mathrm{~d}$. Liabilities-Owing to C. Hobson, £31 6s. 3d. ; owing to F. Fletcher, $£ 1812 \mathrm{~s} .9 \mathrm{~d}$. ; capital, £200. Enter the above, and the transactions for the month, which follow, in the proper books, post to Ledger Accounts, and prepare a Trial lalance, as on December 31, 191-.
De... 2. Paid cheque to F. Fletcher $\begin{array}{cccccccc} & £ & s . & d . & f & s . & d \\ 18 & 3 & 0 & & & & \end{array}$ Discount . . . . $0 \quad 9 \quad 9$
4. Sold goods to W. Watson . 10110
7. Sold goods to D. Denison . 46118
11. Received cash from W. Watson (on account) . . 15000
, 12. Paid cash to Bank. . .
$10 \quad 0 \quad 0$
12. Paid sundry expenses in cash .
$310 \quad 0$
", 14. Bought goods of C. Hobson
23167
16. Sold goods to D. Denison . 6130
„, 18. Withdrew from Bank for office cash .

500
, 19. Received cheque from W.
Watson and paid same to Bank
$20 \quad 8 \quad 0$
,, 19. Allowed W. Watson discount.
0183
,, 24. R. Morton withdrew cash for private purposes.
$4 \quad 0 \quad 0$
,, 29. Bought goods of F. Fletcher
$3313 \quad 3$
30. Sold goods for cash
$710 \quad 0$
", 31. Paid in cash, sundry expenses.
$512 \quad 6$
Prepare a P. and L. Account for the above transactions, valuing the stock at $£ 15111 \mathrm{~s} .7 \mathrm{~d}$.
25. On June 1, 191-, the books of P. Walker showed the following balances: Assets-Goods on hand, £97 10s. ; cash in hand, £14; cash at Bank, £89; J. Smithson, £31 13s. 4d.; W. Clarkson, £18 10s. Liabilities-L. Thompson, £15 13s. 4d. ; P. Walker's Capital Account, £235. Record the above and the following transactions in the proper books, post to Ledger Accounts, take out a Trial Balance and P. and L. Account, and determine the net profit, if the residual stock be worth $£ 15211 \mathrm{~s} .9 \mathrm{~d}$.

191-. $\quad$ £ $\quad$ s. $\quad$ d. $\quad$ £ $s . \quad$.
June 2. Received cash from J. Smith-

| son. |
| :---: |
| And allowed |
| him discount |$\quad . \quad$| 31 | 0 | 0 |
| ---: | ---: | ---: |
| 0 | 13 | 4 |


| 4. Sold goods to W. Clarkson | 25 | 10 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 7. Paid into Bank . . . | 35 | 0 | 0 |

, 10. Bought goods from L. Thompson . . . . . $3710 \quad 0$
15. Paid rates by chegue . . 4150
19. Received cash from W. Clarkson and paid it into Bank. 17 15 0
Allowed hini discount . . 0150
22. Bought goods from L. Thompson
26. Paid L. Thompson by cheque $5010 \quad 0$

He allowing me discount . 2134
28. Sold goods for cash . . 710 0
30. Paid trade expenses for the month in cash .

1200
P. Walker drew cheque for private purposes

1500
26. On March 1, 191-, Charles Henry Smithson commenced business as a grocer with $£ 1000$ capital, of which $£ 950$ was paid into his Banking Account, and £50 retained as cash in hand for business purposes. His transactions for the month were as follows: March 1, 191-. Purchased goods at J. Robinson \& Son's auction mart, and paid cheque, $£ 7315 \mathrm{~s}$. ; also bought office furniture and fittings for which he paid cash, £38. March 9. Sold to Mrs. B. Vero, goods, $£ 75 \mathrm{~s}$. March 13. Purchased from Lipton's Ltd., tea, £28 10s. March 15. Purchased from J. G. Cooper, sugar, £13 5s. March 16. Paid Lipton's Ltd. a cheque
in full settlement of account, £27. March 18. Goods bought at J. Robinson's auction mart and paid cash, £10. March 19. Sold to Mrs. A. Harker, goods, £3 3s. March 25. Received from Mrs. B. Vero, cash, $£ 7$; and allowed her discount, 5s. March 29. Cash sales for month, $£ 152$; paid shop assistants' wages for month (cash), $£ 56 \mathrm{~s}$. ; paid rent for month (cheque), $£ 5$; paid trade expenses for month (cash), £9 10s. ; paid into l3ank, £102 5s. Enter the above items in the proper books, post to Ledger Accounts, and prepare a Trial Balance. From the foregoing, make out P. and L. Account and Balance Sheet, on March $31,191-$, taking the value of the stock on that date at $£ 6593 \mathrm{~s}$.
27. In Question 26 determine (1) what traders owe Smithson money ; (2) to whom he owes money and the amounts; (3) the capital for April; (4) the net profit; (5) his cash in hand and at Bank. Is "capital" an asset or a liability of a business?
28. Dec. 1, 191-. A cycle dealer begins business with a capital of $£ 120$, of which he pays $£ 100$ into the bank. Dec. 3 . He buys ten cycles from the Roman Cycle Co. at $£ 65 \mathrm{~s}$. each, and pays by cheque. Dec. 4. He sells two cycles at $£ 810$ s. each, and receives cash for the amount. Dec. 6. He buys three cycles on credit from Harrison \& Co. for £18. Dec. 10. He sells on credit two of the Roman cycles at $£ 87 \mathrm{~s} .6 \mathrm{~d}$. each, and one of the Harrison cycles at $£ 85 \mathrm{~s}$. to John Thomas; he pays various expenses in cash, $£ 55 \mathrm{~s}$. Make the necessary entries in the Ledger to record these transactions; prepare a P . and L . Account, Capital Account, and Balance Sheet, as on 10th December. Value the unsold cycles at cost price.
29. The following is the Manufacturing Account of the X.Y.Z. Co. Ltd., which has a capital of $£ 40000$ : Dec. 31, 191-. Cost of materials, £8165; wages (including superintendence), $£ 6284$; power, $£ 1000$; wear and tear of machinery, $£ 526$; establishment charges, $£ 742$; value of materials unused, $£ 1717$. By sales, 10000 machines at $£ 22 \mathrm{~s}$., $£ 21000$. You are required -(a) To find the profit; (b) the rate of profit per cent. on the cost price of each machine; (c) the rate of profit per cent. on the turnover ; (d) the rate of profit per cent. on the capital.
30. John Cunningham acquired a restaurant business on Jan. 1,191 -. He paid into the Bank $£ 600$. His transactions were as follows: Jan. 6. Takings during week, £94 11s. 2d. Jan. 8. Paid into Bank, £60. Jan. 13. Takings during week, $£ 9910 \mathrm{~s} .4 \mathrm{~d}$. Jan. 15, Paid into Bank, £40; received accounts as under-J. Brown $\&$ Co., meat, $£ 5916 \mathrm{~s} .2 \mathrm{~d}$; W. Thomas, fish, game, etc., £18 17 s . 3d.; R. Green, bread, etc., £7 9s. 4d.; H. Gowe Ltd., vegetables, etc., $£ 6$ 18s. 3d. ; R. Joker, minerale, etc., $£ 1617 \mathrm{~s} .4 \mathrm{~d}$. Jan. 20.

Takings during week, £100 15s. 8d. Jan. 24. Provisions, etc., paid for in cash during three weeks, $£ 14018 \mathrm{~s}$. 2 d . ; paid following accounts by cheque-J. Brown \& Co. (receiving discount, $£ 219 \mathrm{~s} .2 \mathrm{~d}$. ), $£ 5617 \mathrm{~s} . ;$ H. Gowe Ltd. (receiving discount, 8s. 3d.), $£ 610 \mathrm{~s} . ;$ W. Thomas (receiving discount, 18 s .3 d. ), £17 $19 \mathrm{~s} . ;$ R. (rreen (receiving discount, 9s. 4d.), £7. Jan. 27. Paid rent in cash, $£ 10$; wages and sut:dry expenses, threc weeks, $£ 1818 \mathrm{~s} .11 \mathrm{~d}$. On January 31 the value of the stock in hand was £50. Enter in proper books and post to Ledgers, debiting and crediting appropriate accounts, and prepare Trial Balance, P. and L. Account, and Balance Sheet.
31. John Howe, Albert Cole, and Andrew Barker were in partnership as wholesale fruiterers, etc., John Howe putting $£ 360$ in the business, Albert Cole $£ 240$, and Andrew Barker $£ 120$, which was paid into the Bank. Their transactions were: Aug. 2. Bought from Willingham \& Co. Ltd., fruit, $£ 12617 \mathrm{~s} .4 \mathrm{~d}$. Aug. 3. Bought from John Upwell, potatocs, £59 16s. Aug. 6. Sold and received cash for fruit, $£ 13214 \mathrm{~s}$.; sold and received cash for potatoes, $£ 654 \mathrm{~s}$. ; paid carriage in cash, £1 2 s .7 d . ; paid wages, ctc., in cash, £3 17s. 6d. Aug. 8. Paid Bank, £180; bought J. Allen \& Co., asparagus, £32 6s. 8d. Aug. 10. Paid J. Allen (receiving discount, £1 12s. 8d.), £30 14s. Aug. 11. Bought J. Coe, tomatoes, $£ 3816 \mathrm{~s}$. Aug. 12. Sold W. Almond, isparagus, $£ 226 \mathrm{~s}$.; sold W. Skimp, tomatoes, $£ 437 \mathrm{~s}$. ; sold J. Turner, asparagus, $£ 146 \mathrm{~s} .8 \mathrm{~d}$. Aug. 20. Paid carriage two weeks by cheque, $£ 119 \mathrm{~s}$. 7 d .; paid wages, etc., two weeks by cheque, $£ 715 \mathrm{~s}$. ; paid Willingham \& Co. Ltd., by cheque (discount, $£ 61 \mathrm{~s} .4 \mathrm{~d}$.), $£ 12016 \mathrm{~s}$. ; paid J. Upwell, by cheque (discount, £2), $£ 57 \mathrm{l6s}$. Aug. 27. Paid wages, etc., by cheque, £4 2s. 3d.; paid carriage by cheque, 16 s .8 d . Aug. 31. Paid rent and taxes for month by cheque, £5. Enter in proper books and post to Ledger, debiting and crediting appropriate accounts, and prepare Trial Balance. From the foregoing, make out P. and L. Account and Balance Sheet, dividing the profits or losses according to the capital invested.
32. John Miller commenced business, as a draper, on July 3, 191 -, with $£ 250$ at the Bank, $£ 3$ cash in hand, and stock $£ 300$. The stock had not yet been paid for, having been obtained on credit as follows: J. Beale \& Co., £110; F. Hall \& Sons, £60; Thomas Fisher, £90; and Hugh Jones Ltd., £40. J. Miller also possessed furniture, fixtures, and fittings valued at $£ 70$. Open John Miller's Ledger with these items, and post, through the Subsidiary Books, to it, his transactions during the first week of July (as follows): July 3, 191-. Paid cash for stamps, 5s., and
stationery, 6 s .8 d. ; purchased from J. Beale \& Co., 120 yards of flamelette at 4s. 3d. per dozen yards, on credit. July 4. Purchased from F. Hall \& Sons 600 yards of shirting ( 240 yards at 8 s . 3d. per dozen yards, and 360 yards at 10 s . 9 d . per dozen yards), on credit. July 5. Bought for cash, brown paper and string, 15 s . ; banked cash sales for July 3 and 4, £27 10s. July 6. Banked cash sales for July 5, £165s.; paid by cheque, J. Beale \& Co., £30 on account; paid by cheque, Hugh Jones' account (less $2 \frac{1}{2} \%$ discount). July 7. Paid by cash, carriage, 13s. 6d. July 8. Sold to Miss H. Hayman, on credit, 10 yards of sheeting at 1 s .5 d . per yard, 1 dozen reels of assorted cottons for $2 \mathrm{~s} .3 \mathrm{~d} ., 2$ pairs of lace curtains at 16 s . 11d. per pair ; received credit note from F. Hall \& Sons for 8 yards of shirting at 10s. 9 d . per dozen yards, which were damaged in transit and returned to Hall on the 8th inst. ; banked cash sales for July 6 and 7, $£ 3215 \mathrm{~s}$.; drew and cashed cheque for $£ 10$, and paid wages, $£ 75$ s. Balance the Ledger Accounts, taking the value of the strock at £261 8s. 7d., extract a "Trial Balance" as on July 8, 191-, and prepare P. and L. Account and Balance Sheet.
33. The following was the lalance Sheet of Henry Coulthard, a waste rubber merchant, as on December 31, 191-:-

| Dr. | BALANCE SHEET. |  | $C r$. |
| :---: | :---: | :---: | :---: |
| To Henry Coulthard'sCapital Account. | $\begin{array}{ccc} \mathfrak{£} & \text { s. } & d . \\ 361 & 0 & 0 \end{array}$ | By machinery, fixtures, and fittings . | $\begin{array}{ccc} £ & s & d . \\ 120 & 0 & 0 \end{array}$ |
| ,, Sundry Creditors:- |  | , Debtors:- |  |
| F. Nelson . 19600 |  | A. Coats . £72 00 |  |
| G. Harrod. 4800 |  | S. Wileor 2400 |  |
| T. Arnold . 2400 |  | B. Vickers 800 |  |
| , Bank overdraft . | 168 6 000 | ,, Stock in hand . <br> ", Cash in hand | 104 236 000 |
|  | £535 00 |  | £535 00 |

You are required to open the accounts in Henry Coulthard's Ledger which are necessary to record the above; and to post thereto, through the proper books of original entry, the following transactions: Jan. 1, 191-. Purchased, on credit, from T. Arnold, $\frac{1}{2}$ ton of motor inner tubes at $£ 26$ per ton; received cheque (which was paid into the Bank) from $\Lambda$. Coats for $£ 70$, and allowed him the balance of his account as discount ; sold, for cash, 5 cwt . of ground rubber at $£ 117 \mathrm{~s} .4 \mathrm{~d}$. per cwt. Jan. 2. Sold, on credit, to B. Vickers, 1 ton of cab tyres at 40s. per cwt. ;
sold, for cash, $\frac{1}{2}$ ton of ground rubber at $£ 232 \mathrm{~s}$. per ton. Jan. 3. Paid T. Arnold, by cheque, the amount of his account as on December 31, 191-, less $10 \%$ discount; sold, on credit, to S. Wilcox, 2 tons of bus tyres at $£ 42$ per ton, and received cheque from him for the amount of his account as on December 31, 191-, less $5 \%$ discount; drew cheque for $£ 5$ for private purposes. Jan. 4. B. Vickers returned, as unsuitable, $\frac{1}{2}$ cwt. of the rubber invoiced to him on the 2nd inst. ; sent him a credit note for same ; sold, for cash, 6 cwt . of inner tubes at 38 s .6 d . per cwt. Jan. 5. Paid in cash, wages, £10 16s. 4d. (including insurance stamps) ; paid G. Harrod cheque for $£ 18$ on account ; purchased, on credit, from F. Nelson, 2 tons of cab tyres at $£ 4110 \mathrm{~s}$. per ton, including charge for bags ; paid cash for sundry trade expenses, £9 12s. 4d. Jan. 6. Purchased a weighing-machine for $£ 12$ from H. Jackson, and paid him by cheque ; returned to F. Nelson 40 empty bags, and received credit note from him for 6 s .8 d . ; paid into Bank from cash, £21 9s. Balance the accounts, bring down the balances, take out a Trial Balance as on January 6, 191-, and prepare P. and L. Account and Balance Sheet, valuing the stock at $£ 38111 \mathrm{~s}$. 6 d .

## SECTION XX

## INTEREST

## A. Simple Interest

313. A friend of mine tells me that he has been offered a $£ 300$ house for $£ 200$, and that it is a very good bargain, but he finds himself unable to spare more than $£ 100$, and asks me to lend him the other $£ 100$, promising to pay me $4 \%$ per annum for the loan. I lend him the $£ 100$, and he pays me $£ 4$ for the privilege of using my money for one year.

The $£ 4$ is called the Interest on the loan.
314. Again, if you were a dealer in fruit and had an unexpected offer of a cargo for a very low figure, you would borrow $£ 300$ to effect the purchase, and pay, say, 3 s . or 5 s . for the loan for a week or ten days.

Now the point to notice is this, that by obtaining a loan of £300 you are able-(1) To purchase the fruit cheaply; (2) to sell it, perhaps, for $£ 340$; while the total extra cost to you has been but a few shillings by way of interest, but there would be behind you, as well, an honourable commercial standing of yous own building up.

The cases we have illustrated are such as occur day after day, and even every hour of the day, in the great commercial centres of the world.
315. It would be a simple matter for a well-known City merchant to borrow money, and the student should understand that the loan would be negotiated through a broker or a banker and not obtained from a " moneylender." In many cases, however, security for the loan would be given, and it might take the form of (1) a promissory note (Plate XIV., p. 470), (2) a bill of exchange (Plate XIII., p. 488), (3) a mortgage deed on real property, (4) a life policy or a bill of lading, etc. (See Plate in Part III.)
316. The sum of money borrowed or lent is called the Principal, and Principal + Interest $=$ Amount .

The word Amount is used somewhat ambiguously, and the student should take care to note the senses in which it is used. We might say, for example: "A sum of money which amounts to $£ 100$ is invested at $4 \%$ for 5 years. To what will it amount?" The word is used in the first case in its ordinary colloquial sense, but in the second case it means

Principal + Interest.
$£ 100$ invested for one year at $4 \%$ per annum earns $£ 4$ interest; $\therefore$ the amount of $£ 100$ in one year at $4 \%$ per annum is $£ 104$.

It is also very necessary to notice the time for which a rate is quoted, for $5 \%$ per month is a very different rate from $5 \%$ per annum.
317. In the method of borrowing and of paying interest which we have described, you will see that we borrow $£ 300$, pay the interest due, and then return the principal at the end of the period for which we have borrowed it. Such a method of obtaining money is known as borrowing (or lending) at Simple Interest ; another method, described on page 454, is known as borrowing at Compound Interest.

We shall always reckon interest to the nearest penny.
318. Simple Interest is most often used in transactions involving a number of days less than one year. Bankers, for instance, allow Simple Interest on deposits and "throw out" the interest every six months or twelve months, but if a client leaves that interest in the Bank for two or three years, as he may do, then the total amount due to him is the Simple Interest on the deposits for two or three years. In the same way, if a merchant invests $£ 100$ with the Corporation of a town and receives the interest half-yearly, if he wishes to know the total amount so received in ten years, he must employ Simple Interest to find it
out. We therefore include some questions involving a period of time greater than one year.
319. The following examples illustrate the application of Simple Interest:

Example 1.-What interest must be paid for a loan of $£ 200$ for 7 days at $5 \%$ per annum (p.a.)?

Interest on $£ 100$ for 365 days at $5 \%$ p.a. $=£ 5$

$$
\begin{aligned}
& " \quad, £ 200, \quad " \quad=\frac{£^{200 \times 5}}{100} \\
& \therefore \quad " \quad, \quad, \quad 7 \quad, \quad, \quad=\frac{200 \times 5}{100} \times \frac{7}{365} \\
& =3 \mathrm{~s} .10 \mathrm{~d} \text {. }
\end{aligned}
$$

Hence, Interest (S.I.) $=$ Principal ( P ) $\times$ rate per cent. ( R ) $\times$ time $(\mathrm{T}) \div 100$, or, S. $\mathrm{I} .=\stackrel{\mathrm{P}}{100} \mathrm{O} \times \mathrm{R} \times \mathrm{T}$.

Example 2.-Find the Simple Interest on $£ 348$ 15s. 8d. for 2 years at $2 \frac{1}{2} \%$ p.a.

$$
\begin{aligned}
\text { Here we have S.I. } & =£^{\frac{348.7833}{100}} \times 2.5 \times 2 \\
& =£ 3.487833 \times 2.5 \times 2 \\
& =£ 178 \mathrm{~s} .9 \mathrm{~d} .
\end{aligned}
$$

Example 3.-To what will $£ 138517 \mathrm{~s}$. 4 d . amount if lent from 1st January to 15 th June at $4 \%$ p.a. Simple Interest?

Note that $£ 138517 \mathrm{~s} .4 \mathrm{~d}$. is the principal, not the amount.

$$
\begin{aligned}
\text { S.I. } & =£^{1385 \cdot 8666} 100 \\
& =£ 25 \frac{165}{365} \\
\therefore \text { amount } & =£ 1385.17 \mathrm{~s} . \\
& =£ 141017 \mathrm{~s} .5 \mathrm{~d} .+£ 250 \mathrm{~d} .
\end{aligned}
$$

320. Example 1.-In what time will the interest on $£ 325$ 15s. 6d. amount to $£ 818 \mathrm{~s} .10 \frac{1}{2}$ d. at $5 \frac{1}{2} \%$ p.a. ?

Decimalising, we have $£ 16 \times 28875$ is the interest on $£ 325 \cdot 775$ at $5 \%$ p.a. for 1 year


Example 2.-At what rate per cent. per annum will $£ 760$ 10s. amount to $£ 897 \mathbf{7 s}$. 10d. if invested for 3 years?

$$
\begin{aligned}
\text { Interest } & =£ 8977 \mathrm{~s} .10 \mathrm{~d} .-£ 76010 \mathrm{~s} . \\
& =£ 13617 \mathrm{~s} .10 \mathrm{~d} . \\
& =£ 13689 .
\end{aligned}
$$

$£ 22.815$ is interest on $£ 760.5$ for 3 years at $1 \%$ p.a.

| £1 | " | " | " | $\frac{1}{22 \cdot 815} \% \text { р.а. }$ |
| :---: | :---: | :---: | :---: | :---: |
| $\therefore £ 136 \cdot 89$ | " | " | " | 13689 |
|  |  |  |  | $\overline{22.815}$ " |
|  |  |  |  | $=6 \%$ p.a. |

321. In each of the examples we have given above the working has been more or less protracted. Simple Interest tables allow of much shorter working. Let us find the interest on $£ 1$ for 1 day at $1 \%$ p.a.

$$
\begin{aligned}
\text { Interest } & =£_{1}^{100} \times 1 \times \frac{1}{365} \\
& =\frac{0.01}{365} \\
& =£ 000002739726 .
\end{aligned}
$$

We now compile a very easy table:
TABLE OF SIMPLE INTERESTON ON A'T $1 \%$ FOR 1 TO 9 DAYS.


The student will now see that having once gone to the trouble of making this table the Simple Interest on any amount for any time at any rate can be found readily and simply. Hence the value of Simple Interest tables.

Example 1.-Find, from the table, the interest on $£ 1000$ for 30 days at $5 \%$ p.a.

We work at length :
Interest on $£ 1$ for one day at $1 \%=£ 0 \cdot 00002739726$

$$
\begin{aligned}
& £ 1000 \\
& £ 1000 \text { for } 30 \text { days at } " \%=£ 0 \cdot 02739726 \\
& " \#=£ 0 \cdot 8219178 \\
& 5 \%=£ 4 \cdot 109589 \\
&=£ 4 \cdot 1096 \\
&=£ 42 \mathrm{~s} .2 \mathrm{~d} .
\end{aligned}
$$

Example 2.-What is the interest on $£ 240$ 12s. 6 d . for 96 days at $3 \frac{1}{2} \%$ p.a.?

$$
\begin{array}{rccccc}
\text { Principal }=£ 240625 \\
\text { Interest on } & £ 1 & \text { at } & 1 & \% & \text { for } 90 \\
\text { days } & =£ 0 \cdot 0024657534 \\
" & " & " & " & 6 & "
\end{array}=£ 0.00016438356
$$

$\therefore$ Interest on $£ 240.625=£ 240.625 \times 0.00920547936$, which, by contracted multiplication $=£ 24 \mathrm{~s} .4 \mathrm{~d}$., to the nearest penny.
322. Example 1.-The Post Office Savings Bank pays $2 \frac{1}{2} \%$ p.a. on every complete $£ 1$ standing to the credit of the depositor for one complete calendar month-that is, $\frac{1}{2} d$. per $\boldsymbol{£}_{1}$ per month. Find the interest due on the following, up to December 31. December 31, Amount in Bank, £25; January 10, Withdrawal, £5; February 27, Deposit, £10; June 18, Deposit, £15; August 20, Withdrawal, £10; November 30, Deposit, £15.

The amounts standing to the depositor's credit and the interest due are:

| January | £25-£5=£20; | Interest, |
| :---: | :---: | :---: |
| February | £20 | 10d. |
| March, April, May, June | £30 | 60d. |
| July | £45 | 22 d . |
| August, September, \} October, November , | £35 | 70d. |
| December | £50 | 25d. |
| Total int | 7d., or 16s. bd. |  |

Example 2.-A Bank pays interest at $2 \frac{1}{2} \%$ p.a. on minimum monthly balances. Calculate the interest due on 1st July from the following : March 31, Cash in Bank, £300; April 10, Deposit, £50; April 18, Withdrawal, £30; May 2, Deposit, £100; May 31, Deposit, £40; June 15, Withdrawal, £600.

Minimum amount in the Bank during April was $£ 300$; during May, £320; during June, £180;
$\therefore$ interest is due on $£ 300+£ 320+£ 180$ at $2 \frac{1}{2} \%$ for 1 month, and amounts to $£ 8.00 \times 2.5 \times \frac{1}{12}=£ 113 \mathrm{~s} .4 \mathrm{~d}$.

Example 3.-A merchant owes $£ 1000$ on 1st November for goods received, pays $£ 500$ on that date, and also $£ 200$ on 10th November, $£ 100$ on 6th December, and the balance on 30th December. If he has to pay $5 \%$ p.a. on the amount overdue, find the interest charged.
$£ 200$ is 9 days overdue, or $£ 1800$ is 1 day overdue

$$
£ 100 \text { is } 35
$$

$£ 200$ is 59 ", " $£ 11800$ is 1 ", ",
$\therefore$ the interest due is equal to the interest on $£ 17100$ for 1 day at $5 \%$ p.u.

Interest on $£ 1$ for 1 day at $5 \%=£ 0.0001369863$;
$\therefore \quad$, $£ 17100 \quad " \quad=£ 26 \mathrm{~s} .10 \mathrm{~d}$.

## EXAMPLES. LXXIV.

Find, to the nearest penny, the Simple Interest as required (in Questions 1 to 12 using the method of Example 2, §319):

1. $£ 100$ for 6 days at $5 \%$ p.a.
2. $£ 150$ for 15 days at $5 \%$ p.a.
3. $£ 180$ for 50 days at $4 \%$ p.a.
4. £230 for 25 days at $3 \%$ p.a.
5. $£ 355$ for 4 months at $2 \frac{1}{2} \%$ p.a.
6. $£ 658$ for 8 months at $4 \frac{1}{2} \%$ p.a.
7. £856 16s. for 2 years at $4 \%$ p.a.
8. £834 15s. 6d. for 3 years at $4 \frac{1}{2} \%$ p.a.
9. $£ 517 \mathrm{l} 4 \mathrm{~s}$. for 95 days at $4 \frac{1}{4} \%$ p.a.
10. $£ 13914 \mathrm{~s} .6 \mathrm{~d}$. for 228 days at $3 \frac{3}{4} \%$ p.a.
11. £575 16s. for 135 days at $2 \frac{3}{4} \% \mathrm{p}$.a.
12. $£ 516$ for 60 days at $4 \frac{1}{4} \%$ p.a.

In Questions 13 to 22 use the table, § 321 :
13. $£ 100$ for 6 days at $2 \%$ p.a.
14. $£ 100$ for 50 days at $2 \%$ p.a.
15. £200 for 8 days at $3 \%$ p.a.
16. $£ 250$ for 25 days at $5 \%$ p.a.
17. $£ 350$ for 12 days at $4 \%$ p.a.
18. $£ 400$ for 35 days at $\frac{1}{2} \%$ p.a.
19. $£ 460$ for 146 days at $1 \frac{1}{2} \%$ p.a.
20. $£ 520$ for 154 days at $1 \frac{4}{5} \%$ p.a.
21. $£ 63015 \mathrm{~s}$. for 270 days at $2 \frac{1}{8} \%$ p.a.
22. $£ 125016 \mathrm{~s}, 8 \mathrm{~d}$. for 300 days at $3 \frac{1}{5} \%$ p.я,
23. Confirm the results of Questions 1 to 12 by using the Simple Interest table (§321) and of Questions 13 to 22 by the method of Example 2, § 319.
24. To what does the principal in Questions 10 to 12 and 20 to 22 amount?
25. If 500 guineas be invested at $4 \frac{1}{2} \%$ p.a. Simple Interest, to what will the interest amount if allowed to remain for $3 \frac{1}{2}$ years?
26. Upon what amount is $£ 115 \mathrm{~s}$. the Simple Interest for 10 months at $3 \frac{3}{4} \%$ p.a.?
27. A clerk insures his life and may pay a premium of $£ 1010$ s. p.a., or he may add $2 \frac{1}{2} \%$ to this amount and pay half of it every 6 months, or he may add $5 \%$ and pay one-quarter quarterly. What interest would he pay every 6 months and every quarter?

In what time will the following take place (Questions 28 to 33) :
28. $£ 517 \mathrm{14s}$. amount to $£ 5238$ s. 6 d. at $44 \%$ p.a.?
29. $£ 85616 \mathrm{~s}$. produce $£ 6810 \mathrm{~s}$. 11d. interest at $4 \%$ p.a.?
30. £575 16s. produce £5 17 s .2 d . interest at $2 \frac{3}{4} \%$ p.a.?
31. $£ 13914 \mathrm{~s} .6 \mathrm{~d}$. amount to $£ 143$ at $3 \frac{3}{4} \%$ p.a.?
32. $£ 63015 \mathrm{~s}$. amount to $£ 64013 \mathrm{~s} .4 \mathrm{~d}$. at $2 \frac{1}{8} \%$ p.a.?
33. £1250 16s. 8d. produce $£ 1019 \mathrm{~s} .4 \mathrm{~d}$. at $3 \frac{1}{\mathrm{~B}} \%$ p.a.?

What rate per cent. p.a. must be charged (Questions 34 to 39) so that-
34. £2 2s. may be interest on $£ 1536$ s. for 100 days?
35. $£ 7613 \mathrm{~s}$. may amount to $£ 807 \mathrm{~s}$. in 200 days?
36. The interest on $£ 53616 \mathrm{~s}$. for 6 months may be £20 2 s .7 d .?
37. The amount of $£ 27510$ s. may be $£ 285$ 0s. 10 d . in 4 months?
38. $£ 25016 \mathrm{~s}$. may amount to $£ 258$ 6s. 6 d . in 9 months ?
39. £2 16 s .8 d . may be the interest on $£ 22919 \mathrm{~s}$. for 90 days?
40. An insurance company receives $£ 205600$ in premium income up to 30 th June in one year. If that amount be invested at $3 \frac{1}{2} \%$ for the rest of the year, what profit will the company have made?
41. Given that the interest on $£ 100$ for 1 day at $4 \%$ is $£ 0.0109589$, make a table showing the interest at that rate for $1,2,3$, up to 9 days. Use the table to find the interest on $£ 200$ for 271 days, to the nearest penny.
42. A merchant agrees to pay a bill for $£ 119$ 10s. 9 d , on 10 th

January, but is unable to do so until 10th April. If interest is reckoned at $4 \frac{1}{4} \%$ p.a., calculate the amount due on 10 th April.
43. If we lend $£ 1238$ to the Corporation of $\mathrm{Lip}_{\mathrm{p}}$ worth on the security of the rates, and interest is payable half-yearly on 31st March and 30th September at the rate of $3 \underset{4}{4} \%$ p.a., calculate the amount due each half-year.
44. In 1910-12 the Japanese Government raised an internal loan ${ }^{1}$ of yen $276,220,000$ at $4 \%$. Of this amount yen $45,434,000$ has been redeemed. How much interest per annum has still to be paid? (Answer in pounds.)
45. A grocer finds he has $£ 1500$ which he can lend, so he puts $£ 350$ out at $3 \frac{1}{2} \%$ p.a. for 6 months, $£ 400$ at $5 \frac{1}{4} \%$ p.a. for 4 months, and the remainder at $4 \frac{1}{2} \%$ p.a. for 8 months. What amount does he receive in interest?
46. What income-tax would the grocer of the last question pay on the interest received at 1 s . 3d. in the pound, and what did he pay on the original $£ 1500$ of earned income at 10 d. in the pound?
47. A banker lends $£ 550$ from 12th June 1915 to 18th January $1916^{2}$ at $5 \%$ p.a. What interest does he receive?
48. What interest should be paid for a loan of $£ 1000$ from 25th November 1915 to 21st March 1916 at $4 \%$ p.a. ?
49. For how much can I borrow 50000 dollars at $4 \frac{1}{2} \%$ p.a. from 25th December 1915 to 25th March 1916 ?

Questions 50 to 54 relate to the Post Office Savings Bank. ${ }^{3}$ (See Example 1, § 322.)
50. I deposit $£ 30$ on 31 st December, and draw out the whole on lst March ; what interest have I earned?
51. What interest is due on $£ 36$ deposited 15 th January and drawn out 15th March?
52. If $£ 48$ is deposited on 25th February and the whole withdrawn on 8 th December, what is the amount so withdrawn, including interest?
53. What interest should the Savings Bank pay on the following account: £26 deposited 28th February ; £12 deposited

[^40]18th March ; £5 withdrawn 20th April, if the interest is paid up to and including 31st December of the current year?
54. Make up the interest on the following Bank Book statement:

Deposits.
January 20, £15.
February 8, £16. ${ }^{1}$
April 15, £8.
June 21, £16.
August 30, £3.
September 20, $£ 1$.
December 30, £3.

Withdrawals.

March 5, £18.
May 10, £15.
July 5, £10.
55. If the capital of a marine insurance company be yen $10,300,000$, and interest is paid at $44 \%$ p.a. to the 5860 shareholders, what is the average amount each one receives per annum?
56. A Bank has $55,356,500$ francs out on loan, and the average rate of interest earned is $4 \frac{1}{4} \%$ p.a.; what is the income of the Bank every quinquennium?
57. A company places $£ 58654$ 12s. 6d. on deposit at Bank as the result of one year's working. If interest is paid at the rate of $5 \frac{1}{2} \%$ p.a., what is the total amount the company will have to its credit in 9 months?
58. It is proposed to construct some drainage works in Spain at a cost of $1,060,630$ pesetas. Calculate the interest upou this amount for 3 years at $4 \frac{1}{2} \%$, and express the result in English money.
59. A merchant dies worth $£ 750350$ personalty on 20 th January 1914, and the estate duty is at the rate of $14 \%$, but his executors do not pay the duty till 30th June and are charged $3 \%$ p.a. interest by the Government. What is the total amount paid into the coffers of the State?

60 . What should I receive quarterly upon $£ 1000 \mathrm{ls}$. 6 d . invested at $10 \%$ p.a.?
61. Calculate the Simple Interest on 10560 francs invested at $3 \%$ p.a. if it accumulates for 5 years.
62. An American banker has had 25580 dollars out at $3 \frac{1}{2} \%$ p.a. for $4 \frac{1}{4}$ years. What amount can he then draw out without touching his original deposit?
63. Calculate the interest I have to pay on a loan of a quarter of a million pesetas for 9 months at $5 \frac{1}{2} \%$ p.a.

[^41]64. A clerk borrows $£ 500$ from a money-lender for $2 \frac{1}{2}$ years at $3 \%$ per month. He takes the arrangement to be $3 \%$ per annum. How much does he pay for his inexperience?
65. Jonah Macpherson's bankers pay $3 \%$ on the minimum monthly balance. How much interest should Mr. Macpherson receive at the close of the year (31st Dec.) if his account is as follows:

December 31, £1000.

Deposits.
January 8, £500.
March 10, £600.
April 18, £350.
September 21, £1000.
November $5, £ 800$.

Withdrawals.
February 18, £50.
May 20, £400.
66. Calculate the interest due on the following when the books are made up at the close of the year:

Deposit, 200000 dollars.

which continues to the end of the year.
67. $£ 1000$ is deposited by a merchant on 31st December when the rate of interest is $2 \frac{1}{2} \%$ p.a. ; on lst June the rate becomes $3 \%$ p.a.; what amount stands to his credit at the close of the year?
68. A clerk agrees to purchase premises valued at $£ 800$ on the understanding that he pays $20 \%$ in cash and the remainder in ten equal instalments at intervals of 6 months, together with interest at the rate of $5 \%$ p.a. on the amount outstanding at the beginning of each 6 months. Find the total amount that he pays, and the time it takes him to clear his debt.
(Note.-He pays 6 months' interest on all but $20 \%$ at the time when he pays that $20 \%$, and in 6 months' time $5 \%$ on all but $20 \%$ and the first instalment.)
69. At what rate per cent. per annum would the clerk of the previous question have had to borrow enough money to pay the $£ 800$ in cash so that it might be as cheap as paying by instalments?

## B. Compound Interest

323. Compound Interest, the second means by which money may be borrowed or lent, will probably be made clear by the following illustrations:

We have worked our business all the year and have made $£ 1000$ profit. We deposit this sum at the Bank and are paid $4 \%$ p.a. upon it. At the end of the year the amount standing to our credit at $4 \%$ will be $£ 1000$ (Principal) $+£ 40$ (Interest) $=£ 1040$.

Let us suppose ${ }^{1}$ that we have no occasion to draw this out, and that we leave it in the Bank and receive interest not only on the $£ 1000$ but also on the $£ 40$-then will the $£ 1000$ give us another $£ 40$ interest, and the $£ 40$ interest for the first year produces, as you will have learnt, £1 12s.; so that we have:


Making a total of $£ 1081$ 12s. at the end of the second year.
Money lent in this way is said to be lent at Compound Interest.
324. Another way in which Compound Interest enters into commercial enterprises is in connection with life insurance calculations, where a bonus is paid on the value of the policy at the end of either three or five years, and then at the end of the next period the bonus is paid both on the value of the policy and on the previous bonus, so that we may say that the policy is earning money at Compound Interest.

So also an insurance company, in calculating the amount to be charged in premiums, allows for the fact that the amount paid in any year can be invested at Compound Interest for twenty or thirty years, and so the "Premium Income" earns money (§ 249-§ 256). See also Part III.
325. Again, suppose that $£ 5000$ has been collected to build a memorial hall, and it is undesirable to make any further public

[^42]appeal although another $£ 300$ is required. All that it is necessary to do is to deposit the $£ 5000$ in a bank at $4 \%$ p.a., and at the end of a year it will be worth $£ 5200$, while if it be left a little longer it will, at Compound Interest, give the sum required automatically.
326. Example 1.-What is the Compound Interest on $£ 200$ invested for 3 years at $5 \%$ p.a.?

In Compound Interest sums we shall decimalise the shillings and pence, and reconvert to money at the end of the sum.
$£ 200$ = Principal for first year.
$10=$ Interest for first year, i.e. $£_{\frac{200}{100} \times 5 .}$
$\therefore £ 210=$ Principal for second year.
$10 \cdot 5=$ Interest for second year, i.e. $£ 2 \cdot 10 \times 5$.
$£ 220 \cdot 5=$ Principal for third year.
$11 \cdot 025=$ Interest for third year, i.e. $£ 2 \cdot 205 \times 5$.
$£ 231 \cdot 525=$ Principal for fourth year.
$\therefore$ in three years $£ 200$ amounts to $£ 231 \cdot 525$.

$$
\begin{aligned}
\therefore \text { interest required } & =£ 231 \cdot 525-£ 200 \\
& =£ 3110 \mathrm{~s} .6 \mathrm{~d} .
\end{aligned}
$$

Simple Interest for same period $=£ 30$.
Example 2.-Find the Compound Interest on $£ 754$ 15s. 8d. invested for $2 \frac{1}{2}$ years at $5 \%$ p.a.
$£ 754 \cdot 7833=$ Principal for first year.
$37 \cdot 7392=$ Interest for first year.
$£ 792 \cdot 5225=$ Principal for second year.
$39 \cdot 6261=$ Interest for second year.
$£ 832 \cdot 1486=$ Principal for third year.
$20.8037=$ Interest for half-year, i.e. $\frac{8.321486}{2} \times 5$.
£852.9523
Compound Interest $=£ 852 \cdot 9523-£ 754.7833$
$=£ 98 \cdot 1690$
$=£ 983 \mathrm{~s} .5 \mathrm{~d}$. , to the nearest penny.
Example 3.-If $£ 386$ 12s. 6 d . be invested at $6 \%$ p.a. for

2 years, calculate the sum to which the principal will amount at Compound Interest payable half-yearly.
$6 \%$ p.a. $=3 \%$ per half-year.
$£ 386 \cdot 625=$ Principal for first half-year.
$11.5988=$ Interest for first half-year.
$£ 398 \cdot 2238=$ Principal for second half-year.
$11.9467=$ Interest for second half-year.
$£ 410 \cdot 1705=$ Principal for third half-year.
$12 \cdot 3051=$ Interest for third half-year.
$£ 422 \cdot 4756=$ Principal for fourth half-year.
$12.6743=$ Interest for fourth half-year.
$£ 435 \cdot 1499=$ Principal for fifth half-year, i.e. principal at beginning of third year.
$\therefore$ the amount required is $£ 435 \cdot 1499$
$=£ 4353 \mathrm{~s}$., to the nearest penny.
327. It is possible to find the Compound Interest on any sum of money by reference to Compound Interest Talles and by the application of logarithms. These methods are described in Part III.

## EXAMPLES. LXXV.

(To be regardod as Compound Interest sums except where otherwise stated.)

1. What is the Compound Interest on $£ 150$ for 2 years at $3 \%$ p.a.?
2. Find the Compound Interest on $£ 175$ for 3 years at $2 \%$ p.a.
3. To what sum does the Compound Interest on $£ 240$ for 2 years at $4 \%$ p.a. amount?
4. Find the Compound Interest on $£ 350$ for 3 years at $4 \%$ p.a.
5. What is the Compound Interest on $£ 550$ for 4 years at $2 \%$ p.a.?
6. Find the Compound Interest on $£ 460$ for 2 years at $2 \frac{1}{2} \%$ p.a.
7. If a banker invested $£ 750$ at $3 \%$ p.a. for 4 years, how much interest would he receive at Compound Interest?
8. How much more did the banker of the last question receive than if he had invested at Simple Interest?
9. What is the Compound Interest on $£ 350$ 10s. invested for 2 years at $3 \%$ p.a. ?
10. How much interest would a stockbroker receive on in. vesting $£ 430 \mathrm{l} 5 \mathrm{~s}$. for 3 years at $4 \%$ p.a.?
11. What interest would be derived from $£ 36412 \mathrm{~s} .9 \mathrm{~d}$. invested at $2 \frac{1}{2} \%$ p.a. for 2 years?
12. To what does $£ 3505 \mathrm{~s}$. 8d. amount if invested for $2 \frac{1}{2}$ years at $3 \frac{1}{2} \%$ p.a.?
13. What is the Compound Interest on 50000 francs invested for $2 \frac{1}{2}$ years at $3 \frac{1}{4} \%$ p.a.?
14. Calculate the Compound Interest on $£ 73810 \mathrm{~s} .9$ d. for $3 \frac{1}{4}$ years at $2 \%$ p.a., and find by how much it exceeds the Simple Interest.
15. What shall I receive in interest at the end of 4 years from 50560 dollars invested at $3 \frac{1}{2} \%$ p.a.?
16. Find the Compound Interest which an Italian merchant who invests 50000 lire fur $2 \frac{1}{2}$ years at $3 \frac{1}{4} \%$ p.a. will receive at the end of the period named.
17. Find the Compound Interest on $£ 37518$ s. 9 d. invested for 2 years at $4 \%$ p.a., payable half-yearly. By how much does the Compound Interest excced the Simple Interest?
18. Determine the amount due at the end of 18 months on $£ 156$ 12s. placed out at Compound Interest at $4 \%$ p.a., payable quarterly.
19. What will be the amount of $£ 27413 \mathrm{~s} .6 \mathrm{~d}$. ; at $3 \%$ p.a., payable half-ycarly, in $2 \frac{1}{2}$ years?
20. Find the difference between the Compound Interest on $£ 35515$ s. 3 d., invested for 2 years at $12 \%$ p.a., payable quarterly, and the same rate payable annually.
21. If a grocer, who had $£ 5000$ capital in his business, made a profit of $5 \frac{1}{2} \%$ on his capital in a year's working, and he invested one-fifth of that profit for 3 years at $3 \%$ p.a. Compound Interest, to what would the money invested amount?
22. A dealer in antiques has a picture worth $£ 1000$, and he reckons that its value increases $20 \%$ every 3 years. Calculate its value at the end of 12 years.
23. If the dealer of the last question had sold the picture at the end of 9 years, what profit would he have made if his cost price were $£ 750$ ?
24. A fish buyer of Newfoundland invests 10000 dollars in Montreal at $4 \%$ p.a. and 55000 francs in Lyons at $3 \%$ p.a. Find which investment has brought him in the greater income at the end of $2 \frac{1}{2}$ years, and the difference between the incomes in dollars. ( 1 (Newfoundland) dollar $=4 \mathrm{~s} .2 \mathrm{~d} . ; 1$ franc $=9 \cdot 513 \mathrm{~d}$.)

## SECTION XXI

## DISCOUNT

328. Merchants very often prefer to be paid "cash on delivery" rather than to allow credit ; in business, therefore, you would be prepared to accept from one of your debtors a little less than the actual amount due so that you might get the money at once, rather than wait a month or so for the full amount.

This is true for two reasons:
I. If you have the money it is no longer in the smallest degree uncertain, while if it is to be paid in the future there is more or less risk.
II. If you have the money you can use it, probably to very great advantage (see Interest, § 314).

Suppose, then, that a debtor owes you $£ 500$, payable in one month, you might accept $£ 498$ and allow him $£ 2$ in return for his immediate payment. This allowance, whenever and however made, is called a Discount, and the chief reason why merchants allow discount is to get " cash down."

We shall divide the subject into three parts:
A. Cash Discount.
B. Trade Discount.
C. Banker's, or Commercial Discount, and True Discount.

## A. Cash Discount

## I. RETAIL

329. A person goes into a house furnisher's shop and buys $£ 100$ worth of furniture, but does not wish to pay cash down. The retailer, however, wants cash, and so offers him a $5 \%$ cash discount-that is to say, he offers to accept $£ 95$ cash instead of £100 on credit.

Such a discount is called a Cash Discount.
330. Again, a tailor will often allow $2 \frac{1}{2} \%$ cash discount, a pianoforte dealer as much as $50 \%$, and very frequently we see on dairymen's carts, " $2 \frac{1}{2} \%$ cash discount on weekly (or monthly) accounts."

## II. WHOLESALE

331. The wholesale merchant allows the retailer a cash discount if his account is settled in a stated time, which is usually a month after delivery, and, in London, accounts between whole
sale and retail dealers are usually settled on the 10th of the month. A wholesale invoice usually states the conditions under which a cash discount is allowed. ${ }^{1}$
332. Example 1.-A tailor allows his customers $5 \%$ for cash, calculate the cash price of a suit of clothes priced £3 3s.

Cash discount $=5 \%$ of $£ 33 \mathrm{~s} .=3 \cdot 15 \mathrm{~s} .=3 \mathrm{~s} .2 \mathrm{~d}$., i.e. 3 s .
$\therefore$ cash price $=£ 3$.
Example 2.-A dairyman allows a cash discount of $2 \frac{1}{2} \%$ on monthly accounts. If the actual amount paid be $£ 210 \mathrm{~s}$., what was the gross amount of the account?

A net amount of $£ 97 \frac{1}{2}$ would mean a gross amount of $£ 100$

| $\therefore$ | " | " | £1 | " | " | $£_{9}^{100}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\therefore$ | " | " | $£ 2.5$ | " |  | $\pm 100 \times 25$. |
|  |  | " |  | " | " | 97.5 |

Example. 3.-- What cash discount does a grocer allow if he receives 18 s .4 d . on an account for 18s. 9d.?

Cash discount on 18s. 9d. is 5 d .

$$
\begin{array}{cccc} 
& " \quad 1 \mathrm{~s} . \quad " \frac{5}{18.75} \text { pence } \\
& " \quad " \quad 100 \mathrm{~s} . \quad, \frac{500}{18.75} \times 12 \\
\text { shillings } \\
\therefore \quad & " \quad \text { is } \frac{500}{18.75 \times 12} \%=2.22 \% .
\end{array}
$$

## EXAMPLES. LXXVI.

1. Explain what is meant by cash discount, and show what purpose it serves in commerce.

Allow the cash discount named on the amounts quoted in Questions 2 to 13, giving the answers to the nearest penny:
2. $5 \%$ on $£ 815 \mathrm{~s} .6 \mathrm{~d}$.
3. $6 \%$ on $£ 1214 \mathrm{~s} .8 \mathrm{~d}$.
4. $10 \%$ on $£ 312 \mathrm{~s} .4 \mathrm{~d}$.
5. $12 \frac{1}{2} \%$ on $£ 14 \mathrm{~s}$.
6. $7 \frac{1}{2} \%$ on 19 s .6 d .
7. $15 \%$ on $£ 2512 \mathrm{~s} .8 \mathrm{~d}$.
${ }^{1}$ See Examples XXXVIII., Questions 9, 10, 19, 23.

Calculate the gross amount of invoices when the net amount and the cash discount rate are as follows (Questions 14 to 25):

| Net Amount. | Rate of <br> Discount. | $\begin{gathered} \text { Net } \\ \text { Amount. } \end{gathered}$ | Rate of Discount. |
| :---: | :---: | :---: | :---: |
| 14. 15 s .8 d . | 21 | 20. £1 1 s . | $12 \frac{1}{2} \%$ |
| 15. $£ 112 \mathrm{~s} .4 \mathrm{~d}$. |  | 21. 18s. $0 \frac{1}{2} \mathrm{~d}$. | $7 \frac{1}{2} \%$ |
| 16. £3 15s. 6d. | $1 \frac{1}{2} \%$. | 22. £21 15s. 9d. | 15 |
| 17. £8 6s. 9 d . | 5 | 23. $£ 8212 \mathrm{~s} .10 \mathrm{~d}$. | 18 |
| 18. £11 19s. 5 d . | 6 | 24. £84 | 20 |
| 19. £3 5s. 1 d . | 10\%. | 25. £32 13s. | $33 \frac{1}{3}$ |

26. A clerk pays 15 s . 6 d . for a pair of boots, and has been allowed $5 \%$. What was the original price?
27. If a carpet is offered at $£ 1010$ s. and $2 \frac{1}{2} \%$ allowed for cash, find the cash price of the carpet.
28. I am offering a number of clocks at the popular figure of $2 \mathrm{~s} .6 \mathrm{~d} .$, with a cash discount of 2 d . in the shilling. What did I pay per dozen if I gain $15 \%(a)$ on my cost price; $(b)$ on my selling price?
29. A sports supply firm advertises cowhide cricket bags at a cash discount of $10 \%$. If a cricketer pays 24 s . for his bag, what was it marked?
30. My butcher's account amounts to 15 s .9 d . and he professes to have allowed me $2 \frac{1}{2} \%$. What is the gross amount?
31. A Strand auctioneer offers a plaster representation of the "Venus of Milo" for $£ 25$, declaring that he has allowed a cash discount of $20 \%$. What might have been the value of the goddess?
32. A bookseller obtains for you the latest Statistical Abstract of the British Self-Governing Dominions, ${ }^{1}$ etc., for 1s. 8d. It is published at 2 s . What discount per cent. does he allow?
33. Some jewellers in London have been holding sales, " because the premises are about to be pulled down," for upwards of five years, and have been offering $12 \frac{1}{2} \%$ off marked prices. What should one pay for the following articles: (1) an engagement ring marked 10s. 6d.; (2) a gold hunter watch priced $£ 55 \mathrm{~s}$. ; (3) a bracelet, £4 14s. 6d.; (4) a pair of silver-backed hair brushes, 45 s .9 (Give the prices to the nearest shilling in favour of the jeweller.)
34. From the data given make out a carefully ruled statement, putting prices for the figures given, which are either pints, pounds, or, in the case of eggs, dozens. Reckon 4 d . qt. for milk; ${ }^{1}$ This book is full of information. Get it.

6d. qt., nursery milk ; ls. 6d. lb., cream ; 1s. 4d. lb., fresh butter ; $1 \mathrm{~s} .6 \mathrm{~d} . \mathrm{lb} .$, Dorset butter ; ls. 6d. doz., eggs ; 1s. doz., cooking eggs.

35. Allow the cash discount quoted in the following list of articles which are to be included in an invoice. Charge for the casks, etc., as not having been returned (supply names, etc.) : Jan. 12, 85 -gall. drums lamp oil, 4 s .6 d . per drum ; 3 casks ( 40 galls.) lamp oil, 37 s . 1d. each ; 310 -gall. casks linseed oil, 3s. 6 d . per gall.; 28 -gall. drums linseed (boiled), 3 s . 6 d . per gall. ; 3 galls. machine oil, 1s. 10d. per gall. ; $8 \frac{1}{2}$ galls. gas-engine oil, 2 s .6 d . per gall.; 122 -gall. tins motor spirit, 3 s . each; 5 galls. Bosphorus air-cooled motor-oil, 3s. 6d. per gall. ; 12 galls. Colza (French) oil, 3s. 3d. per gall. ; $614-\mathrm{lb}$. tins deep chrome paint, $3 \frac{1}{2} \mathrm{~d}$. per lb. Casks, 1 s . each ; drums, 7 s .6 d . ; tins, 6d. each ; all jars contained in rest of order, 5s. 6d. Carriage, 2d. per gallou or per 14 lb . Cash discount, $7 \frac{1}{2} \%$.
36. Make out an invoice for the following, allowing the cash discount quoted (supply names) : 15 lb . butter @ $1 \mathrm{~s} .3 \mathrm{~d} . ; 10 \mathrm{lb}$. Irish salt @ 1s. 2d.; 12 lb . margarine @ 6 $\frac{1}{2} \mathrm{~d} . ; 12 \frac{1}{2} \mathrm{lb}$. English Cheddar@11d.; 61 $\frac{1}{2}$ lb. English Stilton @ 1s. 2d. ; 8 lb. lard @ $8 \frac{1}{2} \mathrm{~d}$. ; pail of American lard, 28 lb ., @, $7 \frac{1}{2} \mathrm{~d}$. ; gammon, 13 lb
(a) 10d. ; prime quarter side, 11 lb . @ 1s. $0 \frac{1}{2} \mathrm{~d}$. ; 6 galantines chicken and ham, 1 s . 10 d d. each; 3 galantines turkey and tongue, 1s. $10 \frac{1}{2}$ d. each. 8 packages charged 6 d . each ; rail charges, 12 s . 6 d. ; cash discount, $5 \%$.
37. A retailer's cost price is to his marked selling price as $8: 15$. He allows a cash discount to a customer such that cost price is to the actual selling price as $6: 11$. At what rate per cent. does he allow a cash discount?

## B. Trade Discount

333. A wholesale dealer in silver, silver-plate, etc., issues a price list, which costs him perhaps $£ 5000$ to proituce, and instead of charging the retailer the actual prices quoted he allows him a discount (for reasons given below), which may vary from $20 \%$ to $50 \%$, while in some trades it is as low as $10 \%$ or as high as $75 \%$.

The discount that the wholesale dealer allows the retailer off the list price is called a Trade Discount.
334. If now the manufacturer raises his prices obviously the price list might be thrown out entirely, and the wholesale house might have to issue a new one. Clearly enough this is a very costly matter, and to avoid the expense the prices stand as they are, but a smaller trade discount is allowed.

Thus, if a particular kind of watch were listed at $£ 10$, and a trade discount of $25 \%$ were allowed, then the retailer would pay $£ 710$ s. for it. If the manufacturer raised his price, either (1) the $£ 10$ would have to be altered to, say, $£ 12$, and the watch would then cost £9: or (2) the wholesale dealer could allow $10 \%$ trade discount instead of $25 \%$ on the list price of $£ 10$, and the watch would then cost $£ 9$, but the cist price would remain as before.

Thus trade discount is a means whereby the wholesale dealer can adjust the price charged to the retailer so as to meet any fluctuations of the market of the manufacturer, and thus save the cost of producing a new price list.

If the student were to take up almost any price list issued in the last five years he would find a slip enclosed saying that the trade discount had been reduced from, say, $25 \%$ to $10 \%$ because of increased cost of production or of raw material-wood, wool, cotton, etc.
335. Example 1.-Messrs. Webb \& Co., house furnishers,
have a suite listed at 30 guineas and allow $20 \%$ trade discount. What does the retailer pay for it?

$$
\begin{aligned}
20 \% \text { on } 30 \text { guineas } & =\frac{20}{100} \text { of } £ 31 \cdot 5 \\
& =£ 6 \cdot 3 \\
\therefore \text { retailer pays } & £ 31 \cdot 5-£ 6 \cdot 3 \\
& = \pm 25 \cdot 2 \\
& =£ 254 \mathrm{~s} .
\end{aligned}
$$

Example 2.-A retail dried-fruit merchant buys at a trade discount of $12 \frac{1}{2} \%$. What is the list price of a consignment of currants for which he pays £18 10s. ?

Retail price, $£ 87 \frac{1}{2}$, gives list price $£ 100$

$$
\begin{aligned}
& \text { " " £1, " } \quad £_{\frac{100}{87 \cdot 5}}^{10} \\
& \text { " "£18.5, " " } £ \frac{100 \times 15}{87.5} \\
& =£ 212 \mathrm{~s} .10 \mathrm{~d} .
\end{aligned}
$$

Example 3.-If the list price of a motor-car is 128 guineas, and the retail dealer obtains the same for 102 guineas, find the trade discount.

The retail price is $\frac{102}{123}$ of the wholesale price
$\therefore$ the " " $\frac{10.2}{12}$ of $100 \%$ "

$$
=79.7 \% ;
$$

$\therefore$ the retail price is $79.7 \%$ of the wholesale price ;
$\therefore$ the trade discount is $20.3 \%$, i.e. $20 \%$.
Example 4.-Brooks \& Co. manufacture crystal glass vases which they list at $£ 60$ per dozen, and allow the wholesale trade a trade discount of $20 \%$. The cost of manufacture advances $5 \%$; at what rate must they allow a trade discount to avoid altering the list price?

First list price is $£ 60$ per dozen.
First price to wholesale dealer is $£ 60$, less $20 \%$ of $£ 60$, or $£ 48$.

Second list price ought to be $£ 60+5 \%$ of $£ 60$, or $£ 63$.

Hence the price the wholesale dealer pays must bear to $£ 63$ the same ratio that $£ 48$ bears to $£ 60$;
$\therefore$ price paid by wholesale dealer $=£_{\frac{48}{60}}^{48} \times 63=£ 508 \mathrm{~s}$, :
and all that remains is to find what rate of discount is allowed on $£ 60$ to give $£ 508 \mathrm{~s}$.

$$
\begin{aligned}
& \quad \text { Discount on } £ 60=£ 912 \mathrm{~s} . \\
& \therefore \quad, \quad £ 100=£ \frac{100 \times 9 \cdot 6}{60}=£ 16 \\
& \therefore \text { trade discount is reduced to } 16 \% .
\end{aligned}
$$

## EXAMPLES. LXXVII.

1. Explain the use of trade discount in commercial operations, and distinguish it from cash discount. Could both be allowed on any transaction? Does trade discount apply to the retail as well as to the wholesale trade?

Find the retailer's cost price from the following wholesale list prices and the given trade discount rate (Questions 2 to 11):

| Wholesale List Price. | Trade Discount. | Wholesale List Price. | Trade Discount. |
| :---: | :---: | :---: | :---: |
| 2. $£ 5$ | $20 \%$ | 7. $£ 2514 \mathrm{~s} .9 \mathrm{~d}$. | $33 \frac{1}{3}$ |
| 3. $£ 710 \mathrm{~s}$. | $18 \%$ | 8. £158 13s. 9 d . | $40 \%$ |
| 4. $£ 815 \mathrm{~s}$. | 121 18. | 9. £459 17s. 6d. | $45 \%$. |
| 5. £10 10s. | - $50 \%$ | 10. £100 16s. 8 d . | - $62 \%$ |
| 6. £18 15s. 8d. | - $25 \%$. | 11. $£ 28012 \mathrm{~s} .6 \mathrm{~d}$. | $68 \%$. |

What was the wholesale list price of the following articles, the retailer's cost price and trade discount being given (Questions 12 to 21):

Goods.
12. Turkey carpet
13. Works of Dickens .
14. Cases of raisins
15. Coal and coke

Retailer's
Cost Price.
$£ 713 \mathrm{~s}$.
£4
$£ 55 \mathrm{~s}$.
$£ 14$ 1s. 9d.
£252 18s. $7 \frac{1}{2} \mathrm{~d}$.
£89 16s.
$68 \%$ ?
17. Motor accessories
$£ 63 \mathrm{~s}$.
$18 \%$ ?
18. Account books
$£ 63$ 9s. 6d.
$40 \%$ ?
20. Linens . . . . . $£ 386 \mathrm{~s} .4 \mathrm{~d}$.
21. Stationery

- $£ 17$ 3s. 2 d .
$62 \%$ ?
- • • •
$33 \frac{1}{3} \%$ ?

Trade Discount.

What trade discount has been allowed in each of the following cases :

32. The list price of a watch is $£ 1515 \mathrm{~s}$. ; the trade discount $10 \%$. What does the retailer pay?

33 . The list price of a case of fish servers is 35 s ., and $12 \frac{1}{2} \%$ is allowed ; find the price to the retailer.
34. The price of $7-\mathrm{lb}$. jars of jam per dozen is $£ 11 \mathrm{~s}$., and $5 \%$ is allowed. Find the net price per jar.
35. Gas fittings are listed at $33 \frac{1}{3} \%$ above the price the retailer has to pay. What does a pair of ornamental brackets listed at 18 s .6 d . cost him?
36. Boots listed at 17 s .6 d . a pair are sold at 11s. 8 d . What percentage is the retailer allowed off the list price?
37. A draper pays 36 s. each for ladies' serge costumes, and has been allowed $24 \%$ off the list price. Calculate the latter.
38. What is the retail price per dozen of books listed at $£ 9$ a gross and sold at $30 \%$ trade discount?
39. At what price must each book of the last question be sold to the public in order that the retailer may make $10 \%$ profit on the selling price?
40. What is the trade discount if the retailer pays $£ 1515 \mathrm{~s}$. for a marble statuette listed at $£ 52 \mathrm{~L}$ 10s. ?
41. What is the list price per dozen of walking-sticks sold to the retailer at a discount of $20 \%$ for 25 s . per dozen?
42. A wholesale draper allows $15 \%$ off his list prices, and a retail dealer pays 2 s . $1 \frac{1}{2} \mathrm{~d}$. per dozen yards of calico. What is the list price per dozen yards?
43. If the list price of coffee per cwt. be $£ 44 \mathrm{~s}$. and the retailer pays $£ 319 \mathrm{~s}$. 10 d., what is the trade discount?
44. The retail price of a cask of moter oil is $£ 711 \mathrm{~s}$. 1 d ., and the trade discount $7 \frac{1}{2} \%$ off the list price. What is the list price?
45. Complete the following invoice, allowing trade discount $12 \frac{1}{2} \%$ (items 2 and 3 are net):

46. Make out an invoice for the following, allowing $20 \%$ trade discount, choosing your own names for buyer and seller, etc. : 6 lawn mowers @ 26s. 9d; 9 garden rollers, 24 by 27, weight 4 cwt .2 qrs., @ $45 \mathrm{~s} .9 \mathrm{~d} . ; 1$ dozen lawn seats with arms, @ 5s. 3d. (net) ; 3 improved rainproof shelters @ 41s. ; 1 dozen rustic tables, elm, 15 in . diameter, @ 6s. (net); 3 dozen strong chairs in genuine Willesden canvas @ 3s. 6d. Receipt this account.
47. Taking the two invoices (pages 461 and 462) make them out, allowing trade discounts of $25 \%$ and $30 \%$ respectively, and also cash discounts of $5 \%$ and $2 \frac{1}{2} \%$ respectively, and receipt them.
48. A wholesale merchant lists wine at 500 s . a barrel of 110 gallons, and allows a trade discount of $15 \%$. The retail dealer eharges $20 \%$ more than his cost price per gallon, but finds in the
end that he has 2 gallons of bilge in the bottom of the cask which are useless. What is his actual percentage profit?
49. The wholesale list price of shellac is to the retailer's cost price as $3: 1 \frac{1}{4}$. What is the trade discount?

## C. Banker's (or Commercial) and True Discount

336. We have already explained that a merchant will allow one of his customers a discount for cash, but it very often happens that the customer will not pay cash, even though a discount is offered him, and this may be (1) because he has not the cash by him ; or (2) because he can use the money himself and make more out of it than the discount the merchant offers him.

33\%. In point of fact, the interests of the merchant and customer are very often opposed to one another : the former wants the money at once and offers a discount as a bait ; the latter wants to keep the money for a month or two and use it himself, so that whether he accepts the discount or not will depend on whether he can make more by keeping his money and using it himself. If he can, he will not accept the discount.

The length of time that credit is allowed depends on the character of the trade concerned, and may vary from a few days to 3 months, 90 days or even more. In any case, a merchant will not generally let a customer have credit for any length of time without some written statement to the effect that the money is owing.
338. Let us illustrate the matter thus. Sir John Falstaff is a merchant to whom Messrs. Quickly, of Eastcheap, have sold wine to the value of $£ 1000$, payable in 3 months. They will not, however, accept his word that he will pay, but prepare an Inland Bill of Exchange, ${ }^{1}$ which must be properly stamped. ${ }^{2}$ It will appear as shown in Plate XIII. (p. 468).
339. There are now several points to be noted:

1. A "Bill" is a contraction for a "Bill of Exchange," and has nothing whatever to do with an Invoice.
2. Instead of the bill being made payable in 3 months it might have been due 6 months, etc., after date, or "at sight," in which case Sir John would have been obliged to pay when it was presented to him for payment ; this also applies to bills "on demand."

[^43]3. Since Messrs. Quickly drew the bill they are the Drawers, while Sir John is the Drawee, and he has to pay. When he writes acciepted across it he becomes the Acceptor, and until he has done so the bill is of no value. The student will now write the name "John Falstaff" across Plate XIIT. just below the red ink "London, E.C.," and thus "accept" the bill as if he were the acceptor. If the money is paid to Messrs. Quickly (or their $\overline{\text { agents) they }}$ are the Payees.
4. The bill was drawn on 10th March and is due on 13th June, which is 3 months and 3 days after date. ${ }^{1}$ These 3 days, called I)ays of Grage, are allowed in Canala as well as in the United Kingdom. In the United States the period varies, but days of grace are not allowed on inland bills ${ }^{2}$ in other countries.

Days of grace are not allowed on bills drawn "at sight" or "on demand," for they must be met when they are presented. The student is referred to Part III. for a facsimile of some Foreign Bills of Exchange.
340. So far then, Sir John, not wishing to pay cash, has given a definite promise to pay $£ 1000$ into the Bank on 13 th June, hoping to use the money to great advantage in the meantime. If Messrs. Quickly had liked they could have obtained Sir John's promise in the form of a properly stamped Promissory Note ${ }^{3}$ which would have been similar to Plate XIV. (p. 470).
341. The student should notice that bills are far more largely used than Promissory Notes. If an acquaintance asked you for a loan of $£ 20$ for a few months you would get him to sign a Promissory Note and not saddle him with a bill; or, if you wanted to borrow a little money from your life insurance company on the security of a life policy, they would ask you to deposit the latter with them, and sign a Promissory Note to give them the necessary protection.
342. Messrs. Quickly now hold Sir John's bill and he uses his money to the best of his ability. But they too want cash badly, and so they try to sell the bill (just as you might, in

[^44]another place, sell bread or flour), and so get cash at once instead of waiting 3 months.

Messrs. Quickly, therefore, take the bill to a bill-broker ${ }^{1}$ who looks it down and says to himself that Sir John Falstaff, whom he knows, is "good" for the amount, ${ }^{2}$ and then he offers, say, $£ 980$ for the bill. Clearly enough he will not offer $£ 1000$, for he may have to wait 3 months for his money, but he will offer rather less; in other words, the broker will Discount the Bill, pay over the cash, and then either keep the bill till it matures, that is, becomes due, on 13th June, or sell it to some one else for $£ 982$ and so make a profit. If he keeps it he will send it to the Bank and receive the money or have it paid into his account on the "due date" (13th June).
343. We might just summarise our proceedings to this point.

Sir John Falstaff owes Messrs. Quickly £1000. He will not pay cash. He "accepts" a 3 months' bill drawn by Messrs. Quickly. They want cash and so sell the bill to the bill-broker for $£ 980$. The broker keeps it till it matures and then receives the $£ 1000$, or he sells it to some one else for $£ 982, £ 983, £ 990$, as the case may be, and so makes a profit.

As a matter of fact, an enormous amount of business is done every week at the Royal Exchange in simply buying and selling bills.
344. We must notice, however, that the broker might refuse to buy the bill under the following circumstances:

1. If bills were very plentiful, or he had already bought a good many.
2. If Sir John Falstaff were not a well-known merchant.

The Rate at which he will discount the bill, and consequently the amount Messrs. Quickly will receive, will depend (among other things, which we shall deal with in their proper place) on

1. Whether money is plentiful or not. If it is, the broker will be disposed to give a little more than if it is not.
2. Whether the Bank rate is high or low (Part III.).
3. Whether the acceptor's name is good, bad, or indifferent. A broker might have three or four $£ 1000$ bills, and yet might offer $£ 985, £ 990, £ 750$, or $£ 700$ for them, respectively, because the first two are accepted by wellknown men, and the others bear names not so creditable in the financial sense.

[^45]345. When the broker has decided to buy the bill and settled the Rate at which he will discount it, he must calculate the Amount of the discount, which is always reckoned to the nearest penny, and which will depend

1. On the amount for which the bill is drawn;
2. On the time that it has to run before its due-date;
for the greater the amount of the bill the greater will be the discount, so also will it be greater the longer the time it has to run.
(The student should try to explain the last statement in his own words, for it involves the fundamental principle of discount.)

This is the question :
What discount must be allowed on a bill of $£ 1000$, dated 10th March at 3 months, and discounted on 14th April at $4 \%$ ?

The bill is due on 13th June (not 10th June).
The bill is discounted on 5th April.
$\therefore$ The bill is discounted 60 days before it is due.
The question reduces itself to this:
What is the simple interest on $£ 1000$ for 60 days at $4 \%$ ?

$$
\text { Interest }=10.00 \times \frac{60}{365} \times 4
$$

$=£ 611 \mathrm{~s} .6 \mathrm{~d}$. , to the nearest penny.
$\therefore$ the discount $=£ 6$ 11s. 6 d .
$\therefore$ the cash paid $=£ 1000-£ 611 \mathrm{~s} .6 \mathrm{~d}$.
$=£ 9938 \mathrm{~s} .6 \mathrm{~d}$., which is called the present worth of the bill, or better, the discounted value of the bill.
346. We have here found the discount just as it is found every day by bankers and by bill-brokers, and so it is called the Banker's or Commercial Discount (it might just as well be called the bill-broker's discount), and it equals the interest on the bill at a specified rate for the time between the date of discounting and the date of maturity.

Hence-
Bill - Banker's discount $=$ Discounted value or present worth.
347. In point of fact a bill for $£ 100$ due 6 months hence may
be worth $£ 98$ to-day, and it is obvious that in discounting it to-day we should allow the discount on to-day's value, $£ 98$, but bankers allow the discount on the $£ 100$ and thus save the trouble of finding the present value.

The discount on $£ 98$ would be called the True Discount, and that on the $£ 100$ the Banker's Discount. The latter is always used in commercial practice, and is always greater than the former, but the illogical nature of the procedure is compensated for by the brevity of the work involved.
348. If the broker had had any doubt whatever about Sir John's solvency he would have refused to negotiate the bill, unless it was "backed"-that is to say, the holder would have to take it to a banker, or to a merchant whose reputation was sufficiently high to be accepted by the broker, and ask him to sign his name, Lionel B. Josh, on the back ; then if Sir John failed to pay, Mr. Lionel B. Josh would have to do so. If he did not, then the holder of the bill could put the bailiff into his house and sell his goods or, following the money-lenders' custom, could make him a bankrupt ${ }^{1}$ and so obtain at least a part of the amount due.

It is a safe rule scrupulously to abstain from backing bills for any one.
349. It is most important to note that, in reckoning interest or discount, only one day of the two extreme ones is counted, e.g. 4th to 11 th February is 7 , not 8 days. 14th February to 10th March is 14 days in Febrnary and 10 in March, 24 in allthat is to say, a simple subtraction sum enables one to find the number of days that a bill has to run. The "table of days" (see p. 474) will be found useful, although most office diaries give the number of days to the end of the year, and so serve the same purpose as the table. In a leap year add one to each number after 28th February, that is to say, after the 59th day.
350. Example 1.-Find the banker's discount on a bill for £580 drawn on 4th February in London on a merchant in America at 93 days and discounted at $2 \frac{1}{2} \%$ on 19th March.

February 4 to March $19=43$ days (ordinary year)
Bill due 93 days after date $=93$
Discounted before maturity by 50
9
$\therefore$ banker's discount $=£ 5 \cdot 8 \times \frac{50}{365} \times 2.5$
$=£ 119 \mathrm{~s} .9 \mathrm{~d}$. , to the nearest penny.
${ }^{1} \S 258$ to § 262.

Example 2.-Discount in Paris, on 21st September, a bill for 10000 francs at $4 \%$ p.a. due 30th November.

In France days of grace are not reckoned.
Bill is due 30th November
,, ", discounted 21st September
Difference $=70$ days.
What is then the S.I. on 10000 francs for 70 days at $4 \%$ ?
S.I. or banker's discount $=£ 100 \times \frac{70}{365} \times 4$

$$
=76.7 \text { francs }
$$

Example 3.-Upon what amount would a bill-broker allow a discount of $£ 506 \mathrm{~s}$. 8 d . at $3 \frac{1}{2} \%$ p.a. if the bill matured in 73 days, including days of grace?

On $£ 100$ due 365 days hence the discount is $£ 35$ s.
On $£ 100$ due 73 days hence the discount is $£ \frac{73}{365}$ of $3.5=£ 0.7$
$\therefore$ on $£ 100 \div 0 \cdot 7$ due 73 days hence the discount is $£ 1$
$\therefore$ on $\frac{100}{0 \cdot 7} \times £ 506 \mathrm{~s} .8$ d. due in 73 days, the discount is $£ 506 \mathrm{~s} .8 \mathrm{~d}$.
$\therefore$ sum required $=£ \frac{100}{0.7} \times 50.3333=£ 71909 \mathrm{~s} .6 \mathrm{~d}$.
$\therefore$ discounted value is $£ 71909$ s. 6d. less $£ 506$ s. 8 d., or $£ 71402 \mathrm{~s} .10 \mathrm{~d}$.
Example 4.-A 3-months' bill is discounted at $4 \%$ p.a. To what rate of interest is this equivalent?

The broker would deduct $£ 4$ on a 12 -months' bill for $£ 100$ at $4 \%$ p.a.
$\therefore$ he deducts $£ 1$ from a 3 -months' bill for $£ 100$ at $4 \%$ p.a.
$\therefore$ the broker receives $£ 1$ as the interest on $£ 99$ for 3 months, and we want to know how much he would receive on $£ 100$ for 12 months, that is, the rate \% p.a.

Since he gets $£ 1$ on $£ 99$ for 3 months

$$
\begin{aligned}
& \text { " } \quad £_{\frac{1}{99}} \times 100 \text { on } £ 100 \text { for } 3 \text { months } \\
& \quad \text { or, } £ \frac{100}{99} \times 4 \text { on } £ 100 \text { for } 1 \text { year. } \\
& \therefore \text { Interest p.a. on } £ 100=4.04 \\
& \therefore \text { Rate } \% \text { p.a. } \quad=4.04
\end{aligned}
$$

Example 5.-A merchant purchases a motor-car valued £405, and agrees to settle the account in 7 months' time. At
the end of a month he finds he can pay. What amount should he offer (reckoning $2 \frac{1}{2} \%$ ) if he is to lose nothing by paying ?

1. Taking true discount.

Time account has to run $=6$ months.
Interest on $£ 100$ for 6 months at $2 \frac{1}{2} \%=£ 1 \cdot 25$.
$\therefore$ if bill were $£ 101 \cdot 25$ the discounted value would be $£ 100$.
If bill were $£ 1$ the discounted value would be $£ \frac{100}{101.25}$
Since bill is $£ 405$ the discounted value is $£ \frac{100 \times 405}{101.25}$

$$
=£ 400,
$$

and so the true discount is $£ 5$.
2. Taking commercial discount.

Interest on $£ 405$ for 6 months at $2 \frac{1}{2} \%$ p.a.
$=£ 4.05 \times 1.25$
$=£ 5.063$
$=£ 51 \mathrm{~s} .3 \mathrm{~d} .$, to the nearest penny,
and the difference of 1 s . 3 d . is not worth the extra work, nor would any one bother about it.

Example 6.-The difference between the banker's and true discount on a bill due in 6 months is 4 s . If the discount rate be $4 \%$ p.a., calculate the amount of the bill.

1. True discount.
$£ 100$ now is worth $£ 102$ in 6 months at $4 \%$ p.a.
$\therefore$ a bill of $£ 102$ due 6 months hence is worth $£ 100$ now.

$$
\therefore \quad " £ 100 \quad " \quad \begin{array}{r}
\frac{100}{102} \text { of } £ 100 \quad " \\
=£ 98 \cdot 0392
\end{array}
$$

$\therefore$ the true discount is $£ 100-£ 98 \cdot 0392=1 \cdot 9608$.
2. Banker's discount.

The banker's discount on $£ 100$, due 6 months' hence at $4 \%$ p.a., is $£ 2$.
$\therefore$ If the bill be $£ 100$ the difference between banker's discount and true discount is $£ 2-£ 1.9608$ or $£ 0 \cdot 0392$; hence the amount of a bill upon which the difference is 4 s ., or $£ 0 \cdot 2$, is

$$
\frac{£ 100 \times 0.2}{0.0392}=£ 5104 \mathrm{s.} .1 \mathrm{~d} .
$$

This can be proved by finding the banker's discount and the true discount on $£ 5104 \mathrm{~s}$. 1d., and showing that the difference is 4 s .

TABLE OF DAYS．

|  | $\stackrel{\text { g }}{\text { g }}$ | $\begin{aligned} & \dot{\square} \\ & \stackrel{0}{4} \end{aligned}$ | 嵌 | 安 | $\stackrel{\dot{m}}{\text { 分 }}$ | $\underset{\Xi}{\underset{\Xi}{\Xi}}$ | $\stackrel{\underset{\sim}{3}}{\underset{3}{\circ}}$ | $\stackrel{\dot{x}}{\stackrel{c}{4}}$ |  |  | $\stackrel{\dot{\circ}}{8}$ | ¢ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | 1 | 32 | 60 | 91 | 121 | 152 | 182 | 21 | 24 | 274 | 305 | 5 |
| 2. | 2 | 33 | 61 | 92 | 122 | 153 | 183 | 214 | 245 | 275 | 306 | 336 |
| 3. | 3 | 34 | 62 | 93 | 123 | 154 | 184 | 215 | 246 | 276 | 307 | 337 |
| 4. | 4 | 35 | 63 | 94 | 124 | 155 | 185 | 216 | 247 | 277 | 308 | 338 |
| 5. | 5 | 36 | 64 | 95 | 125 | 156 | 186 | 217 | 248 | 278 | 309 | 339 |
| 6. | 6 | 37 | 65 | 96 | 126 | 157 | 187 | 218 | 249 | 279 | 310 | 340 |
| 7. | 7 | 38 | 66 | 97 | 127 | 158 | 188 | 219 | 250 | 280 | 311 | 341 |
| 8. | 8 | 39 | 67 | 98 | 128 | 159 | 189 | 220 | 251 | 281 | 312 | 342 |
| 9. | 9 | 40 | 68 | 99 | 129 | 160 | 190 | 221 | 252 | 282 | 313 | 343 |
| 10. | 10 | 41 | 69 | 100 | 130 | 161 | 191 | 222 | 253 | 283 | 314 | 344 |
| 11. | 11 | 42 | 70 | 101 | 131 | 162 | 192 | 223 | 254 | 284 | 315 | 345 |
| 12. | 12 | 43 | 71 | 102 | 132 | 16 | 193 | 22 | 255 | 28 | 316 | 46 |
| 13 | 13 | 44 | 72 | 103 | 133 | 164 | 194 | 225 | 256 | 286 | 317 | 347 |
| 14. | 14 | 45 | 73 | 104 | 134 | 165 | 195 | 226 | 257 | 287 | 318 | 348 |
| 15. | 15 | 46 | 74 | 105 | 135 | 166 | 196 | 227 | 258 | 288 | 319 | 349 |
| 16. | 16 | 47 | 75 | 106 | 136 | 167 | 197 | 228 | 259 | 289 | 320 | 350 |
| 17. | 17 | 48 | 76 | 107 | 137 | 168 | 198 | 22 | 260 | 29 | 321 | 51 |
| 18. | 18 | 49 | 77 | 108 | 138 | 169 | 199 | 230 | 261 | 291 | 322 | 352 |
| 19. | 19 | 50 | 78 | 109 | 139 | 170 | 200 | 231 | 262 | 292 | 323 | 353 |
| 20. | 20 | 51 | 79 | 110 | 140 | 171 | 201 | 232 | 263 | 293 | 324 | 354 |
| 21. | 21 | 52 | 80 | 111 | 141 | 172 | 202 | 233 | 264 | 294 | 325 | 355 |
| 22. | 22 | 53 | 81 | 112 | 142 | 173 | 203 | 23 | 265 | 295 | 326 | 356 |
| 23. | 23 | 54 | 82 | 113 | 143 | 174 | 204 | 235 | 266 | 296 | 327 | 357 |
| 24. | 24 | 55 | 83 | 114 | 144 | 175 | 205 | 236 | 267 | 297 | 328 | 358 |
| 25. | 25 | 56 | 84 | 115 | 145 | 176 | 206 | 237 | 268 | 298 | 329 | 359 |
| 26. | 26 | 57 | 85 | 116 | 146 | 177 | 207 | 238 | 269 | 299 | 330 | 360 |
| 27. | 27 | 58 | 86 | 117 | 147 | 178 | 208 | 239 | 270 | 300 | 331 | 361 |
| 28. | 28 | 59 | 87 | 118 | 148 | 179 | 209 | 240 | 271 | 301 | 332 | 362 |
| 29. | 29 |  | 88 | 119 | 149 | 180 | 210 | 241 | 272 | 302 | 333 | 363 |
| 30. | 30 | － | 89 | 120 | 150 | 181 | 211 | 242 | 273 | 303 | 334 | 364 |
| 31. | 31 | － | 90 |  | 151 |  | 212 | 243 |  | 304 | － | 365 |

## EXAMPLES．LXXVIII．

1．Explain the use of a bill of exchange and of a promissory note．
2．Draw up a bill for $£ 500$ where J．Brook is the drawer， T．Nunn the drawee，who accepts it，payable at the Union Bank in 3 months．

3．Distinguish between banker＇s and true discount．
4．Explain what you mean by discounting a bill and by its discounted value．

5．T．Jones borrows $£ 50$ from R．Bell．Draw up a promissory note showing the amount due in 3 months at $5 \%$ p．a．interest．
6. A wine merchant holds a stock which he reckons will be worth $£ 1500$ in 3 years. In determining its present value should he reckon banker's or true discount, and why?

What is the discounted value ${ }^{1}$ of the following bills:

(The student should now take any names that may occur to him and draw up twelve bills in accordance with the data given in Questions 7 to 18.)

Find the value of the following bills discounted on the day that they were drawn (Questions 19 to 30 :)
19. 51100 francs drawn 25th January, due 25th March, at $1 \frac{1}{4} \%$.
20. 21900 dollars drawn 10th August for 3 months at $2 \%$ (U.S.A.). (Allow 6 days' grace.)
21. 10950 dollars drawn 25th June for 60 days at $3 \%$ (Canada).
22. 29200 drachmæ drawn 8th April, due 8th May, at $2 \frac{3}{4} \%$.
23. 14600 marks drawn 5th December, due 10th March (leap year), at $3 \%$.
24. 80000 roubles drawn 15 th October for 6 months at $21 \%$.
25. 58400 gulden drawn 10 th December for 60 days at $3 \%$.
26. $£ 250$ due 37 days hence at $3 \frac{1}{2} \%$ p.a.
27. $£ 560$ due 70 days' sight at $2 \frac{3}{4} \%$ p.a.
28. 4015 francs due 60 days hence at $4 \frac{1}{4} \%$ p.a.
${ }^{1}$ In Questions 7 to 30 "days of grace" should be allowed if and when the monetary unit employed belongs to a country where days of grace are usually allowed. The due-date which we give does not include the days of grace.
29. 12045 roubles due 80 days hence at $6 \frac{1}{2} \%$ p.a.
30. 8030 lire due 146 days hence at $3 \frac{3}{4} \%$ p.a.

In the following questions do not add Days of Grace unless told to do so :
31. What is the discount on a bill for $£ 35016 \mathrm{~s}$. 8 d . maturing on 23 rd December and discounted at $6 \%$ p.a. on 30 th September?
32. What is the discounted value of a bill for 50000 francs due 25 th July and discounted on 24th June at $2 \frac{1}{4} \%$ p.a.?
33. I have a bill for $£ 7300$ due on 25 th November and I sell it on 20th August at a discount rate of $4 \%$ p.a. Would it have been better for me to have held it till let September and sold it then at a discount rate of $4 \frac{1}{4} \%$ p.a.?
34. A broker charged $3 \frac{1}{2} \%$ p.a. in discounting on 15 th September a bill which matured on 1st November, and received $£ 23$ 10 s . by way of discount. What was the amount of the bill?
35. If in Question 34 the discount had amounted to $£ 73$, what would have been the amount of the bill?
36. A bill for 3504 dollars is due on 3 lst January and is discounted in New York on 27th November, 24.96 dollars being allowed as discount. What is the rate per cent. p.a.?
37. What is the rate per cent. p.a. charged in discounting, on 4 th April, a bill for $£ 876$, which matures on 25 th May, if the discount allowed is $£ 72 \mathrm{~s}$. 7 d .?
38. We see by our newspapers that the East Indian Railway Company (guaranteed by the Secretary of State for India) wants people to subscribe $£ 3,500,000$ in multiples of $£ 100$ as follows : $£ 5 \%$ at once ; $£ 24 \%$ on 21 st May ; $£ 20 \%$ on 11 th June ; £25 \% on 8th July ; and $£ 25 \%$ on 5th August. We are informed, too, that all the balance can be paid on 21st May and will be discounted at $2 \frac{1}{2} \%$ p.a. How much must we pay on 21st May?
39. "War Loan 1925-1928, bearing interest at $3 \frac{1}{2} \%$ p.a. Applications must be for $£ 100$, or multiples of $£ 100$, which must be paid as follows: $£ 2 \%$ on application: $£ 3 \% 7$ th December 1914 ; £10 \% 21st December 1914; £10 \% 7th January 1915 ; $£ 10 \%$ 21st January 1915 ; £10 \% 4th February 1915 ; £10 \% 22nd February 1915; £10 \% 11th March 1915 ; £10 \% 25th March 1915 ; $£ 10 \% 12$ th April 1915 ; $£ 10 \% 26$ th April 1915." Find the amount that must be paid on 7 th December 1914, per $£ 100$ stock, to complete the outstanding payments, discount being reckoned at 3 \% p.a. (See also Question 40.)
40. If we paid on 1lth March what discount was allowed us?
41. A banker discounts, on 29 th December, a bill for $£ 57515 \mathrm{~s}$.
drawn on 28 th October at 3 months allowing $2 \frac{1}{4} \%$ p.a. Find (1) the amount of the discount; (2) the rate per cent. p.a. which he receives as interest on his money.
42. If the tigures for the last question had been $£ 100010$ s. 6d. due 30th January discounted on 31 st December at $2 \frac{1}{8} \%$ p.a., what would have been the rate per cent. p.a. at which the banker received interest on his money?
43. If I took a bill to my broker and he deducted $£ 3$, and handed me the balance, find what I received if the discount rate was $5 \%$ p.a. and the bill had 30 days more to run.
44. You have a bill for $£ 700$ which your banker discounts at $3 \%$ p.a., and you put the cash received into the Bank at $2 \frac{1}{2} \%$. If the bill were due in 6 months would you gain or lose by the transaction, and how much?
45. For what time would it be necessary to keep the money referred to in Question 44 in the Bank so that you would neither gain nor lose? (Reckon 30 days to a month, and give the answer to the nearest day.)
46. What will you offer on 11th May for a bill of $£ 865$ due 10th July if you know the discount rate to be $2 \frac{3}{4} \%$ p.a.?
47. If you sold the bill (Question 46) on 21st May at $3 \%$ p.a. discount, what profit did you make?
48. A merchant buys goods agreeing to pay the full cash value of $£ 560$ on delivery. He finds, however, that he cannot pay, and so asks for a 3 -months' bill. His creditor finds that the current rate of discount yesterday was $2 \%$ p.a., but charges $2 \frac{1}{4} \%$ in drawing the bill to safeguard himself. For what amount should the bill be drawn?
49. To what interest rate per cent. p.a. is a discount rate of $4 \%$ on 60 -day bills equivalent?
50. A draper purchases goods to the value of $£ 10000$ from the wholesale house and agrees to pay $£ 3500$ down and the balance in 3 months. If the discount rate p.a. be $4 \%$, for what amount must a 3 -months' bill be drawn so that the creditor may not lose any money at all ?
51. What would you offer now for a consignment of wine which will be worth $£ 10000$ in 12 months? (Interest, $5 \%$ p.a.)
52. A merchant has received a consignment of iron pipes which he can pay for in cash at $3 \%$ cash discount, or at 3 months net. Which course should he adopt if he can get $3 \frac{1}{2} \%$ p.a. on his money by holding it over?
53. If the discount on a bill for $£ 3807 \mathrm{~s} .8$ d. due 24 th December and discounted on 25 th September be $£ 22 \mathrm{~s}$. $2 \frac{1}{2} \mathrm{~d}$., what is the discount rate per cent. p.a.?

54 . The discount on a bill for $£ 7456$ s. 4 d. at $3 \%$ p.a. is $£ 18$ 7 s .6 d . For how many days had it to run (to the nearest day) ?
55. One of my clients owes me £485 which is due on 30 th November, but he offers to pay on 14th October. What amount shall I accept if the current discount rate is $2 \frac{1}{2} \%$ p.a.?

56 . Upon what amount due 6 months hence at $5 \%$ is the difference between the banker's and true discount 12s.?
57. A merchant has a 3 -months' bill for $£ 100$ which his broker discounts at $2 \frac{1}{2} \%$. Find what rate per cent. p.a. he must earn on the discounted value so that he does not lose by selling the bill.
58. If the Govermment has borrowed $£ 150,000,000$ at $4 \%$ and sets aside $£ 30,000,000$ a year partly to meet the interest due and partly to paying off the debt, in how many years will the whole be settled? (Work after reading Part III.)
59. A fruit-grower reckons that his orchards will be worth $£ 5000$ in 4 years' time. What would you offer for them now, reckoning Simple Interest at $4 \%$ ?
60. A broker buys a $£ 350$ bill and he allows $2 \frac{1}{2} \%$ p.a. discount. If it had 60 days to run (including days of grace), at what rate must the money be invested that the vendor of the bill may not lose anything?
61. Upon what sum of money due 146 days hence at $4 \%$ p.a. is the difference between the commercial and true discount 15 s .?

## SECTION XXII STOCKS AND SHARES

## A. Stocks

351. Smith is an old friend of mine who has been working at dyes for some years. Yesterday he asked five of us round to his house, and told us the general plan of a scheme he has in his mind for developing a particular dye and for making it pay. He also explained that he wanted $£ 500$ to buy machinery and the like to start working, but said that he, not having the money, would like to borrow it from us, and in return would give us a proper proportion of the profits. We agreed to this, and he prepared some vouchers which ran as follows:

and handed one to each of us on payment of $£ 100$. We then held $£ 100$ of the Dye Scheme "Stock," and the voucher was our receipt and our title to a share of the profits as well.
352. Let us now imagine that a year has passed, and that we each get $£ 20$ out of the profits, and then, after another year, £21. Smith's Iyy Scheme is a paying concern, and the dividends, of $£ 20$ and $£ 21$, are good. A friend of mine gets to hear that I have one of Smith's vouchers, and he wants to buy it, while I happen to want some ready money to buy a motor-car, so I agree to sell it to him for $£ 106$. If the business had not paid well, I might have been glad to sell the voucher whose face value is $£ 100$ for $£ 90$, or even for $£ 9 .{ }^{1}$

In this imaginary episode you have the whole run of stocks, and, we might add, that two men might have each bought $£ 50$ worth of my stock and then they would have received half the dividend each.
353. Now consider the following:

On going into a grocer's shop we can buy 1 lb . or $\frac{1}{2} \mathrm{lb}$. of coffec and have it weighed up and put in a small parcel while we wait, or we can buy a $1-\mathrm{lb}$. or $\frac{1}{2} \cdot \mathrm{lb}$. tin. In the same way we might buy 2 oz. of tea and have it weighed up and put into a bag, or we could have a $1-\mathrm{lb}$. or $\frac{1}{2} \mathrm{lb}$. packet of tea, but we could not have $\frac{1}{2} \mathrm{lb}$. of coffee out of a $1-\mathrm{lb}$. tin, nor 2 oz . of tea from a $\frac{1}{4}-\mathrm{lb}$. packet, for the grocer would not break the tin or the packet.

So it is with stocks and shares.
Stocks are as the coffee or tea which can be bought in bulk, $2 \mathrm{oz} ., 5 \mathrm{oz} ., 18 \mathrm{oz}$., or any amount, for you can buy any amount of stock, e.g. $£ 5, £ 6815 \mathrm{~s} .8 \mathrm{~d} ., £ 123419 \mathrm{~s} .6 \mathrm{~d}$.

Shares are as the coffee, etc., bought in tins or in packets, which cannot be broken up, and you can buy only a complete number of them. If, for example, each share be worth 10 s ., then you could not get 15 s . worth of shares, for 10 s . would buy one and $£ 1$ two, while 15 s. would buy one and give you 5 s. change, not half a share.

We now apply our elementary notions to the general case.
354. Business houses, or railway companies, or Governments, can prepare vouchers just as Smith did, which can be bought and

[^46]sold, sometimes at their face value, at other times a good deal above or below it.

Take the case of a Government which wants money for war purposes ; it will advertise half a million $£ 100$ vouchers for sale at $£ 99$ each. If the Government is a good one, people will buy up the vouchers as quickly as possible and receive a guaranteed amount or Dividend every quarter, half-year, or year, as the case may be. (See Plate XVl., p. 496.)

The face value of all the vouchers sold is called the Stock of the Government, and the holder of a $£ 100$ voucher is said to have £100 stock.

In raising the Great War Loan of June 1915 the Government issued 5s. and 10 s. vouchers which could be bought at any Post Office. We give a facsimile of one on opposite page.
355. Sometimes vouchers must he handed back to the Government at the end of a period of years, when the face value will be paid for them, but they can be bought and sold just as we please in the interim. When the stock is bought back by the Covernment it is said to be Redeemed.

If, having bought a voucher, we keep it, then it provides a regular income of $£ 3$ or $£ 4$ a year until we feel disposed to sell it. If, however, we had bought a railway company's voucher, then the dividend upon it might have been much higher, perhaps $£ 10$ or $£ 12$, but this and the marketable value of the voucher itself depend entirely on the prosperity of the company and the consequent demand for its vouchers. As we have said, the face value of a voucher, even when it is first issued, is not necessarily its cash value. For example, the face value of the following is £100, but their price when issued was:

Queensland Government 41 $\%$ Loan, ${ }^{1}$ £99; Great War Loan, $3 \frac{1}{2} \%, £ 95$; East India Railway Co., $4 \frac{1}{2} \%, £ 99$ : Argentine $6 \%$ Bonds, ${ }^{2} £ 99$. We pay, therefore, $£ 95$ for a $£ 100$ War Loan voucher and $£ 99$ for the others.
356. A voucher has then-(1) a face value; (2) a price of issue; and (3) a marketable value; and the last can always be ascertained from the newspapers.

[^47]

Thus, to-day ${ }^{1}$ we find the price of a $£ 100$ voucher in the fous concerns named is: (1) London and North-Western Railway, £1123 ${ }^{\frac{3}{4}}$; (2) Bank of England, £242; (3) New Zealand $4 \%$, $£ 96 \frac{5}{5}$; (4) London, Chatham, and Dover Railway, $£ 67$.

When the price is above £100, as in (1) and (2), the stock is said to be at a Premium ; when £100, at Par; and when below $£ 100$, at a Discount, as in (3) and (4). Note that (1) is at a Premium of $12 \frac{3}{4} \%$, but (4) is at a Discount of $33 \%$.

35\%. It is then most important to distinguish between $£ 100$ stock and $£ 100$ cash. The former may have any value whatever and the $£ 100$ voucher may be worth (e.g.) $£ 1000$ or nothing at all ; but $£ 100$ cash is a perfectly definite amount of money, and in any question the student should be careful to decide whether $£ 500$ means $£ 500$ stock or $£ 500$ cash. The word "voucher" can always be put for "stock" but not for "cash."
358. In considering the dividend we have really to ask just one question. Shall we be content with a small dividend if the money we put into the concern is safe, or are we ready to risk all we put in for the sake of a high dividend? The former is the wiser, the latter the more attractive course. Companies cater for both classes by issuing different kinds of stock, which are:
(a) Debenture Stock. -The vouchers for this are issued on the understanding that a definite dividend will be paid, or, failing that, the holders can, if necessary, take the buildings, land, and plant of the company and dispose of them to get back their money and to pay their dividends. Debenture Stock is then absolutely safe, and the dividend is usually lower than that declared on
(b) Preference Stock.-On these vouchers a fixed dividend is paid after that due on (a) has been met, and a Cumulative Preference Stock is one upon which the dividend, if it cannot be paid in any one year because of bad business, must be paid even though it is not for five years to come. So that if you had a Cumulative Preference voucher at $5 \%$ and the dividend was not paid for 3 years, and in the fourth year things went well, the company might pay you not only $£ 5$ for that year, but also $£ 15$ arrears, or at any rate a part of that $£ 15$, and you would be paid in full before the holders of
(c) Ordinary Stock were paid at all. Holders of these vouchers have what remains when (a) and (b) have had their due, but very often (c) draws a dividend of $8 \%$, against (b) $5 \%$ and (a)

[^48]$4 \%$. If, however, the company lost, then (c) would get no dividend at all, (b) might get a little, but (a) is quite certain to be paid.
359. If you wish to buy or to sell stock it is necessary to go to a broker ${ }^{\mathbf{1}}$ and tell him that you want $£ 100$ stock in the Great Western Railway-that is, $£ 100$ worth of the capital of that company. He then meets his Jobber, and they inform you of the price to be paid, and that is determined
(1) By the amount of stock on the market for sale; and
(2) By the prosperity of the company, which, of course, influences condition (1).
The jobber would perhaps want $£ 105 \frac{3}{4}$ for $£ 100$ stock, and, on paying that amount of money, together with the cost of stamps, etc., you would hold $£ 100$, Not $£ 105 \frac{3}{4}$, Great Western Railway Stock. In precisely the same way you could sell $£ 100$ stock in the P. and O. Company and receive perhaps $£ 288$ for it.
360. The jobber always quotes two prices, e.g. Irish Land, $78 \frac{1}{4}$ to $78 \frac{3}{4}$, which means that all who buy from him must pay $78 \frac{3}{4}$, and all who sell to him will get $78 \frac{1}{4}$. If then he sells $£ 100$ stock for one client and buys the same amount for another, he pays the first $£ 78 \frac{1}{4}$ and takes $£ 78 \frac{3}{4}$ from the second, and makes $£ \frac{1}{2}$, i.e. 10s. profit, which is called the "Jobber's Turn."
361. The broker usually adds on one-eighth to the buying price and so charges his client $78 \frac{3}{4}+\frac{1}{8}=78 \frac{7}{8}$, and deducts oneeighth from the price at which he sells for him, namely, $78 \frac{1}{4}-\frac{1}{8}$, or $78 \frac{1}{8}$. The public therefore really buy at $78 \frac{7}{8}$ and sell at $78 \frac{1}{8}$, while the broker and jobber flourish on the difference.

Hence we have the following rule:
In buying add one-eighth to the Buying Price. In selling subtract one-eighth from the Selling Price, to allow for the brokerage (Section XVIII. B. II.) paid to the broker.
362. We have pointed out that the price of stock may vary, ${ }^{2}$ and in some cases it must be said that the fluctuations are very

[^49]great. This being so, it is clear that if one can anticipate a particular change and buy in or sell out quickly, it is possible to make a great deal of money in an hour or a day, while it is just as likely, and, among the uninitiated, practically certain, that one may be ruined by a wild speculation. In the case of Government and railway stocks, however, people usually buy with the intention of allowing their money to remain and produce a certain annuity upon which they may live, and hence it is important to know what Dividend is to be paid. (See Plate XVI., p. 496, where a space is left for the signature of the payee when he pays the warrant into his bank.)
363. In considering the income we shall derive from any "investment," or purchase of vouchers, we find from our newspapers that:
(1) Metropolitan $3 \frac{1}{2} \%$ Stock stands at 95 ;
(2) Union of South Africa $4 \%$ Stock stands at 94 ;
(3) Brazilian $5 \%$ Stock stands at 63 ;
(4) Italian $3 \frac{1}{2} \%$ Stock stands at 73 ;
(5) Russian $4 \%$ Stock stands at $80 \frac{1}{2}$;
(6) New South Wales $4 \frac{1}{2} \%$ Bonds at $101 \frac{1}{2}$;
and all but the last are at a discount.
In (1) every $£ 95$ paid produces $£ 3 \frac{1}{2}$ interest; in (2) every $£ 94$ paid produces $£ 4$ interest; in (3) every $£ 63$ paid produces $£ 5$ interest; in (4) every $£ 73$ paid produces $£ 3 \frac{1}{2}$ interest; in (5) every $£ 80 \frac{1}{2}$ paid produces $£ 4$ interest; in (6) every $£ 101 \frac{1}{2}$ paid produces $£ 4 \frac{1}{2}$ interest.
364. At first sight it would seem best to invest in (3), for it gives $£ 5$ on $£ 63$, but if Brazil has to pay $5 \%$ to get money, and other Governments canget it at $3 \frac{1}{2} \%$, or, in the case of the British Government, at $2 \frac{3}{4} \%$, then Brazil commands less confidence than the others do. We might say, in general, that if a Government has to offer a high rate of interest to get money, then it is not likely to prove a sound depository for one's money.

Some Governments have found it impossible to pay back the capital borrowed and have often not even paid the interest. In buying, then :
(1) Choose a stable Government and one not likely to be overthrown (as some in Central and South America have been) by a ring of financiers.
(2) Buy at a low price if possible.
(3) Do not look for high rates of interest, for they are usually inversely proportional to stability.
365. In so far as the first point is concerned, British Government stock is perfectly secure. It originated under William in., when a great deal of money was borrowed for war purposes, and when our national debt assumed large proportions, quickly running up to $£ 16,000,000$. The American War added $£ 121,000,000$, the French wars of Nelson and Wellington $£ 600,000,000$, although in times of peace some was paid off by means of taxation and of money specially set apart for the purpose; the loan itself was called "The Funds." Between 1910 and 1912 no less than $£ 51,000,000$ was paid off, while the War Loan of 1915 added $£ 350,000,000$ at one stroke.

The Government originally paid $£ 3$ per annum ${ }^{1}$ on every $£ 100$ voucher, which, in fact, could be bought for as little as $£ 60$ in the early nineteenth century, and so the position was really this: the Government offered an annuity of $£ 3$ a year, and people were ready to pay $£ 60$ for that annuity, hence the loan became called "The Consolidated Annuities," or, shortly, "Consols," dividends on which are paid at the Bank of England quarterly on the 5th of January, April, July, and October.
366. The debt of the Government is divided into :
(a) The Funded Debt, which it need not pay off, although it may do so, and must of course pay the dividend; and
(b) The Unfunded Debt, which consists of loans for short periods which the Government must pay off on a specified date.

The French Government Stock is called "Rentes." ${ }^{2}$
367. Example 1.-What must be paid to-day for $£ 300$ stock in the Transvaal 3 per Cents?

The financial column in our newspaper shows that the stock is at $£ 88$-that is to say, a $£ 100$ voucher costs $£ 88$.
$\therefore$ a $£ 300$ voucher costs $£ 264$.

## Example 2.-What annual income will the last investment produce, and what per cent. return on the cash paid?

1. Income $=£ 3$ on every $£ 100$ stock
$\therefore$ income $=£ 3 \times 3=£ 9$.
2. Income is $£ 9$ for expenditure of $£ 264$
$\therefore$ income is $£ \frac{9}{264} \times 100$ for expenditure of $£ 100$.
Income is at the rate of $3.41 \%$ (nearly).
[^50]Example 3.-How much India 3 \% stock at 691 can be bought for $£ 834$ ?
$£ 69 \frac{1}{2}$ cash will buy one $£ 100$ voucher.
$\therefore £ 834$ cash will buy $£ \frac{100}{69 \frac{1}{2}} \times 834$ worth of vouchers
$=£ 1200$ worth of vouchers or stock.
Example 4.-What income will be derived from investing £1140 in the Birmingham $3 \%$ stock at 76, and £2020 in the Queensland $4 \frac{1}{2} \%$ at 101 ? Which of these two investments pays the better?

1. (a) $£ 76$ produces $£ 3$ income
$\therefore £ 1140$ produces $£ \frac{3 \times 1140}{76}$ income
$=£ 45$ income.
(b) $£ 101$ produces $£ 4 \frac{1}{2}$ income
$\begin{aligned} \therefore £ 2020 \text { produces } & £ \frac{4 \frac{3}{2} \times 2020}{101} \\ = & £ 90 \text { income }\end{aligned}$
$\therefore$ total income $=£ 135$.
2. $£ 76$ produces $£ 3$ income in the Birmingham stock
$\therefore £ 101$ produces $£ \frac{101 \times 3}{76}$ income in the Birmingham stock

$$
=£ 4 \text { very nearly ; }
$$

and $£ 101$ produces $£ 4 \frac{1}{2}$ in the Queensland stock,
$\therefore$ the latter is the more remunerative.

## EXAMPLES. LXXIX. (a)

1. Explain clearly the difference between "stocks" and "shares."
2. What difference is there in meaning between "the price of issue," "the face value," and "the cash value" of stock?
3. What is meant by (a) consols, (b) bonds, (c) redeemable in 50 years at par, (d) "at a discount," (e) "at a premium," $(f)$ Debenture Stock, ( $g$ ) Preference Stock, ( $h$ ) Cumulative Preference Stock?
4. What is the difference between a jobber and a broker? How do they make a living out of stocks and shares?
5. What do you mean by the Funded and Unfunded Debts of the Government?

What must be paid for the following (Questions 6 to 15):
6. $£ 300$ stock at 50 ?
7. £500 stock at 67 ?
8. £800 stock at $72 \frac{1}{2}$ ?
9. $£ 1000$ stock at 120 ?
10. $£ 760$ stock at $80 \frac{1}{4}$ ?
11. £325 stock at 75 ?
12. £586 stock at 60 ?
13. $£ 75610$ s. stock at 80 ?
14. £848 12s. stock at $70 \frac{1}{2}$ ?
15. $£ 535010$ s. stock at $66 \frac{1}{4}$ ?

How much of the following priced stocks can be bought for the cash stated (Questions 16 to 25):
16. Cash £525, stock at 75 ?
17. Cash $£ 836$, stock at 66 ?
18. Cash £850, stock at $65 \frac{1}{2}$ ?
19. Cash $£ 1360$, stock at 8 万̃ ?
20. Cash £1639, stock at 99 ?
21. Cash £3069, stock at 851 ?
22. Cash $£ 5130$, stock at 95 ?
23. Cash $£ 3105$, stock at $86 \frac{1}{4}$ ?
24. Cash £ 1256 , stock at $78 \frac{1}{2}$ ?
25. Cash £2796, stock at $58 \frac{1}{4}$ ?

Disregard brokerage in Questions 26 to 76.
26. What must be paid for $£ 600$ worth of Bristol $3 \%$ stock at 76 ?
27. What is the cash value of $£ 1000$ worth of Victoria $3 \frac{1}{2} \%$ at $91 \frac{1}{4}$ ?
28. How much should be paid for $£ 1030$ London and Brighton at 86 ?
29. How much would you offer a client for $£ 32006 \%$ Underground Electric at $80 \frac{1}{2}$ ?
30. What shall I accept for $£ 2500$ Louisville (American Railroads) at 125?
31. A jobber offers my broker 500 Southern Pacific for £46025. Shall I accept? (The market price is 92.)
32. What will you take for $£ 700$ Grand Trunk (Canada) at 65 ?
33. How much Bank of Ireland stock at $£ 240$ can be bought for $£ 2880$ ?
34. What amount of Consols can be bought for $£ 5320$ if the price is $66 \frac{1}{2}$ ?
35. What amount of Caledonian at 60 can be bought for £21360?
36. How much Illinois Central at 114 can be bought for £4104?
37. What amount of South Australian $4 \%$ at 95 can be bought for $£ 1140$ ?
38. What value of Uruguay $3 \frac{1}{2} \%$ at 64 can be bought for £2048?
39. What is the percentage return on Spanish $4 \%$ at 84 ?

X40. What return per cent. is yielded by Portuguese $3 \frac{1}{2} \%$ at 54 ?
41. What percentage return is yielded (I.) by $2 \frac{1}{2} \%$ Consols at the following prices: (1) £89 16s. 3d. ; (2) £88 6s. 3d.; (3) $£ 842 \mathrm{~s} .6 \mathrm{~d} . ;(4) £ 86 \mathrm{ls} .3 \mathrm{~d} . ;$ (5) $£ 8317 \mathrm{~s} .6 \mathrm{~d} . ;(6) £ 796 \mathrm{~s} .3 \mathrm{~d} . ?$ and (II.) by $2 \frac{3}{4} \%$ Consols at the following prices: (7) £95 15s. ; (8) £110 15s. ; (9) £94 7s. 6d.; (10) £110 18s. 9d ; (11) $£ 10617 \mathrm{~s} .6 \mathrm{~d} . ;$ (12) £99 12s. 6d.?
*42. Which of the following is at a premium and which at a discount: Bengal Railway, 145 ; Buenos Ayres Railway, $96 \frac{1}{4}$; Canadian Pacific Railway, $164 \frac{1}{2}$; Chilian $4 \%$ stock, 74 ; 1'eruvian stock, 90 ; San Paulo Railway, 192 ?
+43. How much does £1182 invested in the Cuban $5 \%$ Bonds at $98 \frac{1}{2}$ yield per annum?
44. What percentage return does the Chinese $5 \%$ at 80 yield?
$\$ 45$. Which pays the higher rate per cent. : the Japan $4 \frac{1}{2} \%$ at $86 \frac{1}{2}$, or the $5 \%$ at 91 ?
46. What yield per cent. is obtained from the Mexican $5 \%$ at $54 \frac{1}{2}$ ?
447 . What must be the price of Consols to yield at $2 \frac{1}{2} \%$ the same as the Mexicans of the last question yield at $5 \%$ ?

What income will the following investments yield :
48. £5000 in the 3 per Cents at 60 ?
49. $£ 860$ in the $3 \frac{1}{2}$ per Cents at 43 ?
50. £1584 in the $2 \frac{1}{2}$ per Cents at 66 ?
51. $£ 91310 \mathrm{~s}$. in the $3 \frac{1}{4}$ per Cents at $72 \frac{1}{2}$ ?
52. $£ 2600$ in the 4 per Cents at $81 \frac{1}{4}$ ?
53. $£ 3615 \mathrm{~s}$. in the 5 per Cents at $73 \frac{1}{2}$ ?
54. $£ 2988$ in the $4 \frac{1}{2}$ per Cents at $62 \frac{1}{4}$ ?
55. £2431 in the $2_{4}^{3}$ per Cents at $110 \frac{1}{2}$ ?
56. $£ 240$ 10s. in the $4 \frac{1}{4}$ per Cents at $120 \frac{1}{4}$ ?
57. $£ 148210$ s. in the $5 \frac{1}{4}$ per Cents at $148 \frac{1}{4}$ ?

What income will be derived from the following holdings:
58. $£ 3000$ stock in the 4 per Cents?
59. $£ 5860$ stock in the $3 \frac{1}{2}$ per Cents?
60. $£ 7382$ stock in the $2 \frac{1}{4}$ per Cents?
61. $£ 655810$ s. stock in the $3 \frac{1}{4}$ per Cents?
62. £821 13s. 4 d. stock in the $4 \frac{3}{4}$ per Cents?
63. $£ 5766 \mathrm{~s} .8$ d. stock in the $5 \frac{1}{4}$ per Cents?
64. £386 15s. stock in the $2 \frac{3}{4}$ per Cents ?
65. £536 17s. 6d. stock in the $3 \frac{1}{2}$ per Cents?
66. $£ 25015 \mathrm{~s}$. stock in the $2 \frac{1}{2}$ per Cents?
67. $£ 360$ 18s. stock in the $3 \frac{1}{2}$ per Cents?
68. $£ 48513 \mathrm{~s} .6$ d. stock in the $4 \frac{1}{4}$ per Cents?
$\checkmark$ 69. How much must be invested in the Belgian $3 \%$ at 67 to produce an income of $£ 240$ per annum?
$\checkmark 70$. What income will be derived from $£ 134257$ 10s. invested in the Grand Trunk Canada $5 \frac{1}{2} \%$ at $101 \frac{1}{4} ?$
$\checkmark 71$. I have a certain sum of money to invest. Which of the following would you recommend as producing the highest income: Canada $4 \%$ at $94 \frac{1}{2}$; Natal $3 \%$ at $75 \frac{1}{2}$; West Australia $3 \frac{1}{2} \%$ at 82 ?
$\sqrt{\circ} 2$. What half-yearly dividend will be derived by investing $£ 1000$ in the $3 \%$ stock at 66 ?
73. What quarterly dividend will be obtained by a holding of $£ 5000$ stock in the 4 per Cents?

74 . What income will be derived in 10 years from an investment of $£ 1400$ in the Japan $4 \frac{1}{2} \%$ at $87 \frac{1}{2}$ ?
75. The trustees for a merchant's estate invested money as follows: £554 8s. in $2 \frac{1}{2} \%$ Consols at $66 ; £ 1805$ in $3 \%$ Exchequer Bonds at $95 ; £ 10647$ in $3 \%$ Local Loans at 78; $£ 8748$ in $3 \frac{1}{2} \%$ India at 81 . What income was derived from these investments?
76. If $£ 237276$ be invested in the $3 \%$ Local Loans at 78, and $£ 68921$ in the $3 \frac{1}{2} \%$ India at 82 , calculate the net income obtained after deducting income-tax at 1 s .2 d . in the pound.
368. Example 1.-The prices quoted for South Australian $3 \%$ are $70 \frac{1}{8}$ to $70 \frac{7}{18}$, and for Johannesburg $4 \%, 86 \frac{1}{4}$ to $86 \frac{3}{8}$. Allowing brokerage at $\frac{1}{8} \%$, calculate the amount to be paid for $£ 1600$ stock in the former, and the amount derived from selling $£ 2400$ stock in the latter.

1. We buy Australian and have to pay $70 \frac{7}{18}$ to the jobber for $£ 100$ stock ; add to this $\frac{1}{8}$, and then the cost becomes $70 \frac{9}{18}$;
$\therefore £ 70 \frac{9}{18}$ has to be paid for $£ 100$ stock ;
$\therefore £ 70 \frac{9}{18} \times \frac{1600}{100}$ has to be paid for $£ 1600$ stock ;
$\therefore$ cost required $=£ \frac{1129}{16} \times \frac{1600}{100}=£ 1129$.
2. For every $£ 100$ stock sold, the jobber pays the broker $£ 86 \frac{1}{4}$ and the broker pays the seller $£ 86 \frac{1}{4}-\frac{1}{8}=£ 86 \frac{1}{8}$;
$\therefore £ 100$ stock brings in $£ 86 \frac{1}{8}$,


## EXAMPLES. LXXIX (b).

1. Fill in the following table:

|  | Name of Stock. | Closing Prices. | Jobber's Turn. | Broker's Price to a Client |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | for Selling. | for Buying. |
|  |  | $\boldsymbol{£}$ £ |  |  |  |
| (1) | London County $3 \frac{1}{2} \%$. | 88 to $88 \frac{1}{2}$ |  |  |  |
| (2) | War Loau . | 94 ,, $94 \frac{1}{5}$ |  |  |  |
| (3) | Metropolitan $3 \frac{1}{2} \%$ | $95 \frac{1}{2},{ }^{65 \%}$ |  |  |  |
| (4) | Port of London $3 \%$ | $69 \frac{1}{2}$, $70 \frac{1}{8}$ |  |  |  |
| (5) | Leeds 21 \% | $63 \frac{1}{4}, 64 \frac{1}{8}$ |  |  |  |
| (6) | Mersey Dock 31 \% | $83 \frac{1}{4}$,, $83 \frac{5}{8}$ |  |  |  |
| (7) | Johannesburg 4 \% \% | $86 \frac{1}{4},{ }^{\text {c }}$ 86 ${ }^{\frac{3}{8}}$ |  |  |  |
| (8) | South Australian 3 \% | $70 \frac{1}{8},{ }^{\text {, }} 70{ }_{1}{ }^{\frac{7}{8}}$ |  |  |  |

What amount would be obtained by selling :
2. $£ 560$ stock at $75 \frac{3}{8}$; brokerage, $\frac{1}{8} \%$ ?
3. $£ 485$ stock at $82 \frac{5}{8}$; brokerage, $\frac{1}{8} \%$ ?
4. £575 stock at $78 \frac{7}{8}$; brokerage $\frac{1}{8} \%$ ?
5. £980 stock at $125 \frac{3}{4}$; brokerage, $\frac{1}{4} \%$ ?
6. $£ 1000$ stock at $156 \frac{1}{4}$; brokerage, $\frac{1}{4} \%$ ?
7. $£ 750$ stock at $175 \frac{1}{8}$; brokerage, $\frac{1}{8} \%$ ?

How much stock at the prices given can be bought for the sums stated:
8. Cash, $£ 5000$ stock at $85 \frac{1}{4}$; brokerage, $\frac{1}{8} \%$ ?
9. Cash, $£ 4850$ stock at $75 \frac{1}{2}$; brokerage, $\frac{1}{4} \%$ ?
10. Cash, $£ 455$ stock at $68 \frac{1}{4}$; brokerage, $\frac{1}{8} \%$ ?
11. Cash, $£ 385$ stock at $120 \frac{1}{2}$; brokerage, $2 \mathrm{~s} .6 \mathrm{~d} . \%$ ?
12. Cash, $£ 755$ stock at $150 \frac{1}{4}$; brokerage, $2 \mathrm{~s} .6 \mathrm{~d} . \%$ ?
13. Cash, $£ 853$ stock at $160 \frac{7}{8}$; brokerage, $2 \mathrm{~s} .6 \mathrm{~d} . \%$ ?

Allow brokerage of $\frac{1}{8} \%$ in the following transactions, taking the prices from Question 1:
14. What must I pay for $£ 6381$ of London County stock ?
15. A merchant sold $£ 2680$ of Johannesburg stock; what cash payment did he receive from his broker?
16. A jobber bought $£ 3750$ Port of London yesterday and sold them this morning. What profit did he make?
17. What does a broker make by buying and selling $£ 50000$ of South Australian $3 \%$ ?
18. What would you expect to pay your broker for buying £5000 War Loan stock?
19. What would a broker make in buying and selling $£ 6500$ Leeds $2 \frac{1}{2} \%$ stock?
20. How much Mersey Dock $3 \frac{1}{2}$ \% should be bought for $£ 75315 \mathrm{~s}$. cash ?
21. If you put 5620 guineas into the Port of London $3 \%$ stock, what income would you get?
22. What would have to be the price of Metropolitan $3 \frac{1}{2} \%$ to give the same income as the Port of London (Question 21)?
23. If my firm bought $£ 3500$ London County stock when it stood at $86-86 \frac{1}{4}$ and sold it at $88-88 \frac{1}{2}$, what profit was made? (Ignore brokerage.)

## B. Shares

369. Let us suppose that we are in a town in the Provinces where there is no electric light, and that Mr. Wells is an enterprising business man who sees what advantages would accrue to the town by having electric light. He has not enough money himself to embark upon the undertaking, and he may therefore do one of three things:
370. He may get a number of friends to combine with him ${ }^{1}$ and enter into Partnership, so that they supply the money and divide the profits among them. ${ }^{2}$

He may also allow people, other than the partners, to put money into the business, for which they may receive a dividend; and if such people exercise no control whatever in the management of the affairs, then the business is said to be a Limited Partnership. The term "limited" is used in the same sense as in § 372 .
2. He may form a Private Company with one of his friends or with more if he likes, but they must not appeal to the public in general to lend them money, nor need they make their affairs public in any way, although the company must be registered. This method of procedure would be excellent if Mr. Wells had a brother, or immediate relatives, who would subscribe and so keep the concern "in the family."
3. He may prepare a statement or prospectus showing the pros and cons of the case, drawing attention to the advantages, and so on, and then he, in company with six others, could float a Public Company, send out the prospectus, advertise in the newspapers, and so get people to lend money to erect a generating station, purchase alternators and plant in general, and then receive a share of the profits in due course. (See also § 372.)

[^51]370. Let us suppose that $£ 100000$ is necessary for the undertaking. This amount will be divided into, say, $1000 £ 10$ $5 \%$ Debenture Shares; ${ }^{1} 3000 £ 5,6 \%$ Preference Shares; and $75000 £ 1$ Ordinary Shares. Mr. Wells will probably become managing director, and he will place his friends in suitable positions, appoint bankers, auditors, a secretary, and others, who will probably take up some shares in the company.
371. Now let us see what the issuing of shares means. There are in all 79000 shares, and so 79000 vouchers will be prepared and numbered consecutively. These vouchers will say, for example:


## £5 PREFRRENCE SHARE.

## No. 3005.

Hrld $\mathrm{by}^{\prime}$
Sir Charles mariowe.

It is clear that Mr. Wells might hold Debenture shares 1-10; Preference shares 3100-4200; and Ordinary shares 8000-9000, but he could not hold $1 \frac{1}{2}$ Debenture shares, for, as we have said, the shares are as packets of tea and one cannot buy half a packet. Shares, we repeat, are sold in whole numbers, but stock in any amount (§ 353).

Facing this page we give a facsimile share certificate (Plate XV.).
372. When the public have bought up all the vouchers ${ }^{2}$ that are for sale, and the directors-that is, Mr. Wells and his friends-have the money, then they proceed to spend the same and endeavour to make the concern pay. If all goes well, the Debenture holders will get $£ 5 \%$ on the face value of each voucher they have, the Preference holders $£ 6 \%$ perhaps, and the Ordinary holders perhaps $£ 10 \%$. If things go badly, the first will still

[^52]get $£ 5 \%$, the second may get something, and the third nothing. If business goes from bad to worse, the Debenture holders may sell the generating station and everything else, reimburse themselves, and hand over the balance, if there is any, to the Preference holders, who then take their due, and finally the Ordinary holders may have to console themselves with just as much money as the cats did cheese in the fable. Be that as it may, if the assets are not enough to meet the liabilities the creditors have to bear the loss, and they cannot call upon the shareholders to advance any more money than they have paid for their shares, so that their liability to pay is limited to the amount they have subscribed. Thus, if you had bought 40 Ordinary vouchers you might lose the amount you paid, namely, $£ 40$, but you could not lose more. Such a company as this is called a Limited Liability Company. Many of the large firms of to-day have merged from partnerships or private companies into limited companies, and if one puts his money into them he is at any rate sure of the extent of his responsibility.
373. The method of buying shares is just the same as that employed in the case of stock, except that the broker usually charges 3d. or 6d. a share and not $\frac{1}{8} \stackrel{\prime}{\circ}$.

The face value of share vouchers is usually low, perhaps 2 s . 6 d., $£ 1$, or $£ 5$, and their cash or marketable value ${ }^{1}$ may be anything at all; we find out what it is on any day from the newspapers.

## EXAMPLES. LXXX.

1. Explain some methods by which a merchant may raise money to extend his business.
2. Would you expect Preference or Ordinary shares to earn the higher dividend? Give reasons.
3. What shares are (a) the surest and (b) most remunerative so long as the business is prosperous?
4. Distinguish between "Authorised Capital" and "Paid-up Capital."
5. What privileges have the Debenture holders of a company if it fails ?
6. What is meant by a Limited Liability Company?
7. What is the capital of a company which has issued 100000 five-shilling shares?
${ }^{1}$ See also Whitaker's Almanack, p. 356, for price of issue of shares of the great Banks and also for their marketable value.
8. How much capital would 5000 £5 Preference shares and $10000 £ 2$ Ordinary shares produce?
9. How many shares of 30 s. must be taken up to raise $£ 60000$ capital?
10. What capital do 5000012 s .6 d . shares produce?
11. A company is floated with 500 Debenture shares of $£ 5$ each, 800 Preference shares of $£ 3$ each, and 10000 Ordinary shares of £l each. What is its capital?
12. A company issues 3500 Debenture shares of $£ 6$ each, 2300 Preference shares of $£ 5$ each, and 10000 Ordinary shares of $£ 1$ each. What is its capital?
13. Distinguish between Stock and Shares.
14. If in Question $12 £ 3$ has been paid up on the $£ 6$ shares, $£ 2$ on the $£ 5$, and 10 s. on the $£ 1$, to how much does the paid-up capital amount?
15. A company intends to issue 300 Debenture shares at $£ 30$ each ; how many Ordinary $£ 5$ shares must it issue as well to raise £20000 capital?
16. The capital of a company amounts to $£ 100000$, of which part is in Ordinary shares of $£ 10$ each and part in 3000 Preference shares of $£ 20$ each. How many Ordinary shares were issued?
17. The ratio of the number of $£ 3$ Preference shares to $£ 1$ Ordinary shares in a company was $2: 9$, and there were 20403 of the latter. Calculate the capital of the company.
18. It is proposed to raise $£ 1,000,000$ partly in $£ 60$ Debenture shares, partly in $£ 40$ Preference shares, and the balance in £10 Ordinary shares. If there are 200 of the first and 4000 of the second, what capital was raised by the Ordinary shares, and how many of them were issued?
19. If there had been $£ 20$ paid up on the Debenture shares of the last question, $£ 30$ on the Preference, and $£ 5$ on the Ordinary, by how much would the paid-up capital have been less than the total provided for?

Ignore brokerage in Questions 20 to 46 :
20. How much ought my broker to charge for 90 London County and Westminster Bank shares at $£ 19$ ?
21. What will you offer for 500 shares in the London-Asiatic Rubber Company at 6s. 6d.?
22. What should be offered for 76 Vickers at 35 s .?
23. What must be paid for 60 Anglo-American Tobacco at £225 ${ }^{5}$ ?
24. What will be left out of $£ 100$ after purchasing as many British South Africans at $£ 2 \begin{aligned} & \text { E } \\ & 8\end{aligned}$ as possible?
25. What will 1500 Bovril at 21s. 6 d . cost me?
26. If you sell 550 Bradford Dyers at a guinea, and buy as many Calico Printers as you can at 6 s . $7 \frac{1}{2} \mathrm{~d}$., how many of the latter can you get, and what cash will be left over?
27. If a merchant bought 350 Coats at $£ 5 \frac{1}{15}$ y yesterday and sold them all to-day at $£ 6$, what profit did he make?
28. What will 500 Dunlop Ordinary cost at 44 s .?
29. How many Hudson's Bay at $£ 6 \frac{9}{16}$ can be bought for £100?
30. If one-third of the shares in Question 29 are sold at $£ 7$ and the remainder at $£ 6 \frac{3}{3}$, what profit or loss is made by the transaction?
31. What difference is there in cost between 560 Aerated Bread at £37 and 640 British South Africans at $£ 2 \frac{5}{8}$ ?
32. How many Marconi Wireless at 33s. 6d. can be bought for $£ 1005$ ?
33. How many Rubber shares at 73 can be bought for $£ 1825$ ?
34. What number of Maypole Dairy shares at 25 s . can be bought for $£ 1950$ ?

35 . How much will be left out of $£ 27$ if the greatest number of $£ 1$ shares in Bovril at 21s 6 d . be purchased?
36. What profit would be made by selling the shares of the last question at 22 s . each?
37. What would you pay for $500 £ 1$ shares in ArmstrongWhitworth at par?
38. What would the shares of the previous question cost at a premium of $10 \%$ ?
39. What would you make by buying $300 £ 10$ Nobel Dynamite at par and selling at $£ 16$ ?
40. If the Aerated Bread $£ 1$ shares stand at $£ 37$, what is the premium?
41. If Lipton $£ 1$ shares are on sale at 16 s . 2d., at what discount do they stand?
42. What loss would be sustained if one had bought 750 Liptons at par and sold them at 16 s . 2 d . ?
43. What income will 1000 Bovril $£ 1$ shares bring in if the dividend is $7 \%$ ?
44. If we buy $£ 105$ worth of Harrod's shares and the dividend is $29 \%$, what income will be obtained if the shares are at par?
45. What income will be derived from 760 ten-shilling shares if the dividend be $15 \%$ ?
46. What income will be obtained by investing $£ 500$ in $5 \%$ shares at $£ 15$ ?
47. Draw up and then fill in the following table, allowing in (1), (2), (3), (6), and (7), 1s. 3d. ; in (4) and (5), 3d. ; and in (8), 1d. per share for brokerage :

|  | Name of Share. | Closing Prices. |  | Broker's Price to his Client |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | for Selling. | for Buying. |
| (1) | Barclay's Bank | $£ 121.1$ |  |  |  |
| (2) | Parr's Bank | £36 $\frac{1}{4}$ to $£ 36$ 5 |  |  |  |
| (3) | Burma (Oil) | $£ 4_{1}{ }^{3} \mathbf{6}$ to $£ 4{ }^{7}{ }^{7}$ |  |  |  |
| (4) | Imperial Tobacco . | 25 s .3 d . to 25 s .9 d . |  |  |  |
| (5) | Anglo-Malay (Rubber) | 9 s . to 9s. 3d. |  |  |  |
| (6) | Royal Dutch (Oil) | £442 ${ }^{\text {do }}$ £443 |  |  |  |
| (7) | London and S. W. Bank |  |  |  |  |
| (8) | Van Den Berghs | 1s. 3 d . to 1 s . 4 d . |  |  |  |

Allow brokerage in each of the Questions 48 to 55, taking brokerage and prices from the last question :
48. What will you pay over to your client if you sell 1000 Parr's Bank shares for him?
49. What must you pay your broker if he buys 5000 Burma Oil for you?
50. For what amount should a cheque be drawn to purchase 5600 Anglo-Malays?
51. A merchant sells 650 Barclay's Bank shares; what cash payment does he get?
52. If the cash of the last question be put into South Australians (page 490), how much stock could be obtained?
53. James Williams, Esq., instructs his brokers, Dawson \& Sons, to buy for him 4500 Glencairn (South African) mining shares at 2 s .6 d . He encloses a cheque for $£ 750$ and knows that he must pay the broker 3d. a share for buying. Find (1) the amount paid for the shares ; (2) the amount paid to the broker ; and (3) draw a crossed cheque upon the Upton Bank (Messrs. Dawson \& Sons are the drawers and Mr. Williams the drawee) for the balance due to Mr. Williams.
54. What will be left out of $£ 1200$ after buying as many $£ 13 \frac{1}{2}$ shares in the London and South-Western Bank as possible, and what income do they produce if the dividend is $17 \%$ (the par value of the shares is £10)?
55. What do the jobber and broker make respectively by buying and selling 1500 Imperial Tobacco shares?

## REVISION QUESTIONS. III.

A. (1)

## SECTION XVII. A (1)

The student will do well to read through the book work in the various seetions before proceeding with these sets of Examples.

1. If I have to pay 5 s. for a piece of looking-glass 25 in. by 12 in., how much shall I have to pay for a piece 30 in . by 11 in ., if the price is proportional to the area?
2. A carpet 15 ft . by 9 ft . costs $£ 33 \mathrm{~s}$. ; what should be paid for one 18 ft . by 12 ft .6 in ., if the maker charges 6 d . per sq. yard more than the ratio of the areas would demand?
3. The ratio of the width of a field to the length is as $2 \frac{3}{4}: 6 \frac{3}{5}$. What is the area if the length is 150 yards?
4. A dairyman pays 25 men $£ 40$ a week in wages. His business increases and then he employs 36 men. What increase is there in his wages bill per week?
5. Three great companies contribute to the erection of a large educational institution. One company contributes as much as the other two together, and they contribute in the ratio of their total incomes, namely, $£ 58000$ and $£ 50000$. If the smallest contribution is $£ 1200$, what is the total amount by which education is indebted to the three companies?
6. There were 15640 felonies committed in London in 1911 and 15980 in 1912, the population being $7,321,420$ and $7,393,970$ respectively. Is the number of felonies per 1000 of the population increasing or decreasing?
7. The value of an engine depends on the time it has been in use, and its life is reckoned at 15 years. Calculate its value at the end of 5 years, of 8 years, and of 12 years, if it cost $£ 7500$ to begin with.
8. If a reaping-machine can reap 8 acres in $1 \frac{3}{4}$ day, how long would it take to reap $15 \frac{1}{4}$ acres if there were a breakdown taking 5 hours to repair? (Take $10 \frac{1}{2}$ hours $=1$ day.)
9. The value of a plantation in South America is greatest in the eighth year of its development, and it is then worth $£ 6000$ Its value in the ninth year bears to that in the eighth the ratio of $2: 3$, and its value in the fifteenth year bears to that in the eighth the ratio of $1: 100$. Find the average fall in value per annum between the ninth and fifteenth years.

## A. (2)

1. The value of the $3,007,040$ galls. of lubricating oil imported into South Africa in 1912-13 was £143760. What quantity was imported in 1913-14 if its value was $£ 150100$ ?
2. The value of the $1,528,000 \mathrm{lb}$. of glue imported into Canada from the United Kingdom was 109200 dollars last year. If that rate continued, what should be the value of the $1,539,000 \mathrm{lb}$. imported in the present year, and how much is the value obtained from the question greater or less than the actual value, 129000 dollars? Is the market improving or not?
3. The cost of providing electric light for the illumination of Southampton I)ocks (and all others too) depends on the candlepower (C.P.) of the lamps employed and also on the number of them and on the time that they "run" (i.e. are lighted). If there are 50300 -C.P. lamps the cost is $£ 3$ a week. What would it cost to run 80 250-C.P. lamps?
4. If a train travels at an average speed of 64 miles per hour between London and Liverpool it can do the journey in 6 hrs . 15 mins. To what must the average speed be increased in order that 15 minutes may be saved on the journey?
5. There are four trap-doors fitted into the gates of a lock, each being $7 \mathrm{sq} . \mathrm{ft}$. in area; they allow the water to flow out to the required level in $4 \frac{1}{2}$ minutes. What size must each of three doors be to allow the water to run out in $3 \frac{1}{2}$ minutes?
6. In planning the seating accommodation of a hall it is found that with seats 1 ft .8 in . wide the total number that can be put in is 1000 . By how much must the width of each seat be reduced in order that there may be room for 1250 people?

The student should now rework Examples LXI. (a) and LXI. (b).

## A. (3)

1. Three grocers in a suburban town enter into partnership together. The first supplies stock valued at $£ 380$ and also $£ 120$ in cash, the second supplies $£ 560$ value of goods and $£ 80$ cash, the third supplies $£ 750$ goods. Divide the profit of $£ 472$ 10s. between them.
2. Divide $£ 4641$ among five merchants engaged in the same business in the ratio of $2: 4 \frac{1}{2}: 5: 8: 3 \frac{1}{4}$.
3. Three partners agree that one shall be managing director of the firm and receive a salary of $£ 450$ per annum, the other shall be town manager at a salary of $£ 300$ per annum, while the third shall be a slecping partner. They advance respectively
$£ 3500, £ 5800, £ 10000$, and the profits are $£ 2487$. Pay the first two their salaries and divide the balance in proportion to the capital advanced.
4. There are 3844 shareholders in a company divided into four equal groups, the value of their holdings being in the ratio of $1: 1 \frac{1}{2}: 2: 2 \frac{1}{2}$. The total amount available for dividend is $£ 93564 \mathrm{~s}$. Calculate the amount available for each group and the average amount received by each individual shareholder in the group.

## A. (4)

## SECTION XVII. B (1) to B (5)

1. A draper pays $£ 234 \mathrm{~s}$. 8 d. in a year in rates which were at 8 s . in the pound; what is the rateable value of his premises, and what rent should he pay if the rateable value is $\frac{7}{8}$ of the rental?
2. The rates in Poplar (London) stand at 11 s .7 d . in the pound and are the highest among the Metropolitan Boroughs, while the rates at Kensington are 7 s ., and are the lowest. If the rateable value of the former borough be $£ 811000$ and of the latter $£ 2,433,000$, calculate which of the two produces the greater amount, and by how much. (To the nearest £100.)
3. The rates in one city are 7 s .6 d . and in another 8 s . 2 d . in the pound per annum. There are 87000 houses in the former and 96000 in the latter. The rateable value is $£ 2,639,000$ and $£ 2,848,000$ respectively. Find by how much the average amount paid in rates per house in the second city is greater than in the first, per half-year.
4. Determine a merchant's net income from the following: Net profit on sales of goods, $£ 500$; income from investments, $£ 180$; rent paid for premises, $£ 84$; rateable value of premises, $\frac{5}{6}$ of rental ; rates are 8 s .6 d . in the pound; income-tax abatement, $£ 150$; income-tax, earned income, 9 d . in the pound; income-tax, unearned income, 1s. 2d. in the pound. Give the answer to the nearest £1. (The income-tax is charged on the income before rent and rates are paid.)
5. With income-tax at 2s. 1d. in the pound a tenant deducts $£ 710$ s. from his March quarter's rent in consideration of the tax he has paid. What rates does he pay per half-year if they are 7 s .8 d . in the pound?
6. My partner has some money in a large silk mercer's, and he finds when the voucher comes in that $£ 241 \mathrm{~s} .3 \mathrm{~d}$. has been deducted for income-tax, which stands at 1 s .9 d . in the pound. What was his net income?
7. A traveller has $£ 3500$ stock in the London and Western Railway which pays him $5 \frac{5}{8} \%$ p.a. If income-tax is 2 s .3 d . in the pound, what is his net unearned income?
8. How much more would the net income of the traveller of the last question have been if he had had his money in the London and Eastern Railway, paying 6 \% p.a. ? (Income-tax as before.)

The student should now rework Examples LXX.
A. (5)

1. If a dairyman pays an annual fire insurance premium of 15 s . on premises valued at $£ 1000$, what is the rate per cent.?
2. If a coal merchant, aged 41, holds a life policy for $£ 5600$ and pays a premium of $£ 37 \mathrm{~s} .2 \mathrm{~d} . \%$, how much abatement can he claim in respect to income-tax?
3. The premium payable to one life office for insured, aged 50 , is $£ 411 \mathrm{~s} .10 \mathrm{~d} . \%$ with profits, while another office charges $£ 25$ 9 s .8 d . on a $£ 550$ policy. If now a merchant insures for $£ 1000$ in the one charging the lower rate, how much would he save per annum in premium?
4. A banker insures his life for $£ 3500$ and pays a premium of $£ 23 \mathrm{~s} .4 \mathrm{~d} . \%$ p.a. After 15 years he surrenders the policy and receives $£ 600$ in cash. What has the company actually charged him for covering his life for the period named? (Neglect interest.)
5. Three tea merchants ${ }^{1}$ are in partnership and they agree to pay all outgoings in proportion to the capital they put in, namely, $£ 3000, £ 5000, £ 4500$. They have a store containing tea valued at $£ 4000$ which is covered against fire at $2 \mathrm{~s} .6 \mathrm{~d} . \%$. What must each contribute to the premium which will provide for a policy to cover both tea and premium?

## A. (6)

## SECTION XVII. B(6)

1. An estate agent finds that his liabilities are $£ 5644$ 16s. and his assets $£ 3292$ 16s. A friend offers to give $£ 940$ 16s., provided the affairs are not put in the receiver's hands. By how much will a creditor for $£ 560$ benefit by accepting the latter arrangement?

[^53]2. A bankrupt's liabilities are $£ 9876$ 6s. 9 d., including preferential claims which amount to $£ 185$. What assets must he have to allow for a dividend of 6 s .8 d . in the pound?
3. A bankrupt pays 4 s .6 d . in the pound, and I find that I have lost $£ 818 \mathrm{~s} .3 \mathrm{~d}$. thereby. What did he owe me ;
4. A firm has assets to the value of $£ 11185$ and the liabilities are stated to be $£ 40650$. On examination it is found that one item in the former is a debt of $£ 750$ which realises 18 s . in the pound, and among the liabilities a claim for $£ 250$ is disallowed. What dividend can be paid?
5. A bankrupt pays a dividend of 8 s . 4 d ., and 6 months later a further dividend of 3 s .6 d ., and after three months a final dividend of 2 s .2 d . What amount does a creditor whose account stands at $£ 2800$ receive on each occasion, and what does he lose altogether?
6. The creditors of a bankrupt find that the assets are $£ 6430$, the liabilities $£ 12600$, and that preferential claims, other than legal expenses, are $£ 350$. The dividend is 9 s .4 d . in the pound, what were the lawyer's charges?
7. Find the dividend payable in the following case: Assets —cash, £2350; goods, £1250; good debts, £1000; bad debts reckoned to produce 5 s. in the pound, $£ 780$; bad debts reckoned to produce 8 s . in the pound, $£ 985$; bad debts reckoned to produce 12 s . in the pound, $£ 360$. Liabilities-preferential claims, $£ 380$; other claims, $£ 8420$.

The student should now rework Examples LXVIII.
B. (1)

## SECTION XVIII.

1. $15 \frac{1}{4} \mathrm{cwt}$. is $60 \%$ of a consignment of mahogany ${ }^{1}$ from the West Indies. What is the total weight?
2. A merchant orders 560 drums of Valencia raisins (of 24 lb . per drum) and finds that 375 have been delivered in one lot. What percentage of his order has still to be delivered?
3. Find, correct to three decimal places, the percentage error in calling an account for $£ 35018 \mathrm{~s} .6 \mathrm{~d} ., £ 351$.
4. The United States is said to have manufactured $88,514,000$ barrels of cement last year and $92,097,000$ the year before. What was the decrease per cent.?
5. In 1910, 35,101,500 sovereigns were coined; in 1911,

[^54]$43,260,000$; and in 1912, 42,519,000. What difference is there between the percentage increase in 1910-11 and the percentage fall in 1911-12?
6. If the rate of exchange be 25.25 francs to the pound on one date and $25 \cdot 20$ on another, calculate the percentage rise or fall in the value of a franc in the second case, and so decide upon which day it would be better to dispose of a 1000 -franc bill ${ }^{1}$ in London.
7. In 1892 the general level of the retail price of beef was $99 \cdot 4$; in 1902, $105 \cdot 3$; and in 1912, 1089 (the year 1900 being taken as the standard, 100). Was the percentage rise 1892-1902 greater or less than that in 1902-12, and by how much?
8. Labour Exchange returns show the following:

| Year. | Applications for Work. | Number of Applicants. |  |
| :---: | :---: | :---: | :---: |
| 1911. | . | . | 2010113 |
| 1912. | . | 2423213 | 1502268 |

Calculato (1) the percentage increase, in each case, on the number for 1911 ; and (2) the difference between the percentage increase in the number of applications for work and that in the number of applicants.
9. A diamond merchant pays his agent $2 \mathrm{~s} .3 \mathrm{~d} . \%$ on his sales, which amount to $£ 1589015 \mathrm{~s}$. What is the total amount paid in commission?
B. (2)

1. Exports of Cardiff-total, $£ 9,695,000$; coal, coke, and patent fuel, $£ 9,650,000$. What percentage of the total exports were not included under coal, coke, and patent fuel?
2. The Government of India spent £114293 in 1912 on Famine Relief, including protective railways and irrigation works, and $£ 188885$ in 1913. Calculate the percentage increase in the expenditure in the second year over that in the first. ${ }^{2}$
3. In two successive years a Russian iron-selling syndicate booked orders to the extent of $147,679,340$ poods and $118,555,680$ poods respectively. Find the decrease per cent. in the year's sales.

[^55]4. Last year the value of the products of a potash manufacturing company in Germany was 156 million marks, while the year before it was 192 million. By how much per cent. did the value of the production fall in the period named?
5. In two successive years the wheat production of the Australian Commonweath increased from 71,636,347 to 91,969,547 bushels. Find the increase per cent.
6.

# THE INDIAN ${ }^{1}$ CROP. <br> (FROM OUR CORRESPONDENT.) 

## Delhi, March 7.

The second wheat forecast shows $32,028,000$ acres of crop, or $23 \%$ above the same period of last year. The first forecast, on January 7 , was $28,694,000$ so that late sowings have increased the acreage by $3,334,000$.
Find from the data given above (taken from a newspaper) (1) the acreage last year ; (2) the percontage increase in the January estimate produced by late sowings.
7. Tenders are invited by the Department of Street Cleaning in Toronto for furnaces and appurtenances for refuse incinerating plant. Sealed tenders must be accompanied by a cash deposit or a marked cheque for $2 \frac{1}{2} \%$ of the value of the offer, made payable to the City Treasurer. If a firm submits a tender of $£ 5864$ 15 s . for part of the plant, for what value, in dollars, must a marked cheque be drawn? ( 1 dollar $=4 \mathrm{~s} .1 \frac{1}{8} \mathrm{~d}$.)
B. (3)
1.

## OFFICIAL CLOSING QUOTATIONS.

Pig Iron (price per ton)-


The details given are taken from our newspaper. By how much per cent. (of yesterday's price) has the cost per ton fallen from yesterday to to-day?
2. What must be the retail price per ton of foreign tin selling wholesale at $£ 176$ per ton to gain $22 \%$ on the retail price?
3. What is the retail price per cwt. of Castile soap imported from France into Canada, if $2,626,500 \mathrm{lb}$. are valued at 152800 dollars and sold retail at $15 \%$ profit on that value?

[^56]4. A merchant in the Midlands sends piston-ring castings in the rough to New Zealand to the value of $£ 35615 \mathrm{~s}$. The duty payable is $20 \%$ ad val. Find the duty to be paid, and thence calculate the percentage profit on the selling price of 420 guineas.
5. If 617500 bunches of bananas valued at $£ 30320$ were exported from British Honduras last year, calculate, to the nearest shilling, the retail price per bunch to gain $10 \%$ on the original value.
6. If bananas are sold in London for three a penny, what is the wholesale price per bunch of 150 if the profit is $12 \frac{1}{2} \%$ on the wholesale price?
7. A costermonger buys oranges at $4 \frac{1}{4} \mathrm{~d}$. a dozen and sells twothirds of them at two a penny, two-fifths of the remainder at five for $2 d$. , and the rest at three a penny. What percentage profit does he make?
8. A wholesale firm allows $5 \%$ off the prices in the price list. The retailer sells to the consumer so as to gain $20 \%$ on his cost price. By how much per cent. of the wholesale list price has the consumer to pay more than if he could buy direct from the wholesale merchant at the list price?
9. A cubic centimetre of water weighs 0.99996 gm . at $4^{\circ} \mathrm{C}$., and 0.99969 at $10^{\circ} \mathrm{C}$. Calculate the average percentage fall in weight for each degree rise in temperature from $4^{\circ}$ to $10^{\circ} \mathrm{C}$.
10. The Freight Market report in our newspaper contains the following: "Steamer, 3000 tons, Bilbao, 12s. 9d. to Middlesborough or West Hartlepool, 12s. 6d. to the Tyne, May." What is the percentage decrease for conveying cargo to the Tyne rather than to either of the other places named? Put the information between the inverted commas into your own words.

## C.

## SECTION XIX.

(The following have been taken from recent examination papers.)

1. Enter the following transactions in your Subsidiary Books, post into the Ledger, and then balance your Ledger and prepare a Trial Balance. Feb. 1, 1915. Charles Dugmore began business with cash amounting to $£ 120$. Feb. 3. Bought goods from R. Russell, £75 6s. 8d. Feb. 5. Bought goods for cash, $£ 22$ 3s. 4d. Feb. 6. Sold goods to F. Shepherd, £21 2s. 6d. Feb. 8. Paid R. Russell on account, £20. Feb. 10. Sold goods for cash, £30. Feb. 15. Bought goods from C. Oliver, $£ 10$ 12s. 5 d .

Feb. 19. Sold goods to G. Markham, £5 16s. 10d. Feb. 25. Received cash from F. Shepherd, £20; and allowed him discount, $£ 12 \mathrm{~s} .6 \mathrm{~d}$. Feb. 28. Paid trade expenses, £4 10s. 6d.
2. (a) Why is there a debit and a credit entry for each transaction? Give as full an explanation as you can. (b) What is the effect on a Trial Balance if (i) a debit entry is not posted into the Ledger; and (ii) a credit entry is posted to the Ledger on the correct side, but to the wrong account?
3. From the following list of transactions write up the Cash Book, Day Books, and Ledger of F. Mathews, and prepare Trial Balance: Nov. 1. Started business with cash, £60. Nov. 2. Bought goods from Smith \& Co., £50. Nov. 3. Cash purchases, £25. Nov. 4. Cash sales, £20. Nov. 5. Sold goods to Burgess \& Co., £50. Nov. 6. Received from Burgess \& Co. cash on account, £40. Nov. 10. Paid gas, rent, fuel, etc., £5. The stock of goods on hand were valued at $£ 50$.
4. Rule a page as for a Columnar Cash Book and enter therein the following receipts and payments: Jan. 1. Balance at Bank, £25; subscriptions received and paid into lBank, £25. Jan. 3. Donations received and paid into Bank, £30. Jan. 5. Dividends received by bankers direct, £25. Jan. 8. Contributions for particular "Cases" and paid into Bank, £35. Jan. 1. Coal purchased for "Cases" by cheque, £23. Jan. 3. Rent of offices paid by cheque, £10. Jan. 8. Money payments to "Cases" by cash withdrawn from Bank, £47. Jan. 8. Salaries paid by cheque, $£ 6$.
5. W. Carrick commenced business on 1st January and paid into his Bank Account as capital, $£ 10000$. There was paid from the Bank for premises, plant, and machinery, £5000. The following are the transactions for the twelve months: Purchases, $£ 30000$; sales, $£ 45000$; received from debtors, cash, $£ 33000$; allowed to debtors for discount, $£ 2000$; paid to creditors, $£ 16000$; received from creditors, discount, $£ 1500$; paid for trade expenses, £2500; paid for salaries and wages, £3000; neglect the value of the stock at the end of the year. Record the above in W. Carrick's Cash Book, Day Books, and Journal, post to the Ledger Accounts, and prepare the Balance Sheet and P. and L. Account at 31st December.
6. Enter the following transactions into the proper Subsidiary Books, post to the Ledger, and take out a Trial Balance : Bought of W. Murray, goods, $£ 400$; sold to M. Flockhart, goods, £840; sold to E. Barr, goods, £320. M. Flockhart settled his account as follows: Cheque, $£ 500$; bill at 2 months, $£ 300$; discount, $£ 40$. Drew from Bank for self, $£ 50$. Bought
from A. Troup, goods, £300. Settled W. Murray's Account as follows : Cheque, $£ 100$; bill at 3 months, $£ 280$; discount, $£ 20$. Paid A. Troup on account, £150. Paid office salaries for this month, January, by cheque, $£ 60$.
7. F. Nicholls has the following transactions with D. Chadwick: (1) On 1st January sells to D. Chadwick goods of the value of $£ 200$ subject to $25 \%$ discount, payable in cash on 31st January. (2) On 1st January purchases from D. Chadwick goods of the value of $£ 100$ subject to $40 \%$ discount, payable in cash on 30th January. The goods were delivered and paid for as agreed. Make the necessary entries in F. Nicholls' Day Books and Cash Book and post to the Ledger.
8. The following totals appear in the tabular Cash Book at the end of the month: On the Debit side-Bills receivable, $£ 2500$; cash sales, $£ 650$; discount, $£ 400$. On the Credit side-Bills payable, $£ 4000$; office expenses, $£ 500$; discounts, £600. Open Ledger $\Lambda$ ccounts for the above and post them to their respective accounts.
9. In preparing a Balance Sheet and P. and L. Account, in which account and on which side thereof do the following appear-(1) Profits; (2) Liabilities; (3) Losses; (4) Assets; (5) Capital; (6) Expenses; (7) Sinking Fund for a Lease; (8) Debenture Issue; (9) Stock at the end of the period; (10) Bills Payable?
10. The position of B. Salt on 1st February 1912 was as follows: Assets-Cash in hand, £24 3s. 6d.; cash at Bank, $£ 312$ 8s. 9d.; bill receivable, due February 10, £86 10s.; G. Thorp, £21 6s. 8d.; W. Stott, £59 5s. 6d.; office furniture, $£ 6215 \mathrm{~s}$. ; goods on hand, £522 7s. Liabilities-J. Firth, $£ 218$ 9s. 6d.; J. Holroyd, £371 3s. 4d. His transactions for the month were as follows:

Feb. 1. Received bill of exchange at 2 months from W. Stott in $\begin{array}{llll}\text { settlement of his account . } & 59 & 5 & 6\end{array}$
„ 2. Sold goods to E. Evans for cash

8160
2. Paid into Bank . . . $100 \quad 0 \quad 0$
3. Bought for cheque roll top desk
$5 \quad 50$
9
6. Drew and cashed cheque for office cash
$20 \quad 0 \quad 0$
9. Paid bill due 10 th inst. into Bank
$8610 \quad 0$


Record the above in the proper books, post to Ledger Accounts, and take out Trial Balance.
11. From the foregoing, close the accounts, bring down the balances, make out P. and L. Account and Balance Sheet. On 29th February 1912 the stock was valued at $£ 339$ 19s. 10d.
12. Enter the following transactions in E. Elgood's Day Books, Cash Book, and Journal, post to the Ledger Accounts, and take out a Trial Balance of the books: Jan. 1. E. Elgood commenced business paying into his Banking Account as capital the sum of $£ 1000$. Jan. 4. Bought of J. Day, dry goods subject to a trade discount of $10 \%$ (£65) of the value of $£ 650$. Jan. 15. Paid J. Day by cheque, receiving a discount of $5 \%$ ( $£ 295$ s.) the sum of $£ 555$ 15s. Jan. 16. Sold above goods to J. Jones, £700. Jan. 16. J. Jones wishes to pay by bill at 1 month with $£ 310$ s. added for interest, which offer is accepted and a bill was received dated this day for $£ 70310$ s. Feb. 18. J. Jones' bill due to-morrow paid into the Bank for collection, the amount of the bill being for $£ 70310 \mathrm{~s}$. Feb. 20. J. Jones' bill returned
unpaid with 3 s .6 d . added for expenses, the entry being for $£ 70313 \mathrm{~s} .6 \mathrm{~d}$. Feb. 21. J. Jones agreed to pay a further sum of £2 for interest and then to discharge his indebtedness as follows: Cheque which was paid into the Bank, $£ 30513 \mathrm{~s} .6 \mathrm{~d}$. ; new bill at 1 month, £400. Mar. 22. J. Jones' bill was paid into the Bank for collection and was duly met for $£ 400$.

## D. (1)

## SECTION XX.

1. What must be paid for a loan of $£ 550$ for 14 days at $3 \frac{1}{2} \%$ p.a.?
2. If interest is charged at $5 \%$ p.a., and a loan for 146 days brings in $£ 10$, what is the amount of money lent?
3. What will $£ 78415 \mathrm{~s} .8 \mathrm{~d}$. invested at $5 \frac{1}{2} \%$ p.a. produce in interest in $4 \frac{1}{2}$ years?
4. What will $£ 856 \mathrm{l} 2 \mathrm{~s}$. amount to at $6 \frac{1}{4} \%$ p.a. if the interest is allowed to accumulate for 10 years?
5. A banker buys Government Bonds ${ }^{1}$ to the value of $£ 15580$, and is to receive the interest quarterly at the rate of $4 \frac{1}{2} \%$ p.a. What does he receive each quarter?
6. If a merchant lends his chief clerk $£ 785$ on mortgage on his house, and receives interest at the rate of $4 \frac{1}{4} \%$ p.a., the clerk paying back the capital at the end of 5 years and the interest annually, calculate the total amount the merchant receives in interest in the 5 years, and the net amount after deducting income-tax at 1 s .2 d . in the pound.
7. If 12000 francs be deposited on 31st January with a rate of interest of $3 \%$ p.a., which becomes $3 \frac{1}{2} \%$ p.a. on 30 th June and $4 \%$ on 30th September, calculate the interest due at the close of the year.
8. Interest is allowed at $2 \frac{1}{2} \%$ p.a. on minimum monthly balances. What amount is due on 31st December on the following: June 30, £500; July 15, deposit, £100; August 18, withdrawal, £350; August 28, deposit, £500; September 8, deposit, £200; October 20, withdrawal, £100; November 3, withdrawal, £50; November 18, deposit, £300; November 28, withdrawal, $£ 10$; December 20, deposit, $£ 200$ ?
9. A sum of money put out at Simple Interest amounted in 6 years to $£ 5200$, and in 10 years to $£ 6000$. Find the sum and rate of interest.
[^57]
## D. (2)

1. I invest $£ 56015 \mathrm{~s} .8 \mathrm{~d}$. for 3 years at $4 \%$ p.a. Compound Interest; what amount shall I then have standing to my credit?
2. The Post Office Savings Bank allows $2 \frac{1}{2} \%$ p.a. on money invested. How much will be due to a clerk at the end of 2 years if he have $£ 50$ in the Bank to begin with?
3. What is the Compound Interest on $£ 83010 \mathrm{~s}$. 6 d . invested for 4 years at $3 \%$ p.a.?
4. Find the Compound Interest due after $3 \frac{1}{2}$ years on $£ 7567 \mathrm{~s} .6 \mathrm{~d}$. invested at $2 \%$ p.a.
5. A French wine merchant has a vineyard for which he paid 30000 francs. For 3 years it brings him in no income and does not increase in value, but from the third to the sixth year its value increases $10 \%$ each year. At what price must he sell it at the end of the sixth ycar to make a profit of $5 \%$ on its value at that time?
6. A colonist has a large area under fruit in Canada. He spends $£ 1000$ upon it, and receives $5 \frac{1}{2} \%$ the first year, $8 \%$ the next, $10 \%$ the next, and $12 \frac{1}{2} \%$ the next on the value at the beginning of the particular year in question. In the fifth year a frost blights the blossom and he makes nothing. Find his average receipts per annum during the five years.
7. A debt of $£ 512$ was left unpaid for 3 years. What amount is due to the creditor at the end of that time, reckoning Compound Interest at $4 \frac{1}{2} \%$ p.a. ?
8. $£ 625$ was invested for 2 years at Compound Interest, the rate being $4 \%$ p.a. for the first year and $3 \%$ p.a. for the second. Interest was added half-yearly. Find the amount earned.
9. A mortgage of $£ 1575$, rate of interest $4 \%$ p.a., was neglected for $3 \frac{1}{2}$ years. What was the total amount then due, Compound Interest being charged?
10. Upon what sum of money invested at $5 \%$ p.a. for 2 years is the difference between the Compound Interest and the Simple Interest 10 s . ?

## E. (1)

## SECTION XXI.

1. If a family consumes 12 loaves, costing $4 \frac{1}{2} \mathrm{~d}$. each, per week, and the baker allows a cash discount of $2 \frac{1}{2} \%$ on the monthly account, find the net amount payable.
2. A lady noticed that a sewing-machine was offered at $£ 37 \mathrm{~s}, 6 \mathrm{~d}$. with $5 \%$ discount for cash. On going to purchase
the same the account was made out for $£ 35 \mathrm{~s}$. By how much was this wrong?
3. A revolving bookcase in walnut is reduced from 32s. 6d. to 28 s . 6d. for cash. At what rate per cent. is discount allowed?
4. What remains in each case after allowing discounts as follow: $2 \frac{1}{2} \%$ from $£ 50010 \mathrm{~s}$.; $4 \%$ from $£ 30015 \mathrm{~s} . ; 7 \frac{1}{2} \%$ from $£ 600 \mathrm{l} 10 \mathrm{~s}$. ; $33 \frac{1}{3} \%$ from $£ 390 \mathrm{l} 0 \mathrm{~s} .6 \mathrm{~d} . ?$
5. The manufacturers' list price of a suite of furniture is $£ 25$, and his prices advance $10 \%$. If the retailer is allowed $15 \%$ on the list price, how much more must he pay than he did before the manufacturers' advance?
6. If dried apricots are sold in cases of (about) 56 lb . at 30 s . a case list price, and the retailer is allowed $2 \frac{1}{2} \%$, calculate his selling price per lb . to gain $20 \%$ on his outlay.
7. The producer of cotton goods advances his price $12 \frac{1}{2} \%$ and still allows the wholesale houses $15 \%$. The latter usually make $50 \%$ profit on the actual cost to them, and they now advance their rate to $60 \%$ and reduce their trade discount to the retailer from $10 \%$ to $5 \%$. How much more has the retailer to pay for shirts which the producer listed at 48s. per dozen?
8. I can buy my stock of ostrich feathers at $25 \%$ cash discount or net at 3 months. If my account runs to $£ 700$, at what rate per cent. per annum must I invest the money so that if I pay at 3 months I may not lose the amount of the cash discount? (Reckon Simple Interest.)

## E. (2)

1. A contractor agrees to honour a bill for 53568 roubles on 9th September; it is discounted in Petrograd at $3 \%$ p.a. on 28th June. What is its discounted value?
2. If the broker who bought the bill in Question 1 sold it for 53250 roubles the same day, and invested the proceeds at $3 \frac{1}{2} \%$ p.a. until 9th September, how much more did he make than if he had held the bill till its due date?
3. A bill for $£ 750$ was drawn on 6 th March, payable 6 months hence, rate $4 \frac{1}{2} \%$ p.a. It was discounted 28 th June. What did the banker pay the holder of the bill?
4. A 6 months' bill is discounted at $5 \%$ p.a. To what rate of interest is this equivalent?
5. What rate of interest is equivalent to a discount rate of $2 \frac{1}{2} \%$ p.a. for 3 months' bills?
6. A stock of timber which will be sufficiently seasoned for sale in 8 months will then be worth $£ 4650$. Find its present value: (a) By the method of true discount; (b) by the method of commercial discount. (Rate of interest per annum, $5 \%$.)
7. John Thompson \& Co. draw on Bell \& Evans at 3 months from 15th December 1914, for $£ 650$ 6s. 8d. They discount the bill with Lloyd's Bank Ltd. on 31st January 1915, the rate charged being $4 \frac{1}{2} \%$ p.a. What amount do Thompson \& Co. receive?
8. A bill of the value of $£ 625$ is drawn on lst March, the latest day for its payment being 4th July following. It was discounted on 31 st March, the rate of discount being $4 \%$ p.a. What was received by the holder of the bill?
9. Find the difference hetween the true discount and the commercial discount on $£ 190610$ s. due in half a year at $5 \%$ p.a.
10. We take the following from our newspapers :-

# "VICTORIAN GOVERNMENT $4 \frac{1}{2} \%$ LOAN, 

## 1920-1925.

Applications on the form prescribed will be received at the London County and Westminster Bank Limited, Lothbury, and must be for multiples of $£ 100$ and accompanied by a deposit of $£ 5 \%$ ou the nominal value applied for.

Payment will be required as follows :

$$
£ 5 \% \text { on application. }
$$

£10\% on 3rd May 1915.
£ $40 \%$ on 28th June 1915.
$£ 45 \%$ on 26th July 1915.
Payment may be made in full on 3rd May 1915, or any subsequent day, under discount at the rate of $2 \frac{1}{2} \%$ p.a."
What amount should be paid on 3rd May for $£ 100$ stock ?
11. Messrs. Roche of Manchester do business with Hubert Frères of Lyons, who are able to buy a 6 months' bill for $£ 5000$ discounted at $4 \%$ p.a. They find that at the current rate of exchange, namely, $25 \cdot 20$ francs, the discounted value of the bill will just meet their account with Messrs. Roche. How much is that account in francs?
12. The French Government issued the $5 \%$ Rentes Loan, and English investors might pay $£ 33 \mathrm{~s}$. 6d. on application or smaller sums at various dates. If the amount to be paid in the latter case were equivalent to $£ 34 \mathrm{~s}$., due in 50 days, determine the discount rate.

## F. (1)

## SECTION XXII.

1. How much must be put into the Russian $4 \%$ at $80 \frac{1}{2}$ to give an income of $£ 1000$ p.a.?
2. Which investment will produce the larger incomeMexican $5 \%$ at $54 \frac{1}{2}$, or $2 \frac{1}{2} \%$ Consols at 66 ? Which would you choose to put your savings into?
3. What income will a merchant get by putting $£ 5836 \mathrm{1s}$. into the Sheffield $3 \%$ at 88 ?
4. If the merchant in Question 3 sells out at 891 , what will he make on the deal?
5. Complete the following table:

| Stock. | Price. | Yield per Cent. on Money invested. | Dividend declared per Cent. |
| :---: | :---: | :---: | :---: |
| G.W.R. | 1354 | $\begin{array}{lll}\text { \& } & s . & d . \\ 3 & 19 & 0\end{array}$ | $\boldsymbol{£}_{\underset{q}{ } .} d$ |
| East Indian | ? | 2193 | 400 |
| N.W.R. | 156 | ? | $6 \quad 26$ |

6. As many Lyons shares as possible are bought for $£ 100$. If their par value be $£ 1$, the present price $£ 6 \frac{1}{2}$, and the dividend $40 \%$, calculate the income obtained.
7. If Lyons shares rose to $£ 7$, what profit would be made by selling out the shares of Question 6 ?
8. If Hudson's Bay $£ 1$ shares stand at $£ 10 \frac{1}{2}$ and the dividend is $50 \%$, what is the percentage return?
9. What would the dividend have to be on Hudson's Bay shares (Question 8) to give $5 \%$ return?
10. What return \% do Lyons $£ 1$ shares yield if they stand at £63 and the dividend is $42 \%$ ?
11. A merchant invests $£ 1000$ in a stock paying $3 \%$ and gets an income of $£ 60$ a year. What is the price of the stock?

$$
\text { F. }(2)^{1}
$$

1. Consols, bearing $2 \frac{1}{2} \%$ interest p.a., stand in the list at $75 \frac{1}{4}$ ( $£ 75 \frac{1}{4}+£ \frac{1}{8}$ for brokerage for $£ 100$ scrip). What amount of such scrip will $£ 1206$ purchase, and what rate per cent. is received on the money invested?

[^58]2. A banker having $£ 1000$ to invest spent part of it in buying £850's worth of $2 \frac{1}{2} \%$ Consols at $78 \frac{1}{4}$, and the remainder in buying $£ 5$ shares in a water company quoted at $£ 5 \frac{7}{8}$. If he received 8 s . per share on the latter, what was his total income?
3. A merchant invests $£ 2852$ in $5 \%$ railway stock at 115 ; he also expends $£ 1620$ in buying industrial shares at $£ 11 \ddagger$. If the half yearly dividend on the latter is 7 s .6 d . per share, what is his total income?
4. A merchant had $£ 6850$ in $2 \frac{1}{2} \%$ Consols. He sold out at $78 \frac{3}{4}$ and invested, in $3 \frac{1}{2} \%$ India stock at $96 \frac{1}{4}$, as much as would produce the same income as before. How much money had he left?
5. A merchant invested $£ 750$ in the $3 \frac{1}{2} \%$ Stock at 77 , and $£ 500$ more when the price was 824 . Deduct income-tax at 1 s .2 d . in the pound, and find his net income and the percentage return he obtained.
6. A broker derived an annual income of $£ 2536 \mathrm{~s}$. 8 d. from money invested in $2 \frac{1}{2} \%$ Consols. He sold out at $77 \frac{1}{2}$ and bought $3 \frac{1}{2} \%$ Stock with the proceeds, thereby increasing his income by £36. At what price did he buy the $3 \frac{1}{2} \%$ Stock?
7. A cotton mill has a capital of $£ 40000$. The profit made during the last quarter is $£ 937$; £537 is placed in the Reserve Fund, the rest is paid as dividend. What dividend will be received by a man holding shares of the nominal value of $£ 1500$ ? Supposing that he bought them at a discount of 7 s .6 d . per $£ 1$ share, what interest at least does he make per annum on his investment?
8. In 1875 Britain acquired from the Khedive of Egypt 176602 shares in the Suez Canal Company for $£ 4,000,000$, and each share was of the value of 500 francs. If 25 francs equal $£ 1$, what was paid for one share in 1875 ? If the value of the shares be $£ 34,930,000$ at present, find the present market price of one share and the rate of interest earned on the original purchasing price.
9. A company whose issued capital consists of 90000 Cumulative $6 \%$ Preference shares of $£ 5$ eash fully paid, 500000 Cumulative $6 \%$ B Preference shares of $£ 1$ each fully paid, and 625000 Ordinary shares of $£ 1$ each fully paid, distributes dividends in the year amounting to $£ 166375$. Apportion this amount amongst the three classes of shareholders, and calculate the rate per cent. which the Ordinary shareholders received.
10. A person held for 1 year $£ 600$ stock of the $6 \%$ Peruvian Corporation Debentures, and 1000 mining shares of the value of 2s. 6d. each fully paid, which have paid in the year dividends
amounting to 1 s . 3d. a share. When the selling price of the Peruvian Corporation Debentures is 106 and the selling price of the mining shares is 10 s .9 d ., he sells out all and invests the proceeds in the $2 \frac{1}{2} \%$ Consols at $74 \frac{5}{16}$. What amount of the Consols did he buy, what will his income now be, and what was his income during the year he held the Debentures and the mining shares? (Allow brokerage of $\frac{1}{8} \%$ on sale of Debentures, $\frac{1}{8} \%$ on purchase of Consols, and a commission of $1 \%$ on nominal value of mining shares for selling them.)
11. Taking Plate XVI., presume that you are A. Burt, and endorse the dividend warrant which is payable to your order, so that it may be paid by the bank "to the order of James Wilson." Now assume that you are James Wilson, and that you do not want to cash the warrant. Endorse it again so that it may be payable to the order of R. J. Wilkins.

## ANSWERS TO EXAMPLES

## PAR'T' II.

## EXAMPLES. LIII.

SECTION XIV. A.

## VOLUMES: RECTANGULAR OBJECTS

P. 293. - 1. (1) 5. (2) 6.
2. (1) 12 . (2) 12
3. Objects (1) to (15) have 12 edges and 6 surfaces each; (16) and (17) 2 edges and 3 surfaces; (18) 0 and 1 ; (19) and (20) 2 and 3 ; ( 21$) 1$ and 2 ; (2.2) 12 and 6 if rectangular, 2 and 3 if cylin. drical ; (23) 2 and 3 ; (24) 2 edges and 2 surfaces outside and 2 inside.
P. 294. - 4. Rectangular objects have 12 edges and 6 surfaces.
б.

| Object. | Number of Surfaces. | Number of Edges. |
| :---: | :---: | :---: |
| Sphere | 1 | 0 |
| Closed cylinder. | 3 | 2 |
| Cy'inder open at the top | 2 outside and | 2 |
| Closed cone | $\underset{2}{2}$ | 1 |

6. 5 whitewashed, 4 painted. 7. 9 ft. $\quad$ 8. 486 sq . in.
7. 32 sq . ft.
8. 53 francs 25 centines.
9. 369 mks .60 pf .
10. The dots show the method of nailing. There are 4 edges with 8,4 with 5 , and 4 with 6 nails, making 76 in all.


Experiment 2.-There are nearly $16 \frac{1}{2}(16.38) \mathrm{c} . \mathrm{cm}$. in 1 cub . in. PART II.-I
P. 295. - 12. Experiment 3.-(1) $34 \frac{1}{2}(34 \cdot 66)$ cul. in. $=1 \mathrm{pt}$.
$\begin{array}{lll}\text { (2) } 61 \mathrm{cub} . \mathrm{in} . & =1 \text { litre. } & \text { (3) } 1000 \mathrm{c} . \mathrm{cm} \\ \text { ( } & \text { (4) } 568 \mathrm{c} . \mathrm{cm} . & =1 \mathrm{pt}\end{array}$
(5) $\frac{1}{2} \mathrm{pt} .=17 \frac{1}{4}$ cub. in. (nearly) $=284 \mathrm{c.cm}$.
13. (1) $1 \mathrm{c.cm} .=0.061 \mathrm{cub}$. in., correct to three places. (2) 0.061 . Experiment 4.-(1) 8 cub. in. (2) 27 cub. in. (3) 2 cub. in. (4) 12 cub. in. (5) $17 \frac{1}{2}$ cub. in.

14 and 15 . The results of the last two columns should be the same for each individual vessel. Hence the rule is that the volume of a rectangular vessel is given by the product of its three dimensions (expressed in the same units).
16. There should be no difference whatever, but the student may find a small error called an "Experimental Error," due to the sand being a little more closely packed in one case than in another.

## EXAMPLES. LIV.

## SECTION XIV. A.

## RECTANGULAR OBJECTS-(continued)

P. 297. - 1. (1) 72 cub. ft.
(2) $16800 \mathrm{c} . \mathrm{cm}$.
(3) 0.78 cub. m.
(4) 90 cub. ft.
(5) $33 \frac{3}{4}$ cub. yds.
2. 20 cub. in.
3. $327.7 \mathrm{c.cm}$.
4. 70 c cub. in.
5. $146 \frac{1}{4}$ cub. in.
6. 35 cub. ft .
7. $2180 \frac{1}{2} \mathrm{lb}$.
8. $0 \cdot 1692$ cub. m .
9. $169 \cdot 2 \mathrm{l}$.
10. 1600 cub. in.
P. 298. - 11. 3.9 cub . ft.
12. 5 cub . ft.
13. Volume of first is 0.86 times that of second.
14. First costs 0.124 s ., and the second 0.071 s . per cul. in., so that the larger costs less comparatively. Since labour and material enter into both, their cost for any particular box is more than half as much as for a box twice the size.
16. $£ 116 \mathrm{~s} .6 \mathrm{~d}$. (nearly).
16. $£ 0.775$ worse off.
17. $2 \mathrm{ft} .3 \mathrm{in} . \times 12 \mathrm{in} . \times 7 \mathrm{in}$.
18. $2 \mathrm{ft} .3_{4}^{3} \mathrm{in} . \times 12 \frac{4}{4} \mathrm{in} . \times 7 \frac{3}{4} \mathrm{in}$.
19. 240.
20. $10 \mathrm{ft} .6 \mathrm{in} . \times 4 \mathrm{ft} .6 \mathrm{in} . \times 5 \mathrm{ft} .2 \frac{1}{2} \mathrm{in}$.

## EXAMPLES. LV.

## SECTION XIV. B.

## SPECIFIC GRAVITY

## $\begin{array}{lll}\text { P. 299. - 1. } 28.27 \mathrm{Kgm} . & \text { 2. } 0 \cdot 696 \mathrm{lb} . & \text { 3. } 19 \cdot 3 \mathrm{gm} .\end{array}$

4. In the Metric System the unit of weight, 1 gm. ., is derived from the weight of $1 \mathrm{c} . \mathrm{cm}$. of water, i.e. $1 \mathrm{c} . \mathrm{cm}$. water weighs 1 gm ., and so the weight of $1 \mathrm{c.cm}$. of gold is easily found by multiplying the spuecific gravity by 1. In the English System 1 cab . ft. of water weighs $62.321 \mathrm{lb} . ; \therefore$ the weight of 1 cub. ft. of gold involves multiplying its specific gravity by 62.321 .
P. 299. - 5. Column 3 is-water, 1 ; salt, $1 \cdot 2$; powdered chalk, $1 \cdot 11$; powdered coal, $1 \cdot 5$; sand, $1 \cdot 9$; iron filings, $7 \cdot 2$; mercury, $13 \cdot 6$; paraffin, 0.8 ; glycerine, 1.25 .
P. 300. - 6. $691.07 \mathrm{lb} \quad$ 7. 666 lb . 8. 21 cub . ft. (very nearly).
5. 0.099 cub. ft., i.e. ${ }^{1} \sigma$ cub. ft. (uearly). $10.3571 \frac{3}{7}$ tons.
6. $1 \cdot 5625 \mathrm{lb}$. 12. $16 \cdot 19$ cub. ft.
7. Alcohol, $7 \cdot 9 \mathrm{lb}$. per gall. ; earth, 100 lb . per cub. ft. ; brass, 550 lb . per cub. ft. ; cork, 15 lb . per cub. ft. ; wine, 9.9 lb . per gall.
8. The numbers in Question 13, column 2, give the weights in grams. See answer to Question 4.
9. Lubricating oil, $1 \cdot 19 \mathrm{lb}$. per pint; methylated spirit, 1.06 lb . per pint; linseed oil, 1.175 lb . per pint; turpentine, 1.09 lb . per pint ; sea water, $1 \cdot 28 \mathrm{lb}$. ner pint ; milk, $1 \cdot 29 \mathrm{lb}$. per pint.
P. 801. - 16. 1 cub. ft. contains $6 \cdot 2: 21$ gallons.
10. (1) Keeping tho order of Question 15, the weights per gallon are, in pounds- $9 \cdot 5,8 \cdot 5,9 \cdot 4,8 \cdot 7,10 \cdot 25,10 \cdot 3$. (2) Woights per cub. foot are, in puunds- $59 \cdot 205,52 \cdot 973,58 \cdot 58,54 \cdot 219$, $63 \cdot 879,64 \cdot 191$. (3) There are 6.2321 gallons of any liquid to 1 cub. ft .
11. $222 \cdot 854$ cul. m.
12. 178284 Kgm . (correct to 1 Kgm .).
13. 20.825 tons.
14. 2.75 (i.e. its specific gravity $=2 \cdot 75$ ).
15. 0.9 .
16. $0 \cdot 9$.
17. $98 \cdot 6 \mathrm{lb}$.
18. $2 \cdot 0416$ cub. ft.
19. $1444 \cdot 3 \mathrm{lb}$.
20. $0 \cdot 1075$ ton.

## EXAMPLES. LVI.

SECTION XIV. 0.

## THE PRISM LAW

P. 303. - 1. 0.0346 cmb . ft.
2. $1 \cdot 875$ cub. ft.
3. 0.94 cub. ft.
4. 0.0327 cub. ft.
5. $0 \cdot 00005$ cub. m.
6. $0.707 \mathrm{cub} . \mathrm{m}$.
P. 804. - 7. 0.0203 cub. ft.
8. 116.91 cub. ft.
9. 11.926 tons.
10. 8285 cub. ft.
11. 73730 cub. ft .
12. 98 pints.
13. About $\frac{8}{4}$ more.
14. 60 shipping tons.
P. 305,-15. 4238 cub. yds.
16. 1800 cub. yds. ; $£ 180$.

## EXAMPLES. LVII.

SECTION XIV.

## MISCELLANEOUS QUESTIONS

P. 306. - 1. 29 hrs . 10 min .
2. 14 ft . 3. $£ 92 \mathrm{~s}$. (correct to 1 s. ).
4. 0.949 cub. yd.
5. 1054 lb . (correct to 1 lb .).
6. $3 \mathrm{ft} .6 \mathrm{in} . \times 3 \mathrm{ft} .6 \mathrm{in} . \times 5 \mathrm{ft} .3 \mathrm{in}$.
7. 218 cub. ft.
8. $468 \cdot 3$ loads.
9. 10 ft .


## EXAMPLES. LVIII.

## SECTION XV. WEIGHT AND CAPACITY

## MISCELLANEOUS QUESTIONS


P. 315.-52. The weights in order are, in Kilograms, $40 \cdot 8,16.4,3 \cdot 2,1 \cdot 7,0 \cdot 9$ $5 \cdot 9,1 \cdot 6,97 \cdot 1,109 \cdot 8$.
P. 316.-53. $58199 \cdot 47$ tons.
54. $2 \cdot 4 \mathrm{~d}$.
55. £1 18s. $6 \frac{1}{2} d$.
56. $13 \cdot 7$ kokus per chō $; 27 \cdot 7$ bushels per acre.
57. $12 \cdot 5$ bushels per acre ; difference, $12 \cdot 2$ bushels per acre.
58. 0.54 rouble per pood.
59. $108,450,496$ oranges.
60. $£ 15062513 \mathrm{~s} .9 \mathrm{~d}$.
61. 16276 tons (correet to 1 ton).
62. 32.8 Hl . per Ha.
63. $24 \cdot 3$ franes per Hl.
64. $4 \cdot 8 \mathrm{~s}$. per qr.
65. $2 \cdot 78$ francs per quintal.
P. 317.-66. $4 \% 3 \mathrm{~d}$. per cental; $1 \cdot 775 \mathrm{~s}$. jer $q$.
67. 5 tons 19 ewt. 3 qris. (nearly). 68. £11 19s. (rorrect to 1 s. ).
69. 110 tons 16 cwt 1 qr .
70. 96 tons: $\boldsymbol{2}$ cwt. 3 qrs.
71. 1 ton 3 ewt. 3 qrs. 18 lb .
72. $32 \cdot 16 \mathrm{lb}$.
73. $3848 \cdot 46$ grams.
74. $1 \cdot 2$ in.
75. $\mathfrak{E}^{2} 1617116 \mathrm{~s} .4 \mathrm{~d}$.
76. $5 \cdot 102 \mathrm{~d}$.
77. $916 \cdot 667$.
78. £3 $17 \mathrm{~s} .10 \frac{1}{2} \mathrm{~d}$.
79. £4 4s. 111 d .
80. £1. (Note that the actual value of the gold in a sovereign is its face value. This is not, in general, true for silver coins.)
P. 318. ... 81. 50 lb .
82. 0.304 o\%. (Troy).
83. 2 s. $8 \cdot 7 \mathrm{~d}$.
84. $6 \cdot 048$ grams. $\quad$ 85. $16 \mathrm{~s} .6 \not \mathrm{ftl}^{2}$.
86. 15s. 104 d . Since 1 franc $=9.513 \mathrm{~d} ., 20$ frames $=15 \mathrm{~s} .10 \frac{1}{4}$. - -showing that the actual value of the gold in a 20 -frane piece is the same as its face value. Hence the interchangeability of the standard gold coins of various countries. 87. 22s. (nearly).
88. $4 \cdot 032458$ grams.
89. $4 \cdot 1667$.
90. 10s. 3d.
91. $5 \cdot 96 \mathrm{~d}$.
92. $20 \cdot 650$-sen piecess rqual one 5 -yen piece.
93. £2 1s. 1 dd. ; and since 1 dollar is worth $49.32 d$. , the gold in a 10 -dollar piece is worth the face value of the coin.
94. I•d.
95. $x 12 \mathrm{~s} .119 \mathrm{~d}$.
96. If a banker applips to the Mint for $£ 2$ worth of silver, he receives forty shillings, and pays in two sovereigns. The actual value of the former is $£ 12 \mathrm{~s} .119 \mathrm{~d}$. less than the latter; hence, if this were all to be considered, the Government could olviously make a very great deal over such transactions.
P. 319.-97. $7 \cdot 06 . \quad 98.8 \cdot 96 . \quad 99.2: 390$ pats. 100. $£ 168 \mathrm{~s}$. (correct to 1 s. ). 101. £36 8s. 1d. $\quad 102.2 .517$ cwt. 103. 40.08 lb .
104. If it were made entirely of iron its weight would be about 5200 tons. 105. 3s. $5 \frac{1}{2} \mathrm{~d}$. per lb.
P. 320.-106. 1 franc 60 centimes. 107. 10s. 8 d . per 56 lb . 108. $4 \cdot 34 \mathrm{~d}$.
109. 822 nails. 110. 181 nails. 111. 6s. (very nearly).
112. $172 \cdot 37$ tons.
P. 321. - 113. 5 fraucs 45 centimes.
114. £1003 3s. 5d. 115. £7 9s. 4d.
116. $3 \cdot 4 \mathrm{~d}$. per lb.
117. $1 \cdot 73 \mathrm{~d}$. per lb. 118. $1 \cdot 23 \mathrm{~s}$. perlb.
119. 18 s .1 d .
120. $19,996,720$ kushels.
121. The price per ton in the United Kingdom is 1.08 time dearer than in the United States.
P. 321.-122. 72,675, 000 tons.
P. 322.-124. 38 Kgm .
126. 328 dollars (correst to 1 dollar).
128. Profit is $£ 327 \mathrm{~s} .8 \mathrm{~d}$.
130. 0.00826 ton.
132. 12894.5 tons.
P. 323.-134. £311265 (nearly).
136. $32,589,286$ tons ; $0 \cdot 336$.
138. 399784 litres.
140. $£ 551 \mathrm{~s} .7 \mathrm{~d}$.
142. $38,398,268$ aeres.
P. 324.-143. $2 \cdot 97$ d. per gallon.
145. $1,839,400$ tons.
147. The error is $+21 \cdot 24 \mathrm{Kgm}$.
149. 475.95 tons.
150. (1) 9713 cub. ft. per ton.
(3) 4.7 gallons per ton.
151. (1) $£ 290$ 18s. 9 d . (2) $£ 262$ s. 8 d .
152. £436. 153. 1 franc 88 centimes. 154. $163 \cdot 9$ francs.
155. £29 7s. greater in Austria than in London.
P. 325.-156. 2s. 8d. 157. $1 \cdot 227$ time dearer in the United Kingdom.
158. 650 hours.

## EXAMPLES. LIX.

## SECTION XIV. TIME

## MISCELLANEOUS QUESTIONS

P. 330. - 1. Column 1-17, 29, 46, 41, 65, 52, 53, 33, 60, 42, 56, 71, 102.
," $2-125,199,161,196,197,278,299,316,307,347$, 159, 315, 263.
2. $15 \mathrm{~min} .53 \frac{1}{4} \mathrm{sec}$.
3. 21 min .7 sec .
4. Total, 60 days 14 hrs. 25 min . ; average, 15 days $3 \mathrm{hrs} .36 \frac{1}{4} \mathrm{~min}$.
5. (1) 61 days and 15 days ; (2) 60 days 14 hrs., and 15 days 4 hrs.
6. 10 hrs .10 min . 7. 12 hrs .56 min .
P. 381. - 8. 45 hrs.
9. $1 \mathrm{~s} .5 \frac{1}{2} \mathrm{~d}$.
10. £3 2s. 10 d .
11. 4398 metres per hr. (correct to 1 ft .).
12. $£ 111 \mathrm{~s}$.
13. 4 hrs. 7 min. ; 11 hrs. 20 min. ; 15 hrs. 53 min. ; $7 \mathrm{hrs} 20 min.$. ; 6 hrs .30 min . ; 7 hrs. 59 min . ; 13 hrs .50 min .
14. $\frac{7}{30} \mathrm{hr}$. 15. $1 \frac{8}{4} \mathrm{~min}$. 16. 15 min ., Wimbledon to Surbiton.
P. 832. 17. 7 min .12 sec .
18. $39133_{4} \mathrm{hrs}$.
19. 4892 francs 19 centimes.
20. £ 25025 is lost.
21. The first earns $£ 28$ s. 4 d . more.
22. 11058 oz . (correct to 1 oz .). 23. $£ 110 \mathrm{~s} .3 \mathrm{~d}$. (correct to 1 d .).
24. $£ 419 \mathrm{~s} .11 \mathrm{~d}$. (i.e. £5).
25. 6451 passengers. 26. $£ 815 \mathrm{~s}$
P. 332.-27. It would be better to emigrate ; the difference would be about $£ 36$ (£36 3s. 4l. .).
P. 333.-28. $35 \cdot 3,44 \cdot 15,28 \cdot 06,24 \cdot 58$ miles per hour.
29. $14 \frac{1}{8} \mathrm{~min}$.
30. 3 days 20 hrs.
31. 75600 tons.
32. Put it on 1 hour.
33. $£ 11898 \mathrm{~s}$.
34. None; for Lisbon observes Greenwich time. Lisbon local time is 39 min . slow on Greenwich.
35. $9.30 \mathrm{p} . \mathrm{m}$.
P. 334.-36. $9.55 \mathrm{a} . \mathrm{m}$.
37. 24 '64 nautical miles per hour.
38. $28 \cdot 37$ statute miles per hour.
39. 0.69 mile per hour.
40. Less by $27 \cdot 57$ statute miles per hour.
41. $6 \frac{1}{2}$ hours fast.
42. $150^{\circ}$. 43. $60^{\circ}$.
44. $6.30 \mathrm{a} . \mathrm{m}$. ; by 32 min .
45. 12 hrs .45 min . ; 31.9 mi . per hour.
46. (1) $13: 59$ knots. $\quad$ (2) 12 days 19 hrs. 47. 600 girders.
P. 335.-48. £316s. 2 d .
49. $£ 7$ 1s. ; dearer by $£ 34 \mathrm{~s}$. 10d. ; i.e. electricity is nearly twice as costly as gas.
50. 667 dollars (nearly). $\quad 51.8977 \mathrm{~m}$. per hr .
52. £ 1311 s .6 d .
53. $£ 131400$.
54. $£ 26257 \mathrm{~s} .5 \mathrm{~d}$. per week, so that $£ 562516 \mathrm{~s}$. is wanted for the last 27 weeks, of which $£ 1318 \mathrm{~s}$. is in hand ; . $\cdot$ deficit is $£ 54948 \mathrm{~s}$.
65. Nearly 37 ; 9 hrs. 29 min ., i.e. $9 \frac{1}{2}$ hrs.
56. $54 \cdot 93$ hrs.
57. 11 days 16 hrs. ; 7 days 12 hrs ; 10 days 1 hr .
P. 336.-58. $£ 2449$ 9. (nearly).
59. £12266 13s. 4d.
60. £3930 9s. (correct to 1s.).
61. $1,565,000$ tons
62. 45 secouds (correct to 1 sec .). 63. 6 min .16 sec . (correct to 1 sec .).
64. 40 min . 55 sec . (correct to 1 sec .).
65. 4 hrs. 37 min .
66. 30 min .13 sec .
P. 337.-68. 2 hrs .5 min .43 sec .
70. $1 \mathrm{~min} .52 \ddagger$ sec. (nearly).
72. 44 hrs. 27 min. (nearly).
67. 30 hrs .
74. Two extra men.
69. $52 \cdot 6 \mathrm{sec}$.
71. 13 min .20 sec .
73. $!1 \mathrm{~s} .3 \mathrm{~d}$.
76. $759^{\circ} \mathrm{W}$.
76. $544^{\circ}$.
77. 2 hrs. $32 \frac{1}{2}$ min.
P. 338.-78. 115.1 miles.

## REVISION QUESTIONS. II

## A. (1)

## SECTION XI.

P. 338.-1. 0.000253 gram less.
3. 8 雱.
2. 85 oz. 16 dwt. 21 grs.
4. 0.0337 pint.
P. 338. - 5. 30 quarts.
7. £2 5s. (very nearly).
6. $£ 14$ 1s. (very nearly).
8. 17 s .3 d .
9.

P. 339.-10.

| Metres. | Yards. |
| :---: | :---: |
| $1=1 \cdot 093633$ |  |
| $2=2 \cdot 187266$ |  |
| $3=3 \cdot 280899$ |  |
| $4=4 \cdot 34582$ |  |
| $5=5 \cdot 68165$ |  |
| $6=6.661798$ |  |
| $7=7 \cdot 655431$ |  |
| $8=8.749064$ |  |
| $9=9.842697$ |  |

11. 0.4047 .
12. Cost is $£ 1015 \mathrm{~s}$. ; overcharge is 16 s .
13. $£ 2556 \mathrm{~s} .6 \mathrm{~d}$.
14. 27 s . 5 d .

## A. (2)

For the actual forms of invoice the student is referred to Section XI. C. and Plate IX., but he should make out the invoice in full.

P. 339. - 2. The items cost-

3. The amounts are-

4. The amounts aro-


Receipt as usual.
P. 340. -5.

| £12 120 |  |
| :---: | :---: |
| - 168 |  |
| 3100 |  |
| $\begin{array}{lrr}1 & 1 & 8 \\ 0 & 12 & 6\end{array}$ |  |
| 0126 |  |
| $£ 181210$ | $£ 181210$ |

Sen \& 168.
P. 340. 6. For Statement see $\S 155$, p. 211. Amount outstanding is $£ 515 \mathrm{~s} .4 \mathrm{~d}$
7. Make this out carefully.

8. Work carefully through this as in $\S \S 158-170$, drawing up a facsimile cheque for yourself. The entry in vendor's Sales Book will be-

| No. of In"oice. | Date. | Particulars. | Ledger Folio. | £ s. $\quad$ d. |
| :---: | :---: | :---: | :---: | :---: |
| 63 | July 12 | $\begin{gathered} \text { J. Rogers- } \\ \text { Fish } \end{gathered}$ | 53 | 8140 |

In vendor's Returns Inwards Book there will be an entry for $£ 2$ (§ 177), and Mr. Rogers will receive a Credit Note (Plate VIII., pace 224).
The amounts are-13s. 6d., £1 7s. 6d., £1 4s., £1 5s., £1 8s., £1, £1 16s. ; total, £8 14s.
B. (1)

## SECTION XII.

P. 841. - 1. £1380.
2. $£ 1472$.
3. $£ 47270$.
4. 83 pieces.
5. 6 in .
6. 2, and 80 yds. over.
7. $82 \mathrm{ft} .10 \frac{1}{2} \mathrm{in}$.
8. 18 in .
9. Dimensions, in cm., $14.6 \times 9.525$; $20.32 \times 13.335 ; 25 \cdot 4 \times 15.875$; $27.94 \times 19.05 ; 38.1 \times 25.4$.
B. (2)
P. 342. - 1. 63.976 cm .
2. $43 \cdot 18 \mathrm{~cm}$.
3. 48 ft . of $\frac{3}{8} \cdot \mathrm{in}$. wood and 8 ft . of $\frac{8}{4}-\mathrm{in}$. wood.
4. 4 s .10 4 d.
B. (3)

1. Length, 102 in ., i.e. 8 ft .6 in . ; width, $2 \mathrm{ft} .1 \frac{1}{2} \mathrm{in}$. (nearly).
2. 60 ft . $\begin{aligned} & \text { 3. } £ 472 \mathrm{~s}, 10 \mathrm{~d} \text {. }\end{aligned}$
P. 344. - 4. 946.6 ft . for the two lines of rails.
3. 5s. 1d. 6. 1274 ft .
4. $£ 1918 \mathrm{~s}$. (correct to 1s.).
5. 43 lamps ; $1 \frac{7}{8} \mathrm{~d}$.
6. 59 francs (nearly).
B. (4)
7. $372 \cdot 6,362 \cdot 9,566 \cdot 1 \mathrm{Km}$.
8. $14 \cdot 26 \mathrm{mi} . ; 4 \cdot 7 \mathrm{ft}$.
9. 4 min. 5 see.
10. 2.77 mi .
11. 0.509 mi . There are about five times as many miles of railway per thousand people in the United States than in the United Kingdom, but since distauces are so much greater in the States this is not surprising.
P. 845. - 6. 242 skirts. 7. $£ 1211 \mathrm{~s} .8 \mathrm{~d}$.
12. 2.77 d . each, and 13 s .10 d . per week (nearly).
C. (1)

## SECTION XIII.

1. 3 sq. ft. 108 sq . in.
2. 2 s .3 d .
3. 1029 sq . yds. (short side is front).
4. 4042 .
5. $£ 9414 \mathrm{~s}$. (correct to 1 s. ).
P. 346. - 6. $47_{1}^{12} \mathrm{lb}$.
6. $1.01 \mathrm{sic} . \mathrm{mi}$.

> C. (2)

| 1. $1 \cdot 414 \mathrm{in}$. <br> 2. 10.75 cm . <br> 3. $\mathrm{T}^{4} 9=\frac{0}{2}=0$. <br> 4. Area $=504.86 \mathrm{sq}$. ft. ; cost, $£ 44 \mathrm{~s}$. (correct to 1 s .). |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P. 347. - 5. $0 \cdot 694$. <br> 6. $10.21 \mathrm{sq} . \mathrm{cm}$. <br> 7. 3339 sq <br> 8. 267 sq. in. (correct to 1 sq . in.). |  |  |  |  |  |  |  |
| C. (3) |  |  |  |  |  |  |  |
| $\begin{array}{lll}\text { 1. } £ 3334 \mathrm{~s} \text {. (nearly). } & \text { 2. } 3164 \text { francs. } & \text { 3. } 1160 \cdot 25 \text { francs. } \\ \text { 4. } 8878 \text { marks. } & \text { 5. } 136975 \text { marks. }\end{array}$ |  |  |  |  |  |  |  |
| 6. $161914 \cdot 6$ francs per Ha <br> 9. 0.4307 ton. <br> 10. $954,803,200 \mathrm{Ha}$; 18.72 times larger. |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| P. 348, - 11. 344794 , to nearest sq. mile. 12. $935 \cdot 27 \mathrm{sq} . \mathrm{ft}$; total cost, £1473 |  |  |  |  |  |  |  |

I. (1)

## SECTION XIV.

P. 348. - 1. $1171_{8}^{7}$ cub. ft.
2. $£ 1405 \mathrm{~s}$.
3. 10565 lb ., or 4.7166 tons.
4. 1.0984 Kgm .
5. 27.752 lb . See answer to Question 4, Ex. LV.
6. £3 16s. 4d.
7. 8 oz .
D. (2)

1. 1.8715 cul . ft.
P. 349. - 2. 292 gallons.
2. 875 gallons.
3. 11218 cml . ft.
4. $1{ }^{2 \frac{5}{4} 4}$.
5. 1224 loads.
6. $9 \cdot 63 \mathrm{cub}$ ft.
7. Side, 1 inch ; top, $1 \cdot 8$ inch ; 1 cub. ft. 336 cub. in.
8. $562 \frac{1}{2}$ tons.
D. (3)
9. 13.5 cm .
10. 1.766 m.
11. $1 \cdot 132 \mathrm{cmb}$. m .
12. $39 ; 195 ; 32 \cdot 5 \mathrm{~cm}$.
13. 3.6 times.
14. (1) 21 . (2) 33.
15. 0.5 shipping ton ; 7s. 6 d . freight charge.
P. 350. - 6. 275 cub. ft.
E. (1)

## SECTION XV.

1. $2 \mathrm{~s} .8 \frac{1}{2} \mathrm{~d}$.
2. $\frac{1}{2} \mathrm{~d}$.
3. 3 s . $3 \frac{1}{2} \mathrm{~d}$.
P. 351. - 4. Former year higher by $0 \%$ ed. per oz.
4. $26 \cdot 9 \mathrm{~d}$. per oz. (eorrect to $1_{1}^{1} \mathrm{~d}$.).
5. $£ 23,687,740$ (correct to $£ 10$ ); $224,410,163$ roubles.
E. (2)

> 1. 2s. 5d. (nearly).
> 2. 17 tons 4 cwt .
> 3. $£ 4824 \mathrm{~s}$.
> 4. 291 tons.
> 5. 1 lb .
> 6. 3739 gallons.
> P. 352. - 7. $22 \cdot 86 \mathrm{lb}$. ; £5 14s. 1d.
> 8. $218 \cdot 726$ fathoms ; 13208 gallons.
> 9. $£ 125000$.
> 10. $8 \cdot 8 \mathrm{~d}$. per piut.

## E. (4)

P. 353. - 1. $\frac{1}{6}$ d. (nearly). $\quad$ 2. $51 \cdot 559$ francs.
3. 1.9254 cub . in. ; weight $=0.486 \mathrm{lb}$., i.e. $\frac{1}{2}$ lb. (nearly).
4. London, by about $\frac{1}{3} \mathrm{~d}$. per lb . $\quad 5.20 \mathrm{lb}$. (nearly).
6. 1 ton 4 ewt. 2 qrs.
7. 1 ton 3 cwt. 2 qrs. Yield from United States is 1 cwt . per acre less than from Australia.
P. 354. - 8. Place in a third column, "Price per lb.," and underneath write 0.7357 and 0.9334 .
9. 0.175 and 0.216 franc per Kgm .
10. $£ 842 \mathrm{l} 6 \mathrm{~s}$.
11. 0.16 mark per Kgm.
F. (1)

## SECTION XVI.

1. 2 hrs. $22 \cdot 6 \mathrm{~min}$.
2. $46 \cdot 3$ miles per hr. $\quad$ 3. $£ 392 \mathrm{~s} .6 \mathrm{~d}$. ; f dd,
3. $1 \cdot 16 \mathrm{~d}$. per hr.
4. £21 8s. 2t d. (nearly).
P. 355. - 6. 2448 cub . m.
5. 3 hrs. 10 min . ; 18.95 knots.
F. (2)
6. 14 min 2. The first ; 1 hr .6 min .
7. 32 t (uearest half-day above).
8. 160 (very nearly), 320 (very nearly), $£ 3627$, $£ 1707$.
9. 32552 tous (correct to 1 ton).
10. 107 gallons.
P. 856. - 7. 8.5 seconds.
11. £3 19s. 71 d.
12. 134 min .

EXAMPLES. LX.

## SECTION XVII. A. (1)

## PROPORTION: $\alpha$. DIRECT; $\beta$. INVERSE

P. 358. - 1. $£ 24$.
2. 16s.
3. $1 \mathrm{~s} .1 \frac{1}{1} \mathrm{~d}$.
4. 336 ft .
P. 359. - 5. $£ 70$ 11s.
6. $£ 3613 \mathrm{~s} .4 \mathrm{~d}$.
7. 4 s. $1 \frac{18}{8} \mathrm{~d}$.
8. $\frac{1}{3}$.
9. $4 \frac{4}{8}$ days.
10. 2 s . $0 \frac{1}{2} \mathrm{~d}$.
11. $121500 \mathrm{sq} . \mathrm{mi}$.
12. 7s. 7d.
13. $£ 2,675,000$.
14. $£ 3,595,580$ (correct to $£ 10$ ).
15. $£ 5128$.
P. 360.
16. 30330 barrels
17. $£ 887720$.
18. £485190. Rising.
19. $£ 125420$ (correct to $£ 1$ ). 20. Yen $614140 . \quad$ 21. $£ 15$ 18s. 6 d .
22. 16s. 6d.
23. Last year cost was $\$ 0 \cdot 21257$ per lb. Year before last cost was $\$ 0 \cdot 21743$ per lb. ; $\therefore$ price fell slightly.
24. 31 days.
25. 2 es days approximately.
26. 70 men more; i.e. 155 in all.
P. 361. - 27. 650 guineas.
29. 242 lb . (correct to 1 lb .)
31. 3.26 lb . per day.
34. $\frac{1}{6}$ (or $0 \cdot 167$ ) pint.
37. 39 men.
P. 362.-38. 0.644 cub . ft.
39. 104 metric tons.
40. 48 mi . per hour.

EXAMPLES. LXI. (a)
SECTION XVII. A. (2)
TEMPERATURE
P. 363. - 1. $20^{\circ}, 30 \cdot 4^{\circ}, 36 \cdot 8,240^{\circ},-10^{\circ} \mathrm{R}$.
2. $275^{\circ}, 31 \cdot 25^{\circ}, 475^{\circ}, 50^{\circ},-25^{\circ} \mathrm{C}$.
3. $75 \cdot 2^{\circ}, 96 \cdot 8^{\circ}, 111 \cdot 2^{\circ}, 5^{\circ} \mathrm{F}$.
4. $65.75^{\circ}, 88^{\circ} 25^{\circ}, 117.5^{\circ}, 9.5^{\circ} \mathrm{F}$.
5. $17 \cdot 78^{\circ}, 44^{\circ} 44^{\circ}, 37.44^{\circ}, 98.89^{\circ} \mathrm{C}$.
6. $10.67^{\circ}, 74.67^{\circ},-1 \cdot 77^{\circ}, 0^{\circ} \mathrm{R}$.
7. $37 \cdot 44^{\circ} \mathrm{C}$. 8. $2732^{\circ} \mathrm{F}$.
P. 364.
9. $3.33^{\circ} \mathrm{C}$.
10. $1763.6^{\circ}, 1947 \cdot 2^{\circ}, 1985^{\circ}, 3100^{\circ} \mathrm{F}$.
11. $7232^{\circ} \mathrm{F} ., 3200^{\circ} \mathrm{K}$.
12. $287.78^{\circ} \mathrm{C}$.

EXAMPLES. LXI. (b)
SECTION XVII. A. (2)
TEMPERATURE (GRAPHICAI)
P. 365. - 1.

P. 365.-2. The results should agree fairly closely, e.g. $40^{\circ} \mathrm{R}$. gives $50^{\circ} \mathrm{C}$. 3.

4. See 2 above.
5. Take any two temperatures, $e . g .30^{\circ} \mathrm{C} .=86^{\circ} \mathrm{F}$., and $40^{\circ} \mathrm{C} .=104^{\circ} \mathrm{F}$., and then start from $25^{\circ} \mathrm{C}$. or $77^{\circ} \mathrm{F}$. and draw graph as shown ; then the part between the crosses is alone required. We drew the line longer than was necessary to ensure greater accurary. $104^{\circ} \quad \mathrm{F} .=$ $40.0^{\circ}$ C., i.e. $60.0^{\circ} \mathrm{C}$. below the boiling. point.


# EXAMPLES. LXII. <br> SECTION XVII. B. (1) 

## PARTNERSHIP

P. 368. - 1. £900, £720.
2. The second receives $£ 65210 \mathrm{~s}$. more than the first, and $£ 217$ 10s.
more than the third. 3. $£ 7200$.
4. $£ 4002 \mathrm{~s} ., £ 8004 \mathrm{~s}$., $£ 10005 \mathrm{~s} ., £ 12006 \mathrm{~s}$.
5. $1,1_{1}^{9} 5,1 \frac{1}{2}, 2 \frac{1}{6}$.
6. £360, £684, £540, £780.
7. $£ 500, £ 250, £ 625$.
8. £131 5s., £261, £112 10s.
P. 869. - 9. $60: 27: 70$, i.e. $1:{ }_{29}^{9}: 1 \frac{1}{6}$. 10. £1011 4s. 2d.
11. $£ 70, £ 85$, $£ 4210 \mathrm{~s}$., $£ 104$.
12. $£ 4617 \mathrm{~s} .6 \mathrm{~d} ., £ 6210 \mathrm{~s}, £ 782 \mathrm{~s} .6 \mathrm{~d} ., £ 9315 \mathrm{~s}$. 13. 14 d.
14. 6 s . $11 \frac{1}{2} \mathrm{~d} ., 2 \mathrm{~s}$. $3 \frac{1}{2} \mathrm{~d} ., 16 \mathrm{~s}$. 6 d .
15. £1 11s. 3d., £2 4s. 2d., £1 9s. 7d.
16. Proportion of rent, $£ 189 \mathrm{~s} .5 \mathrm{~d}$. ; proportion of profits, $£ 6610 \mathrm{~s}$.
17. £1 $16 \mathrm{~s} .1 \frac{1}{2} \mathrm{~d}$., $£ 14 \mathrm{~s} .1 \mathrm{~d} ., 12 \mathrm{~s} .0 \frac{1}{2} \mathrm{~d} ., £ 312 \mathrm{~s} .3 \mathrm{~d}$.
P. 370.-. 18.

| Income. | Profit. |
| :---: | :---: |
| 3000 milreis. | $1223 \cdot 5$ milreis. <br> $6666 \cdot 7$ <br> 13333.3,$"$ |

19. £184 11s. 9d., £49 12s. 4d., £49 4s. 6d., £413 9s. 6d.

## EXAMPLES. LXIII.

SECTION XVII. B. (2)

## RATES

P. 373. - 1. $£ 2915 \mathrm{~s} . \quad$ 2. $£ 41$ 1s. 4 d .
3. $£ 2608 \mathrm{~s} .4 \mathrm{~d} ., £ 250, £ 2815 \mathrm{~s} ., £ 291 \mathrm{13s}$. 4d., and $£ 10836 \mathrm{~s} .8 \mathrm{~d}$.
4. Net amual income is (1) $£ 11486 \mathrm{~s}$. 8 d., (2) $£ 1440$; so that the second is better for the landlord by $£ 291$ 13s. 4d., and it would certainly be better to adopt it, provided the chance of keeping the houses occupied was the same in both cases.
E. $£ 3710 \mathrm{~s}$.
6. $£ 2,144,000$.
7. $2 \frac{3}{4}$ d. (nearly).
8. £9 14s. 10d.
9. First, $£ 558 \mathrm{~s} .4 \mathrm{~d}$. ; second, $£ 69 \mathrm{3s} .9 \mathrm{~d}$.
10. £78.
P. 374. - 11. $£ 6,608,000$. 12. First, $£ 108$ 6s. 8 d. ; second, $£ 130$ 13s. 4d.
13. Rent and rates for first, $£ 1076$ s. 8 d . ; rent and rates for seecad, $£ 1256$ s. 8d. Increase, $£ 18$.
14. $£ 794$ 12s. 6 d,

## EXAMPLES. LXIV.

## SECTION XVII. <br> B. (3)

## TAXES

P. $376 .-1 . £ 291$ 3s. $4 \mathrm{~d} ., £ 217$ 10s., $£ 1793 \mathrm{~s} .4 \mathrm{~d}$.
2. $£ 2614 \mathrm{~s} .9 \mathrm{~d}$.
3. $£ 561 \mathrm{ss} .1 \frac{2}{2} \mathrm{~d}$.
4. $£ 315718 \mathrm{~s}$.
5. £723 15 s .
6. 11 d .
7. 1 s.
P. 377. - 8. £469 19s. 5d. (nearly) and £187 19s. 9d. 9. £519s. 6d.
10. £434 13s. 9d.
11. $£ 9558 \mathrm{~s} .4 \mathrm{~d}$.
12. 7 s .4 d .
13. $£ 1,531,250$.
14. $£ 6216053 \mathrm{~s} .4 \mathrm{~d}$.
15. $£ 1,017,51112 \mathrm{~s} .8 \mathrm{~d}$.
16. $£ 60$.
P. 378. - 17. £ 280 , £ $220, £ 336$.
18. £31 7s.

## EXAMPLES. LXV.

SECTION XVII. B. (4)
PROPERTY
P. 379. - 1. Tabulate thus:

| Cost of Building. | Annual Income. | Rate per Cent. |
| :---: | :---: | :---: |
| $£ 50000$ | $£ 8000$ | 16 |

The remaning answers ( 2 to 8 ) are :
2. $10.53 \%$.
3. $2 \cdot 103 \%$.
4. $5.2 \%$
P. 380. - 5. $6.3 \%$.
6. $4 \cdot 94 \%$.
7. $35.53 \%$.
8. $7.63 \%$.
9. $£ 7032$.
10. £135000.
11. $£ 2336 \mathrm{12s}$. 6 d .
12. 12000 guineas.
13. £955.
14. 12500 dollars.
15. $12,112,500$ francs.
16. 587 francs.
17. 125000 dollars.
18. 7639 gulden.
19. 4,350,000 lire.
20. $£ 422475$.
21. £291 7s. 6d.
22. (1) 29.
(2) 14.
(3) 13.
(4) $7 . \quad$ (5) 5.
(6) 4.
(In each case to the nearest year above.)
23. (1) $14 \div 29$.
(2) 12.5 .
(s) 6.67 .
(4) 8.
(5) $5 \cdot 4$.
(6) $4 \%$.

## EXAMPLES. LXVI.

SEOTION XVII. B. (5)

## INSURANCE

P. 884. - 1. 5s. 9d. (very nearly).
4. $£ 106$ 1s. 11d.
5. 1s. 3d. ordinary stock ; 3s. 9d. inflammable part.
6. (1) $£ 63510 \mathrm{~s}$.
(z) $15 \mathrm{~s} ., 12 \mathrm{~s} .6 \mathrm{~d}$.

PART II.—2
P. 384. - 7. Messrs. Stoor \& Co. To the Beadle Ingurance Corporation.

8. He pays in premiums $£ 50113 \mathrm{~s}$. 4 d ., and receives $£ 974 ; \therefore$ he gains $£ 472$ 6s. 8 d .
P. 385. - 9. Promiums are $£ 246$ 9s. 2d. and $£ 194$ 13s. 9d. Profits made are $£ 203$ 10s. 10d. and $£ 556$ 6. 3 d . respectively ; $\therefore$ his gain by following my advice to take out a "With Profits" policy is $£ 1484 \mathrm{~s}$. 7 d .
10. £847 7s. 6d. loss to the company.
11. The payments are respectively-£8 12s., £5 15s. 2d., £7 4s.

The compensation-£179 4s., £119 9s. 4d., £149 6s. 8d.
12. Gained $£ 1611 \mathrm{~s} .2 \mathrm{~d}$. 13. 465 francs ( $£ 188 \mathrm{~s} .8 \mathrm{~d}$.).
14. 44.75 roubles.
15. 2s. $6 \mathrm{~d} . \%$.
16. Policy, $£ 85819$ s. 1d. ; premium, $£ 219$ s. 1d.
17. 186 lire ( $£ 78$ s.).
P. 386. -- 18. Yolicy, $£ 9979$ 2s. 6 d. ; premium, $£ 419$ 2s. 6 d . 19. $£ 211 \mathrm{~s}$.

## EXAMPLES. LXVII.

## SECTION XVII. B. (6)

## BANKRUPTCY

P. 388. - 1. $£ 62$ 6s.
2. 11s. 6 d .
3. $£ 345$.
4. $£ 143613 \mathrm{~s} .4 \mathrm{~d}$.
5. 12 s . 3 d .
6. $£ 8013 \mathrm{~s}$. 3 d .
7. 2 s .6 d . in the $£$. Actual receipts : $£ 3710 \mathrm{~s} ., \mathfrak{£} 565 \mathrm{5s} ., £ 70, £ 10$.
8. 7s. 6d. in the $£$.
9. $£ 10000$. 10. $£ 2238$ s. 10d.
11. Dividend, $40 \%$; 88600 francs.
12. $£ 4618 \mathrm{~s}$., $£ 14014 \mathrm{~s}$. $£ 23410 \mathrm{~s}$.
13. Assets, $£ 1496$ 18s. 2 d. ; loss, $£ 141$ 2s. 9d. per creditor.
P. 389. - 14. $£ 836$ s. $8 \mathrm{~d} ., £ 160$.
15. 5s. 6 d .
16. $75.8 \%$.
17. $£ 831$ (very nearly).
18. $£ 5950$ 15s.
19. $£ 5315$.
20. 17 s .
21. 9 d . in the $£$.
22. $£ 11052$ 12s. 8 d. Increase in dividend, 2s. 5 d. in the $£$.
P. 390.-23. $£ 3250, £ 74750$.
24. $\Lambda$ dividend of 8 s. 6 d. would need $£ 24777$ 10s. assets ;.$\therefore £ 200$ has been allowed in preferential claims.

## ANSWERS

## EXAMPLES. LXVIII.

## SEGTION XVII. 0.

## CHAIN RULE

P. 392. - 1. 1.0160175.
2. $15 \cdot 432349$.
3. 254 metric tons ; 77161.745 grains $=5$ Kgn .
4. 0.984206.

| Metric <br> Tons. | English <br> Tons. |
| :---: | :---: |
| $1=0.984206$ |  |
| $2=1.968412$ |  |
| $3=2.952618$ |  |
| $4=3.936824$ |  |
| $5=4.921030$ |  |
| $6=5.905236$ |  |
| $7=6.88944:$ |  |
| $8=7.73648$ |  |
| $9=8.857854$ |  |

5. 6.3478 Kgm .
$2=1 \cdot 968412$
6. 10274.78 kgm .
7. 1 oz . Av. $=28 \cdot 3495 \mathrm{gms}$; 10 lb . Av.
$=4.5359 \mathrm{Kgm}$.
8. $6.35 \mathrm{Kgm} . ; 12.7 \mathrm{Kgm}$.
$15 \cdot 61$ tons, $3 \cdot 529$ tons.
9. 1 franc $=0.8100714$ marks ; 5863 francs $=4749 \cdot 5$ marks.

10. $1 \mathrm{qt} .=1 \cdot 1359$ litres ; 80 ks. $=726.976$
litres: 350 bush. $=127 \times 22 \mathrm{Hl}$.
11. 1 litre $=0.880386 \mathrm{qt} . ; 5 \mathrm{l} .6 \mathrm{dl}$. $=9.86032$ pints.
12. £41 13s. 4d.
13. $114 \cdot 2857$ gallons.
14. 6 z hours.
P. 393. - 17. $2918 \cdot 1$ francs. $\quad$ 18. 126.56 rupees, 324.3 dollars, 1827.02 kroner.

## EXAMPLES. LXIX. <br> SECTION XVIII.

## PERCENTAGES, COMMISSION AND BROKERAGE, PROFIT AND LOSS

## A. Percentages

P. 896. - 1. (1) 4.
(2) $\frac{1}{20}$.
(8) $\frac{1}{10} \cdot$
(8) $\frac{3}{28}$.
(4) $\frac{1}{2}$.
(5) $\frac{1}{6}$.
(6) $\frac{1}{2} 8$.
(7) $\frac{18}{8}$.
(9) $\frac{4.3}{10} 0$
(10) $x^{1} 0$.

2. (1) $20 \%$.
(2) $50 \%$.
(3) $25 \%$
(4) $12 \frac{1}{2} \%$.
(5) $10 \%$.
(6) $5 \%$
(7) $4 \%$.
(8) $60 \%$.
(9) $62.5 \%$.
(10) $44.44 \%$.
(11) $93 \cdot 75 \%$.
(12) $41.67 \%$.
(13) $72.41 \%$.
(14) $72 \%$.
(15) $87.09 \%$
(16) $78.95 \%$.
(17) $1.5 \%$.
(18) $5.33 \%$.
(19) $11.25 \%$
(20) $\frac{1}{10} \%$.
3. (1) $£ 1210 \mathrm{~s} ., £ 15, £ 2710 \mathrm{~s} ., \mathfrak{£} 38 . \quad$ (2) $3 \mathrm{~d} ., 4 \frac{1}{2} \mathrm{~d} ., 2 \mathrm{~s} ., 2 \mathrm{~s} .6 \mathrm{~d}$.
(8) £45, £S0 1s., £77 10s.
(4) $£ 11 \mathrm{~s} ., £ 1200, £ 1111 \mathrm{~s}$.
(5) 1s. $0 \frac{1}{4} \mathrm{~d} ., £ 1 \mathrm{ls} .5 \mathrm{~d} ., 6 \mathrm{~s} .1 \frac{1}{2} \mathrm{~d}$. (nearly).
4. $£ 710 \mathrm{~s}$., 㝵 mi., $13 \cdot 05$ ac., $2 \cdot 1$ galls.
6. $65 \cdot 625$ francs ; yen $55 \cdot 125$; $12 \cdot 29$ dollars ; $98 \cdot 25$ in. ; $40 \cdot 741$.
6. 132 yds ., $12 \mathrm{~cm} ., 1 \cdot 25 \mathrm{sq}$. ch., 15 ares, $8 \cdot 7$ lire, 5 tons 0 cwt. 2.4 qrs.
7. $12 \frac{1}{2} \%$.
8. Each equals $£ 0 \cdot 66$.
9. £2100.
10. Tis ac.
11. 1 ton 4 ewt. $2 \cdot 1$ qrs.
12. £1250.
P. 397. - 13. 80 ac.
14. $£ 300$.
15. £3 6s. 6 d .
16. $£ 214 \mathrm{~s} .7 \mathrm{~d}$.
17. £3 !s. $4 \frac{2}{2} \mathrm{~d}$.
18. $£^{2} 8 \mathrm{~s}$ s. $1 \frac{1}{2} \mathrm{l}$. .
19. £5 13s. 43 d .
20. $\mathfrak{£ 8 9}$ \%s.
21. $27 \mathrm{~s} .7 \frac{3}{4} \mathrm{~d}$.
22. £3 6s. 6 d .
23. 4s. 4 : d .
24. \&s. $1 \frac{1}{2} \mathrm{~d}$.
25. 16 ac. $11 \cdot 43$ sq. poles. 26. $151 \cdot 442$ grams.
27. $0.694 \%$.
28. $55.56 \%$.
29. $0.41667 \%$.
30. $21!\%$
31. $1 \cdot 0625 \%$.
32. 143 tons.
33. $7.32 \%$
34. $2 \cdot 148 \%$.
35. $11.85 \%$.
P. 398. -36 . $-12 \frac{1}{2},-14 \frac{4}{4},+33 \frac{1}{3} \%$; the last is the gratest.
37. $20 \frac{5}{8} \mathrm{in}$.
39. $2 \cdot 314 \%$.
41. $11.767 \%$.
43. $20 \%$.
45. $2.435 \%$.
P. 399.-47. $18.06 \%$ and $10.89 \%$.
49. $5 \cdot 23 \%, 1 \cdot 54 \%$. The decrease is becoming less marked.
50. Increase per cent. is $12 \cdot 17$ (1891-1901) and $10 \cdot 9$ (1901-11). Differ. ence, $1 \cdot 27 \%$. Oonclusions : 1. Increase per cent. in population (England and Wales) was much greater in 1811-21 than 1901-11, and the average annual increases were $1.8 \%$ and $1.1 \%$. 2. Average increase per cent. for South America was less than for England and Wales in 1811-21, and more than for 1901-11.

## EXAMPLES. LXX.

## SECTION XVIII.

## B. Commission and Brokerage

P. 401. - I. $£ 25$.
2. £5882 7s.
3. $8.5 \%$.
P. 402. - 4. 8979.45 dollars.
5. $2,142,857$ francs. 6. $£ 74$.
7. $85 \cdot 64$ marks.
8. £240000.
9. £11 14 s .
10. $£ 110$ 11s. 4 d .
11. $£ 140414 \mathrm{~s} .4 \mathrm{~d} ., £ 1087 \mathrm{~s} .1 \mathrm{~d}$.

## EXAMPLES. LXXI.

## SECTION XVIII.

## C. Profit and Loss

P. 405. $-1.5 \%$ 2. $2 \frac{1}{2} \%$ 3. $7 \frac{1}{2} \%$ 4. $3 \frac{1}{2} \%$.
5. $10 \%$.
6. $15 \%$.
7. $-15 \%$.
8. $+27 \%$.
9. $-36 \%$.
10. $-18 \%$.
11. $40.176 \%$.
12. $37.23 \%$.
13. $48 \frac{1}{3} \%$.
14. $51 \cdot 16 \%$.
15. $99.4 \%$.
16. $10.42 \%$.
17. $171 \%$.
18. $19.9 \%$.
19. $9 \frac{1}{3} \%$.
20. $14 \cdot 583 \%$.
21. $5.26 \%$.
22. 1s. $2 \frac{1}{4} d$. (eorrect to the nearest $\frac{1}{4}$ d. above).
P. 406.-23. $14 \% 286 \%$
24. 4s.
25. £49, £6.72.
26. Third is 2570 dollars greater than the first, and 800 dollars greater than the second.
27. $24.4 \%$ loss. 28. $£ 1014 \mathrm{~s}$. ; $26.9 \%$.
29. $£ 7687$ 11s., to nearest 1 s .
30. $£ 1210 \mathrm{~s}$.
31. £19 19s. 6d. $32.30 \%$.
$33.26 \% \quad 34.30 \%$.

## EXAMPLES. LXXII.

## SECTION XVIII.

## MISCELLANEOUS QUESTIONS

P. 406. - 1. $966.67 \%$.
P. 407. - 2. $485 \%$.
3. $41 \frac{2}{3} \%$ water, $58!$ wine.
4. $£^{\prime} 68$ :3s. 8 d .
5. $32.6 \%$.
6. $67.74 \%$.
7. $0.209 \%$; 4.6 lb .
8. $44.694 \%$.
9. $17,691,690$.
10. $6 \cdot 33$, to two places.
11. $7.3 \%$ (nearly).
P. 408. - 12. $£ 69 \mathrm{~s} .7 \mathrm{~d}$. per cwt. ; 1d. jer lb.
13. 3 fr . 30 c . is higher by $23 \cdot 5 \%$ of 2 s . $6 \frac{1}{2}$ d. 14. $6 \cdot 25 \%, 81 \cdot 25 \%$.
15. $22.22 \%, 20 \%$.
16. $18.5 \%$.
17. $38.33 \%$.
18. $61.7 \%$ (nearly).
19. $72,398,000$ tons.
21. $20.6 \%, 26 \%$.
20. $35 \cdot 714 \%, 26 \cdot 315 \%$.
23. 23s. per cwt.
22. $1.34 \%, 0.134 \%$.
24. $1 \cdot 155 \%$.
P. 409.-25. 25s. 2 d .
27. £48908 10s. (nearly).
26. $26.25 \%$.
28. $18 \cdot 75 \%$; 6 s .2 d .
29. 1s. $0 \frac{1}{2} \mathrm{~d}$.
30. $25.45 \%$.
31. $£ 336 \mathrm{~s} .8 \mathrm{~d}$.
32. $15 \cdot 56 \%$.
33. $22.71 \%$; $£ 1130$ 12s. 6 d. 34. £24421.
P. 410. $-35.86 \cdot 1 \%$ 36. $7 \cdot 17 \%$.
38. $14.8 \%$ (nearly).
39. £385 17s. 6d.
37. $8 \cdot 16 \%, 7 \cdot 55 \%$.
40. $£ 717 \mathrm{~s} .6 \mathrm{~d}$.
$\begin{array}{lll}\text { P. 410. - 41. } £ 42082 . & \text { 42. } £ 18 \mathrm{l} 5 \mathrm{~s} .1 \mathrm{~d} . & \text { 43. } £ 187 \mathrm{~s} .7 \mathrm{~d} \text {. }\end{array}$
44. English is higher than Freuch by $£ 3712$ s.
45. $1 \cdot 56,0.00698,8 \cdot 57 \%$.
P. 411.-46. $15,508,000$ (correct to 100). 47. 0.4998 lb . 48. £69 5s. 6d.
49. (1) $£ 200$.
(2) $£ 235$.
(3) $£ 825$ 15s.
(4) £1739 10s.
50. Increase, $0.94 \%$.
51. Decrease, $0.66 \%$.
52. 1s. 6d. per lb.
53. $34,675,500$, to nearest 100 Kgm .
54. 2,888,300, to nearest 100 kr .
55. 1912 price was 0.0834 kr . per Kgm.; 1913 price was 0.0606 kr . per Kgm. ; $\because$ percentage decrease is $27 \cdot 25$ nearly.
56. $33.60 \%$.
P. 412. $-57.62 \cdot 73 \%, 90.42 \%$. There was a big fall in the amount sold, for the Government of India is reducing the sale of this drug year by year, but the market price rose more proportionately than the production fell.
58. £20475.
59. 6s. 2 d .
60. (1) $12 \cdot 18 \%$.
(2) $28 \cdot 12 \%$.
(8) $59.69 \%$.
61. $6.196 \%$.
62. £707 7s. (correct to 1s.).
63. $0.3945 \%$.
64. $4.7 \%$.
65. $5.028 \%$.
66. Decrease, $8 \cdot 1 \%$.
P. 413. $-67.64 .8 \%$.
68. $43.3 \%$.
69. Cost of maintenance, $£ 124$ 11.. 9d. ; profit, $£ 131$ 15s. 3 d .
70. $£ 23 \cdot 87 \%$ (nearly).
71. £11092 5s.
72. $£ 7523$ 2s. 10d.
73. $£ 4513816 \mathrm{~s} .10 \mathrm{~d}$.
74. (1) £3:768, i.e. £3 15 s . $4 \frac{1}{2} \mathrm{~d}$.
(2) $£ 6 \cdot 586$, i.e. $£ 611 \mathrm{~s} .8 \frac{1}{2} \mathrm{~d}$.
(9) $£ 5 \cdot 825$, i.e. $£ 516 \mathrm{~s} .6 \frac{1}{4} \mathrm{~d}$.
75. $74.8 \%$.
76. $54.6 \%$.

## EXAMPLES. LXXIII. (a)

## SECTION XIX.

## DOUBLE ENTRY IN ACCOUNTS

P. 419. - 1. $\$ 279$.
2. $\S 278$ and $\S 279$.
3. $\$ 280$. Capital Account (P), Cash Account (R), Bank Account (R), Horse Account (N), Sheer Account (N), Ink Account (N), Silk Account ( N ).

P. 419.-4.



6. Just the same as 4.

P. 419.-5.

6. As in 4 and 5 .

7. On the heavier side.
8. The Dr. side.
9. (1) That there is a certain amount of money in hand with which to continue business; (2) a Debit halance means that the business owes the capitalist money which it cannot pay, and is therefore insolvent.
10.


He has therefore been allowed to take out more than he put in.
11. The balance of a N. Account represents either a profit or a loss, and therefore adds to, or takes from, the capital of the business, hence its proper place is in the Capital Account.
P. 419. 12. The Dr. entry means that wo have bought $£ 20$ worth of silk, and the $C r$. entry that we have sold some, or all, of it for $£ 30$. The balance is a Cr. balance ; it represents a profit, and is put on the $C r$. side of the P. and L. Account.
13. We have made a profit of $£ 20$.
14. The Dr. balance in Capital Account means that T. Wills owes the business £10, or has overdrawn his Capital Account.
15.




P. 419.-15.


Hence the business has been conducted at a loss of $£ 50$.
EXAMPLES. LXXIII. (b)
SECTION XIX.

## DOUBLE ENTRY IN ACCOUNTS

P. 424.-1. § 287.
2. (a) The balances of all N. accounts are entered in the P. and L. Account on the same side as they appear in their respective accounts. (b) Balances of the Personal and Real Accounts.
3. (a) Dr. side of P. and L. Account would be heavier than Cr. side, so that a $D r$. P. and L. balance means a loss. (b) A $C r$. P. and L. balance means a gain. (c) The Cr. balance of the Capital Account. (d) J. Lee's Account must be looked up. A Debit balance means that he owes us money, and a Credit balance that we owe him money. (e) Dr. side of P. and L. Account. ( $f$ ) Dr. side of Cash Book (Cash column). (g) Dr. side of Bank Book (or Bank column of Cash Book).
4.


| Dr. |  | CASH ACCOUNT. |  |  |  | Cr. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\|\begin{array}{rr} \text { Jan. } & 1 . \\ , & 18 . \end{array}\right\|$ | To Henry James' Capital Account ,, Bicycles . | $\boldsymbol{s}$ 300 100 | 8. ${ }^{0}$ d. | Jan. 10. |  | ¢ 75 75 10 2 313 | 8. d. <br> 0  <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 |
| " 31. | To Balance b/d . |  | 0 0 <br> 0 0 |  |  | 400 | $0-$ |

P. 424.-4.


| $D r$. |  | WACES ACCOUNT. |  |  |  | $C r$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 30. | To Cash | - $\left\lvert\, \begin{gathered} \pm \\ 10\end{gathered}\right.$ | $\left\|\begin{array}{cc}8 . & d \\ 0 & 0 \\ -\end{array}\right\|$ | Jan. 30. | By Balance e/d to P. and L. a/c . |  |




| Dr. | PROFIT AND LOSS ACCOUNT. |  |  |  |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 31. | To Wages <br> " Rent <br> " Net Profit c/d to Capital a/c | $\pm$ <br> 10 <br> 2 <br> 13 <br> 13 | s. $\begin{gathered}\text { d } \\ 0 \\ 0 \\ 0 \\ 0 \\ 0\end{gathered} 0$ | Jan. 31. | By Bicycles . | $\left\lvert\, \begin{aligned} & \text { ¢ } \\ & 25\end{aligned}\right.$ | $\ddot{0}$ | ${ }_{0}$ d. |
|  |  |  | 0 0 |  |  | 25 | 0 | 0 |

P. 424.-4.

5. Just as 4. Net profit is £5.
6. Just as 4 and 5, but open a Bank Account as well as a Cash Account. Net profit, $£ 135$.

## EXAMPLES. LXXIII. (c) <br> SECTION XIX.

## DOUBLE ENTRY IN ACCOUNTS

P. 437. - 1. § 295, § $297, \S 298$.
2. Pp. 226-235; §§ 278-9; § 295 ; §§ 297-8; § $303-5$; § 307.
3. On the $D r$. side.
4. By a Cr. balance.
5. That we have been allowed more by way of discount than wo have allowed other firms.
6. On Dr. side of Stock Account on 1st June; it will be transferred to the Dr. side of the P. and L. Account at the end of the month. On 1st July the new value of stock will appear on the Dr. side of the Stock Account.
7. § 311.
8. To show the amount of the net profit or net loss during the trading period.
9.

10. To Capital, $£ 170$ 10s. (set out as in Question 9).
11. To Capital, $£ 610$ (set out as in Question 9).
12. Purchases Account, Dr., £305 ; T. Williams' Account, Cr., £8; and so for the other Personal Accounts.
P. 437. - 13. (a) Purchases Account, Dr., £626; Personal Accounts, $C r$. for various amounts. (b) Sales $\Lambda$ ccount, Cr., £693. Personal Account, Dr. for various amounts.
14. Returns Outwards Account, Cr., £2 10s. ; John Nelson’s Account, Dr., $£ 2 \mathrm{Jos}$.
15-17. See § 305 , and proceed as shown there.
18. (1)


(2)

(8)


| $D r$. | CASH ACCOUNT. |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Jan. 12. | By Henry Jago | $\xrightarrow{ \pm}$ | $\|$8. d <br> 0 0 |

P. 437.- 18 .

P. 438. - 19 .

(a) Would make a difference of $£ 20$ in the D)r. and Cr. sidesthe Dr. £10 too much; the Cr. £'10 short. (b) Would make the side on which error occurred 19s. short.
20.

## SALES BOOK.

Feb. 3.

5.
W. Humphreys-

6 razors @ 3s. each
5.
L. Townsend-

2 cases fish knives (9) $£ 2$ each.
7.
J. Hearne-

3 doz. pocket knives @ 30s. per doz. Less 5 \%
V. Gunn-
$\frac{1}{2}$ doz. glass match-stands (a) 8s. 3d. each

P. 438.- 20 .

## PURCHASES BOOK.

Feh. 3.
F. Grace-

2 doz pocket knives ( $r 4$ s. 6d. each
"
4. G. Mead-

2 doz. photo frames (dt 5s. 6d. each. Less $10 \%$
B. Lilley-

2 doz. match-stands (as. earh
, 8.
L. Spooner-

6 cases of fish knives @ $£ 3$ each Less $10 \%$



RETURNS INWARDS BOOK.

Feb. 3.
B. Briggs-

1 case carvers (@ $£ 15$ s. each .
"
6. J. Abel-

6 photo frames @ 1s. each



## P. 438.20.



| Dr. | L. TOW | Cr. |
| :---: | :---: | :---: |
| Feb. 5. To Goods |  |  |









| Dr. | B. BRIGGS. |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Feb. 3. | By Returns. | ¢ <br> 1 | s. $\left.\begin{gathered}\text { d } \\ 5 \\ - \\ 0\end{gathered} \right\rvert\,$ |

21. 

Dr. CHAS. DUGMORE: DAPITAL ACCOUNT. Cr.

| Feb. 28. | To Balance e/d | $\underset{147}{ \pm}$ | 8. ${ }_{7}$ | $\begin{array}{\|cc\|}\text { Feb. } & 1 . \\ & ,\end{array}$ | By Uash ${ }_{\text {P Proft }}$ : |  |  | ${ }_{0}{ }_{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 147 | 71 |  |  | 147 |  | 1 |
|  |  |  | $1$ | " 25. | By Balance b/d | 1147 |  | 1 |

PART 11.-3


P. 488.-21.


| TRIAL BALANCL. |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | D | Totals. |  |  | Cr. |  | $D r$. |  | Balances. |  |  | Cr. |
|  | £ | 8. | d. | £ | 8. | d. | $\ddagger$ | 8. | d. | £ | 8. | $d$. |
| Capital | 170 | 0 | 0 |  | - 13 | 0 | 123 | 6 | 2 | 120 | 0 | 0 |
| Goods | 108 | 2 | 5 | 51 | 2 | 6 | 56 | 19 | 11 |  |  |  |
| K. Russell - | 20 | 0 | 0 | 75 | 6 | 8 |  |  |  | 55 | 6 | 8 |
| F. Shepherd - | 21 | 2 | 6 |  | 2 | 6 |  |  |  |  |  |  |
| C. Oliver - |  |  |  | 10 | 12 | 5 |  |  |  | 10 | 12 | 5 |
| Discount Trade Expenses | 1 | 2 10 | 6 6 |  |  |  | 4 | ${ }_{10}^{2}$ | 6 |  |  |  |
|  | 324 | 17 | 11 | 324 | 17 | 11 | 185 | 19 | 1 | 185 | 19 | 1 |

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline Dr. \& \multicolumn{6}{|r|}{PROFIT AND LOSS ACCOUNT.} \& \multicolumn{3}{|l|}{\(C r\).} \\
\hline \begin{tabular}{c} 
Feb. 28. \\
" \\
\hline
\end{tabular} \& \multirow[t]{2}{*}{\begin{tabular}{l}
To Discount . \\
,, Trade Expense \\
", Net Profi transferred \(t\) Capital a/c
\end{tabular}} \& 8
1
4

27 \& S. \& ( $\left.\begin{gathered}d . \\ 6 \\ 6 \\ 1\end{gathered} \right\rvert\,$ \& Feb. 28. \& By Profit from \& £

$$
33
$$ \& 8.

$$
0
$$ \& d

1 <br>
\hline \& \& 3 \& 0 \& 1 \& \& \& 33 \& 0 \& 1 <br>
\hline
\end{tabular}

| BALANCE SHEET. |  |  |
| :---: | :---: | :---: |
| Liabilities. |  | Assets. |
| R. Russell C. Oliver Capital |       <br> .    $£$ 8. |  |
|  | $213 \quad 6 \quad 2$ | 21368 |



## SALES BOOK.

| Feb. | 4. | F. Peters |  | - | - | - |  |  |  | $\underset{25}{\text { ¢ }}$ | 8. | ${ }_{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| " | 8. | C. Griffin | - | - | - | - | - |  | - | 10 | 0 | 0 |
| " | 17. | C. Griffin | . | - | . |  |  |  | . | 11 | 10 | 0 |
|  | 27. | C. Griffir | - | - | - | - | - | . | - | 5 | 10 | 0 |
|  |  |  |  |  |  |  |  |  |  | 52 | 0 | 0 |



|  | JOURNAL. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Feb. 1. | Cash, Dr. . <br> To J. Thomas' Capital Account, Cr | $\stackrel{\text { ¢ }}{100}$ | ${ }_{0}^{8 .}$ | ${ }_{0}^{d}$ | $£$ <br> 100 | 8. |


| Dr. | J. THOMAS |  | CAPITAL ACCOUNT. |  |  | Cr. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Feb. 28. | To Balance c/d | $\underset{139}{\text { £ }}$ | ¢.1 <br> 17 | $\begin{array}{cc}\text { Feb. } \\ \text {, } 1 . & 28 .\end{array}$ | By Cash " Profit | 年 100 39 | 8. $d$. <br> 0 0 <br> 17 0 <br> 17 0 |
|  |  | 139 | 170 | Mar. 1. | By Balance b/d | $\frac{139}{139}$ | $\frac{17}{17} 0$ |



| Dr. |  | R. TAYLOR. |  |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\|\begin{array}{rr} \text { Feb. } & 9 . \\ 0 & 28 . \end{array}\right\|$ | To Cash <br> ,, Balance c/d | $\begin{aligned} & \mathbf{e} \\ & 20 \\ & 20 \end{aligned}$ | 8. $d$ <br> 0  <br> 0  <br> 0  <br> 0  | Feh. 3. | By Goods | ¢ 40 | s. $\mathrm{S}_{0} \mathrm{~d}$ |
|  |  | 40 | 00 |  |  | 40 | 00 |
|  |  |  |  | Mar. 1. | By Balance b/d |  |  |


P. 439.-23.

| Dr | PROFIT AND LOSS ACCOUNT. |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Feb. } 28 . \\ " \end{gathered}$ | To Discount . <br> By Net l'roft to Capital a/c | $\pm$ $s$.  <br> 1 10 0 <br> 39 17 0 <br> 9   | Feb. 28. | By Gross Profft | 4 | ${ }_{8}{ }_{7} \int_{0}$ |
|  |  | $41.7 \mid 0$ |  |  | 41 | 710 |

P. 439.-23.

24.-The Cash Book is shown on opposite page.



P. 439.-24.

P. 439.-24.



| Dr. |  | F. FLETCHER. |  |  |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\|\begin{array}{cc} \text { Dec. } & 9 . \\ " & י \end{array}\right\|$ | To Bank ${ }^{\text {Discount }}$ : | $\\| \begin{gathered} 2 \\ 18 \\ 0 \\ - \end{gathered}$ | 8. $d$ <br> 3 0 <br> 9 0 <br> - 9 | Dec. 29. | By Balance " Goods | 118 <br> 8 | 12 | c/ |




TRIAI, BALANCE.


P. 440.-25.

P. 440.-25.


| $D r$ | P. WALKER'S |  | CAPITAL ACCOUNT. |  |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| June 30. <br> " " | To Jrawings a/c . \#, Balance $\mathrm{c} / \mathrm{d}$ | ( $\begin{gathered}5 \\ 15 \\ 242\end{gathered}$ | g. $d$. <br> 0 0 <br> 0 0 <br>  9 | June 1. „ 30. | By Balance ," Net Profit | $\left\lvert\, \begin{gathered}2 \\ 235 \\ 22\end{gathered}\right.$ | 8. 0 6 | d $\begin{aligned} & \text { d } \\ & 0 \\ & 8\end{aligned}$ |
|  |  | 257 | 6 8 |  |  | 257 | 6 | 9 |
|  |  |  |  |  | By Balance b/d |  | 6 | 9 |


P. 440.-25.




P. 440. 25.


| Dr | L. THOMPSON. |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| June 26.$\ddot{30}$ |  | \|c|c $\begin{gathered} \pm \\ 50 \\ 2 \\ 12\end{gathered}$ | 8.  <br> 10 0 <br> 13 4 <br> 15 0 <br>   | $\left\lvert\, \begin{array}{ccc}\text { June } & 1 \\ \# & 10 . \\ \# & 22 .\end{array}\right.$ | By Ralance ", Goods " | f <br> 15 <br> 37 <br> 12 | 13 10 15 | d 4 0 0 |
|  |  |  | 184 |  |  | 65 | 18 |  |
|  |  |  |  | July 1. | By Balance b/d | 12 | 15 | 0 |



| $D r$. | PROFIT AND LOSS ACCOUNT. |  |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| June 30. <br> 9.95 | To Rates <br> ", Trade Expenses <br> , Net Profit to Capital a/c. | \&  <br> 4 1 <br> 12 1 <br> 22  <br> 2  | s. $d$ <br> 15 0 <br> 0 0 <br> 8  <br> 0 8 | $\left\lvert\, \begin{array}{cc} \text { June } 30 \\ " & " \end{array}\right.$ | By Gross Profit ,, Discount | £ 37 1 |  |
|  |  |  | $1{ }^{1}$ |  |  | 89 | 19 |

P. 440.-26.






P. 440.-26.


| Dr |  | RENT ACCOUNT. |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mar. 29. | To Bank | \|E <br> 5 | s.  <br> $\mathbf{0}$ d <br> 0  | d. Mar. 30. | By P. and L. | $\underset{5}{£}$ | 8. ${ }^{\text {c }}$ d |


| D |  | TRADE EXPENSES ACCOUNT. |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mar. 29. | To Oash | \| $\begin{gathered}\text { £ } \\ 9 \\ 9\end{gathered}$ | ( s. $\left.\begin{gathered}\text { s. } \\ 10\end{gathered} \right\rvert\,$ | Mar. 30. | By P. and L. | £ 9 | 8.  <br> 10  <br> 10 d |


| Dr. |  | DISCOUNT ACCOUNT. |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\lvert\, \begin{gathered} \text { Mar. } 31 . \\ " \end{gathered}\right.$ | To Cash Book ,, P. and L. |  | Mar. 31. | By Cash Book | $\stackrel{1}{8}$ | 8. $d$. <br> 10 0 |
|  |  | 110 |  |  | 1 | 10 |


| $D r$. |  | MRS. B. VERO. |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mar. 9. | To Goods | $\stackrel{ \pm}{7}$ | s. |  | Mar. 28. | $\xrightarrow{\text { By }}$ Cash ${ }^{\text {Discount }}$ | $\pm$ 7 0 | s. 0 5 |  |
|  |  | 7 | 5 | 0 |  |  | 7 | 5 | 0 |





| TRIAL BALANCE. |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  | Ealances. |  |
|  |  | Dr. | Or. |
| Capital | - . | $\pm$ s. $d$. |  |
| $\xrightarrow{\text { Oounds }}$ Office Furniture | . | 620120 380 |  |
| Wages . | $\cdots \quad$. | 38 560 50 |  |
| Rent - : | . . . | 500 |  |
| Trade Expenses | - . . . | 9100 |  |
| Discount. ${ }^{\text {a }}$ | . . . . |  | 150 |
| Mrs. A. Harker J. C. Cooper | - | 330 | 1350 |
| Cash. . | . . . | 43180 | , 5 |
| Bank | . . . . | 28900 |  |
|  |  | 1014100 | 1014100 |


| Dr | PROFIT AND LOSS ACCOUNT. |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\lvert\, \begin{array}{cc} \text { Mar. } 30 . \\ \# & " \\ " & " \\ \hline \end{array}\right.$ | To Wages <br> " Rent <br> ," Trade Expenses <br> ,, Net Profit | $\left\|\begin{array}{c} x \\ 5 \\ 5 \\ 9 \\ 20 \end{array}\right\|$ | $s$. $d$. <br> 6 0 <br> 0 0 <br> 10 0 <br> 0 0 | Mar. 30. | By Gross Profit <br> ,, Discount. | $\left\|\begin{array}{c} £ \\ 38 \\ 1 \end{array}\right\|$ | ${ }_{5}^{11}$ | 0 |
|  |  | 39 | 16 0 |  |  | 39 | 16 |  |



PART II.—4
P. 441.-27. (1) Mrs. Harker, £3 3s.
(2) J. C. Cooper, £135s.
(3) $£ 1020$.
(4) $£ 20$.
(5) $£ 4319$ s. and $£ 289$. "Capital" is a liability, for the business owes it to the capitalist.
28.



| Jr. |  | BANK ACCOUNT. |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dec. 1. | To Cash | $\underset{100}{£}$ | s. |  | Dec. 3. $=10$. | By Goods " Balance c/d | $£$ <br> 68 <br> 37 | 8. 10 10 | 0 |
|  |  | 100 | 0 | 0 |  |  | 100 | 0 | $\underline{0}$ |
| Dec. 3. | To Balance b/d | 37 | 10 | 0 |  |  |  |  |  |



P. 441.-28.




29.

(a) $£ 6000$.
(b) $40 \%$.
(c) $28 \%$.
(d) $15 \%$.
P. 441.-30.



| Dr. J. CUNNINGHAM : CAPITAL AOCOUNT. Cr. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 31. | To Balance c/d | $\underset{668}{¢}$ | 8. $d$ <br> 17 2 <br> 2  | Jan. 1. | By Cash | £ 600 69 | s. $\begin{gathered}\text { d } \\ 0 \\ 17 \\ 0 \\ 2 \\ 2\end{gathered}$ |
|  |  | 669 | 172 |  |  | 669 | $17-2$ |
|  |  |  | 1 | Feb. 1. | By Balance b/d |  | $17 \mid 2$ |


| $D r$. |  | TAKINGS ACCOUNT. |  |  |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 31. | To P. and L. | $\xrightarrow{294}$ | ${ }^{8} 8.8$. | Jan. 6. | By Cash ", ". |  |  |   <br> 8.  <br> $1 i$  <br> 10 2 <br> 10 8 <br> 15 8 |
|  |  | 294 | 17 |  |  | 29 | 94 | 177 |






| Dr. |  | J. BROWN \& CO. |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\lvert\, \begin{array}{cc} \text { Jan. } 24 . \\ " & " \end{array}\right.$ | To Bank <br> ", 1iscount | \|c|$\pm$ <br> 56 <br> 2 |  | Jan. 15. | By Provisions | $\stackrel{£}{59}$ | 8. d <br> 16 2 |
|  |  | 15 | $\underline{16} \underline{2}$ | 1 |  | 59 | $\underline{16}$ |




| Dr. |  | H. GOWE LTD. |  |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\|\begin{array}{c} \text { Jan. } 24 . \\ " \end{array}\right\|$ | To Bank <br> , Discount | $\begin{aligned} & £ \\ & 6 \\ & 0 \end{aligned}$ | 8.8. <br> 10 <br> 8 | d. | Jan. 15. | By Provisions | ${ }_{8}^{2}$ | s.  <br> 18  |
|  |  | 0 | 18 | 3 |  |  | 6 | 18 3 |

Ex. LxxiII. (c)]
ANSWERS
P. 441.-30.

| $D r$. | R. JOKER. | $C r$ |  |
| :---: | :---: | :---: | :---: |
| 1 |  |  |  |



| Dr. PROEIT AND LOSS 4 | OOUNT. | Cr. |
| :---: | :---: | :---: |
|  | By Takings ${ }_{\text {\% }}$ Iliscount. |  |


| BALANCE SHEET. |  |  |
| :---: | :---: | :---: |
|  | Labilities. | Assets. |
| $\underset{\text { R. Joker }}{\text { R.tal }}$ |  |  |
|  | 680146 | 686146 |






| $D r$. | A. COLE : CAPITAL ACCOUNT. |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Aug. 30. | To Balance c/d | $\underset{241}{ \pm}$ | 8. d. <br> 17 4 <br>   | Aug. 1. | By Bank " Net Profit | £ 240 1 | 8. 0 17 | $d$. 0 4 |
|  |  | 241 | 17. 4 |  |  | 241 | 17 | 4 |
|  |  |  | 1 | Aug. 30. | By Balance b/d | 241 | 17 | t |

P. 442.- 31 .


| $D r$. |  | FRUIT ACCOUNT. |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Aug. } 30 . \\ " \quad " \end{gathered}$ | To Purchases Hook | $\left\lvert\, \begin{gathered}\text { ¢ } \\ 165 \\ 10\end{gathered}\right.$ | 8.8.  <br> 13  <br> 7 8 <br> 7 8 | Aug. ${ }^{4}$ | By Cash <br> ,, Sales Book | ( $\begin{gathered}\text { £ } \\ 132 \\ 43\end{gathered}$ | 14. | 0 |
|  |  | 78 | 0 |  |  | 176 |  |  |




| Dr. |  | WAGES ACCOUNT. |  |  |  |  | Or. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\|\begin{array}{cc} \text { Aug. } & 8 . \\ \# & 20 \\ " & 27 . \end{array}\right\|$ | To Cash ,, Bank " " |  <br> 3 <br> 7 <br> 4 | 4 17 15 2 | d. | Aug. 30. | By P. and L. | $\stackrel{¢}{15}$ | $\stackrel{8}{14}$ | ${ }_{9}$ |
|  |  | 15 | 14 | 9 |  |  | 15 | 14 |  |


P. 442.--31.









P. 442.-32.

P. 442.-32.


PURCHASES BOOK.


SALES BOOK.





| Dr. | J. BEALE \& CO. |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| July 6. \| To Bank <br> " " " Balance $\dot{c} / \mathrm{d}$ : | \|l|¢ <br> 30 <br> 82 <br> 18 |  |  | July 3. <br> " " <br> , 4. | By Goods " | ¢ 110 2 |  | 8. $\begin{aligned} & \text { d } \\ & 0 \\ & 0 \\ & 6\end{aligned}$ |
|  | 112 | 2 | 6 |  |  |  |  | 6 |
|  |  |  |  |  | By Balance | 82 |  | 26 |



## P. 442.-32.

| Dr. | T. FISHER. |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | \|||July 3. | By Goods | ¢ |  | ${ }^{\text {d. }}$ |






| Lr |  | DISCOUNT. |  |  |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| July 8. | To P. and L. | 2 1 | 8. | . | July 8. | By Cash Book | 2 1 |  | $1{ }^{\text {d }}$ |




P.448.-38.


PART II. - 5

P. 443.-33.


RETURNS INWARDS BOOK.

P. 443.-33.




| $D r$. |  | TRADE EXPENSES. |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 5. | To Cash | $\\|$¢ <br> 9 | 8. $d$ <br> 12 4 | Jan. 6. | By P. and L. | $\begin{array}{r}\text { 2 } \\ 9 \\ \hline\end{array}$ | $\|$8.  <br> 12  <br> 12 4 <br> 4  |


P. 443.- 33 .

| $D r$. |  | S. WILCOX. |  |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Jan. } 1 . \\ , \end{gathered}$ | Tu Balance . <br> ,, Goods . | ¢ <br> 24 <br> 24 <br> 84 | s. $\begin{gathered}\text { a } \\ 0 \\ 0 \\ 0\end{gathered}$ | Jan. 3. <br> ", <br> ". |  | £ 22 1 84 | s.d.  <br> 16 0 <br> 4 0 <br> 0 0 <br> 0  |
| $\text { , } 6 .$ | To Balance b/d | 108 | 0 0 <br> 0 0 |  |  | 108 | 00 |



| Dr | F. NELSON. |  |  |  |  | Cr. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\text { Jan. } 4 .$ | To Returns. ,, Balance . | $£_{0}$ <br> 178 <br> 178 |  | $\begin{array}{r} \text { Jan. } 1 . \\ " \\ " \\ \hline \end{array}$ | By Balance G Goods | ¢ <br> 98 <br> 83 <br> 8 | s. $\begin{gathered}\text { d, } \\ 0 \\ 0 \\ 0 \\ 0\end{gathered}$ |
|  |  | 179 | $\bigcirc 0$ |  |  | 179 | $\bigcirc$ |
|  |  |  |  |  | By Balance . |  | $13 \mid$ |


P. 443.-33.


| TRIAL BALANCE. |  |  |
| :---: | :---: | :---: |
|  | Balances. |  |
|  | Dr. | Cr. |
| H. Coulthard, Capital Account | £ s. $d$. |  |
| Goods . . . . . . | $\begin{array}{llll}236 & 4 \\ 132\end{array}$ |  |
| $\underset{\text { Machinery . . . . . . . }}{\text { M }}$ | 132 0 <br> 10 16 <br>   <br> 1  |  |
| Trade Expenses | ${ }_{9} 124$ |  |
| Discount | 0160 |  |
| S. Wilcox . | 8400 |  |
| B. Vickers . . . . . . . | 4700 |  |
| F. Nelkon . . . . . . . |  | 17813 |
| B. Harrod . . . . . . . |  | 300 |
| T. Arnold . |  | 1300 |
| Drawings . | $\begin{array}{lll}5 & 0 & 0 \\ \\ 8 & 7 & \end{array}$ |  |
| Oash : Bank | $\begin{array}{llll}28 & 7 & 0 \\ 28 & 17 & 0\end{array}$ |  |
|  | 58213 | 582134 |




## EXAMPLES. LXXIV.

## SECTION XX. A.

## SIMPLE INTEREST



## EXAMPLES. LXXV.

## SECTION XX. B.

## COMPOUND INTEREST

P. 458. -- 1. $£ 92 \mathrm{~s} .8 \mathrm{~d}$.
2. $£ 10 \mathrm{l} 4 \mathrm{~s} .3 \mathrm{~d}$.
3. $£ 1911 \mathrm{~s} .8 \mathrm{~d}$.
4. $£ 4314 \mathrm{~s} .1 \mathrm{~d}$.
5. $£ 45$ 6s. 9 d .
6. $£ 235$ s. 9 d .
7. $£ 942 \mathrm{~s} .8 \mathrm{~d}$.
8. $£ 42 \mathrm{~s} .8 \mathrm{~d}$.
9. £21 6s. 11d.
10. 25315 s .8 d .
P. 457.
11. £18 9s. 2d.
12. £31 10s. 4 d .
13. $4168 \cdot 98$ francs.
14. $£ 492 \mathrm{ss} .6 \mathrm{~d} . ; \mathfrak{} 12 \mathrm{~s} .5 \mathrm{~d}$. 16. $7458 \cdot 76$ dollars.
16. $4168 \cdot 98$ lire.
17. £30 19s. 9d. and 18s. 3d.
18. $£ 912 \mathrm{~s}$. 8 d .
19. £295 18s. 1d.

20. $£ 45013 \quad 5$ (1st) $446 \quad 5 \quad 5$ (2nd) | $£ 4 \quad 0$ |
| :--- |
21. £60 2 s .
22. £2073 12 s .
23. $£ 978$.
24. 228.52 dollars.

## EXAMPLES. LXXVI.

## SECTION XXI. A.

CASH DISCOUNT
P. 459. - 1. § 329-331.
2. $£ 86 \mathrm{~s} .9 \mathrm{~d}$.
3. $£ 11$ 19s. 5 d .
4. £3 5s. 1d.
6. $£ 1 \mathrm{ls}$.
6. 18 s . $0 \frac{1}{2} \mathrm{~d}$.
7. $£ 2115 \mathrm{~s} .9 \mathrm{~d}$.
8. $£ 82 \mathrm{l} 12 \mathrm{~s} .10 \mathrm{~d}$.
9. $£ 84$.
10. £11 16s. 1d.
11. £32 13s.
12. $£ 648 \mathrm{~s} .3 \mathrm{~d}$.
13. 9 s .11 d .
P. 460. - 14. 16s. 0
15. £ 113 s .4 d .
16. $£ 316 \mathrm{~s} .8 \mathrm{~d}$.
17. £8 15s. 6d.
18. $£ 1214 \mathrm{~s} .8 \mathrm{~d}$.
19. £3 12s. 4d.
20. $£ 14 \mathrm{~s}$.
21. 19s. 6 d .
22. £25 12s. 8 d .
23. $£ 10015 \mathrm{~s} .8 \mathrm{~d}$.
24. 100 gaineas.
25. $£ 48$ 19s. 6 d .
26. 16 s .4 d .
27. $£ 104 \mathrm{~s} .9 \mathrm{~d}$.
28. (a) 21s. 9d. ;
; (b) 21s. 3d.
29. £1 6s. 8 d .
30. 16 s .2 d .
31. £31 5 s .
32. $16 \frac{2}{3} \%$
33. (1) 10 s .
34.

P. 461.- 35 .

Jauuary 12, 19-.
Messrs. Brown, Oil Merchants (Vendors),
To Thos. Owen \& Co.

|  |  | $\begin{array}{ccc} \pm & 8 & d \\ 1 & 16 & 0\end{array}$ | £ 8. d. |
| :---: | :---: | :---: | :---: |
| 85 -gallon drums lamp oil . | 4s. 6d. per drum. | $\begin{array}{lll}1 & 16 & 0 \\ 5 & 11 & \end{array}$ |  |
| 340 -gallon casks lamp oil. | 37s. 1d. per cask. | 5113 |  |
| 3 10-rallon casks linseed oil | 3s. 6d. per gallon | $5 \quad 50$ |  |
| 28 -gallon drums linseed (boiled) |  |  |  |
| oil . . . . . . | 3s. 6d. $\quad$ | 2160 |  |
| 3 gallons machine oil . | 1s. 10d. ", | $\begin{array}{lll}0 & 5 & 6\end{array}$ |  |
| $8 \frac{1}{2}$ gallons gas-engine oil . | 2s. 6d. ", | $\begin{array}{lll}1 & 1 & 3\end{array}$ |  |
| 12 2-gallon tins motor spirit, . | 3s. each ". | 1160 |  |
| 5 gallons Bosphorus air-cooled motor |  |  |  |
| oil . . . . . . . | 3s. 6d. per gallon | 0176 |  |
| 12 gallons Oolza (French) oil . | 3s. 3d. ${ }^{\prime \prime}$ | 1190 |  |
| $614-\mathrm{lb}$. tins deep chrome paint | $3 \frac{1}{2} \mathrm{~d}$. per lb. | 146 |  |
| Cash discount, 71 \% | - . - . | $\begin{array}{rrrr}22 & 12 & 0 \\ 113 & 11\end{array}$ |  |
| Casks |  | 060 |  |
| Drums | . | 3150 |  |
| Tins . . . | . . . | 090 |  |
| Jars, etc. - | - . . | $\begin{array}{lll}0 & 5 & 6 \\ & \end{array}$ |  |
| Carriage . . | - . . | $\begin{array}{llll}2 & 4 & 1\end{array}$ | 6197 |
|  |  |  | 27178 |

36. The amounts are, in order-
(1) 18 s .9 d .
(2) 11 s .8 d .
(3) 6 s .6 d .
(4) $11 \mathrm{~s} .5 \frac{1}{2} \mathrm{~d}$.
(5) 7 s .7 d .
(6) 5s. 8d.
(7) 17s. 6d.
(8) 10s. 10 d .
(9) $11 \mathrm{~s} .5 \frac{1}{2} \mathrm{~d}$. (10) 11 s .3 d .
(11) $5 \mathrm{~s} .7 \frac{1}{2} \mathrm{~d}$.

P. 462.-37. 22 \%

## EXAMPLESS. LXXVII.

## SEOTION XXI. B.

## TRADE DISCOUNT

P. 464. - 1. See $\S \S 333$ and 334. Yes. No, to wholesale.
2. £4.
3. $£ 63 \mathrm{~s}$.
4. $£ 7138.2 \mathrm{~d}$.
5. $£ 55$ s.
6. $£ 14$ 1s. 9 d .
7. £17 3s. 2d.
8. $£ 639$ s. 6 d .
9. $£ 25218 \mathrm{~s} .7 \frac{1}{2} \mathrm{~d}$.
10. $£ 386 \mathrm{~s} .4 \mathrm{~d}$.
11. $£ 89$ 16s.
12. $£ 815 \mathrm{~s}$
13. $£ 5$.
14. $£ 1010 \mathrm{~s}$.
15. $£ 1815 \mathrm{~s} .8 \mathrm{~d}$. 16. $£ 45917 \mathrm{~s} .6 \mathrm{~d}$.
P. 464. - 17. £280 12s. 6d.
20. $£ 10016 \mathrm{~s}$. 8 d .
18. £7 10s.
21. $£ 2514 \mathrm{~s} .9 \mathrm{~d}$.
P. 465.-22. $\mathbf{2 5} \%$.
26. $12 \frac{1}{2} \%$.
$23.55 \%$.
27. $62 \%$.
31. $45 \%$.
35. 13 s . $10 \frac{1}{2} \mathrm{~d}$
39. 1184. (nearly)
42. 2s. 6d.
41. $£ 111 \mathrm{~s}$. 3 d .
34. 1s. 8 d .
38. 10 s 6d
41. £1 1 s . da .
P. 466.-46.
24. $25 \%$.
28. $25 \%$.
19. $£ 158$ 13s. 9d.
29. $40 \%$.
32. $£ 14$ 3s. 6d. 33. $£ 110$ s. 8 d .
36. $33 \frac{3}{3} \%$
37. $£ 27$ 7. $4 \frac{1}{2} \mathrm{~d}$.
40. $70 \%$

Discount, $12 \frac{1}{2} \%$.
44. $£ 8$ 3s. 4 d . 43. $5 \%$.

| Subject to Discount. |  |  | Net. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{array}{\|l} £ \\ 12 \end{array}$ | s. | ${ }_{0}^{d .}$ | £ | $s$. | $d$. |
|  |  |  | 21 | 0 | 0 |
|  |  |  | 23 | 2 | 6 |
| 26 | 18 | 6 |  |  |  |
| 6 | 6 | 0 |  |  |  |
| 45 | 4 | 6 | 44 | 2 | 6 |
| 5 | 13 | 1 | 39 | 11 | 5 |
|  |  |  | 83 | 13 | 11 |

Messrs. P. Green \& Sons Ltd. (Vendors), I'o Thomas James.
Date, eto.
Amounts are, in order-

Discount, 20 \% .

| Subject to Discount. |  |  | Net. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| £ | 8. | $d$. 6 | £ | 8. | $d$. |
| 20 | 11 | 9 |  |  |  |
|  |  |  | 3 | 3 | 0 |
| 6 | 3 | 0 |  |  |  |
| 6 | 6 |  | 3 | 12 | 0 |
| 41 | 1 | 3 | 6 | 15 | 0 |
| 8 | 4 | 3 | 32 | 17 | 0 |
|  |  |  | 39 | 12 | 0 |


P. 466.-47. (1) Question 35, p. 461. The total

| etc., and carriage, upon which | £ | s. | $d$. | £ | $s$. | $d$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| no discount is allowed) is | 22 | 12 | 0 |  |  |  |
| Trade discount, $25 \%$. | 5 | 13 | 0 |  |  |  |
|  | 16 | 19 | 0 |  |  |  |
| Cash discount, 5 \% | 0 | 17 | 0 |  |  |  |
|  |  |  |  | 16 | 2 | 0 |
| Casks, drums, carriage, etc. | 6 | 19 | 7 | 6 | 19 | 7 |
|  |  |  |  | 23 | 1 | 7 |

(2) Question 36, p. 461. The total amount (less packages and rail charges) is

| $\begin{aligned} & £ \\ & 5 \\ & 1 \end{aligned}$ | 3. 18 15 | d. 3 32 6 | £ | $s$. | $d$. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 4 \\ & 0 \end{aligned}$ | $\begin{aligned} & 2 \\ & 2 \end{aligned}$ | $\begin{aligned} & 9 \frac{1}{2} \\ & 1 \end{aligned}$ |  |  |  |
| 0 | 16 | 6 | 4 0 | $\begin{array}{r} 0 \\ 16 \end{array}$ | $8 \frac{1}{2}$ 6 |
|  |  |  | 4 | 17 | $2 \frac{1}{2}$ |

For receipts, see page 220.
48. 17 Tํ \%.
P. 467. $49.58 \mathrm{~g} \%$.

## EXAMPLES. LXXVIII.

## SECTION XXI. $C$.

## BANKER'S AND TRUE DISCOUNT

P. 474. - 1. See §§ 338-344.
2. See Plates XIII. and XIV. T. Nunn replaces Sir John Falstaff, and J. Brook Messrs. Quickly.
3. See $\S 8345$ and 347 , and Example 5, p. 473.
4. See 342.
5. See Plate XIV. The amount due is $£ 5012 \mathrm{~s}$. 6 d .
P. 475. - 6. He should certainly reckon true discount, for the difference between that and banker's discount is small only so long as the sum of money, the time the bill has to run, and the rate of interest are small.
7. $£ 349$ 11s. $7 \mathrm{cl} . \quad$ 8. $£ 4836 \mathrm{~s} .9 \mathrm{~d} . \quad$ 9. $£ 545 \mathrm{l} 3 \mathrm{~s}$.
10. $£ 861$ 1s. 10 d .
11. $£ 477$ 14s. 9 d .
12. $£ 574$ 13s. 8 d .
13. $£ 3622 \mathrm{~s} .7 \mathrm{~d}$.
14. $£ 728$ 11s. 9 d .
15. $£ 2500$ s. 3 d .
16. £988 15s. 7d.
17. $£ 378$ 5s. 6 d.
18. $£ 743$ 9s. 7d.
19. $50996 \cdot 75$ francs.
20. $21782 \cdot 4$ dollars.
21. 10893 dollars.
22. 29134 drachmæ.
23. $14484 \cdot 8$ marks.
24. 79100 roubles.
25. 58112 gulden.
26. $£ 2490 \mathrm{~s} .10 \mathrm{~d}$.
27. $£ 5570$ s. 11d
28. $8986 \cdot 95$ francs.


## EXAMPLES. LXXIX. (a)

SECTION XXII. A.

## sTOCKS

P. 486. - 1. § 353.
2. $\$ 8355$ and 356 .
3. (a) § 365 .
(b) Page 480, note 2.
(c) § 355 .
(d) and (e) §356. $(f)(g)$ and $(h) \S 358$.
4. $\S 359$ and foot-note.
5. § 366 .
P. 487. - 6. $£ 150$.
7. $£ 335$.
8. $£ 580$.
9. $£ 1200$.
10. $£ 60918 \mathrm{~s}$.
11. £243 15s.
12. $£ 351$ 12s
13. $£ 6054 \mathrm{~s}$.
14. $£ 5985 \mathrm{~s} .3 \mathrm{~d}$.
15. $£ 3544$ 14s. 2 d .
16. $£ 700$.
17. $£ 126613 \mathrm{~s} .4 \mathrm{~d}$.
18. £1297 14s. 2 d .
19. $£ 1600$.
20. $£ 1650$.
21. £3600.
22. $£ 5400$.
23. £3600.
24. $£ 1600$.
25. $£ 4800$.
26. $£ 456$.
27. £912 10s.
28. £885 16s. 29. £2576.
30. £3125.
31. No; £25 too much.
32. £455.
33. $£ 1200$.
34. $£ 8000$. $35 . £ 35600$.
36. $£ 3600$.
37. $£ 1200$.
38. $£ 3200$.
39. $476 \%$.
P. 488.-40. $6.48 \%$.
41. (1) $£ 215 \mathrm{~s} .8 \mathrm{~d}$.
(2) $£ 216 \mathrm{~s} .6 \mathrm{~d}$
(3) $£ 219 \mathrm{~s}$. 5 c
(4) $£ 218 \mathrm{~s} .1 \mathrm{~d}$.
(5) ££ 19s. 7d. (6) $£ 3$ 3s. 1d. (7) $£ 2$ 19s. $5 \mathrm{~d} . \quad$ (8) $£ 29 \mathrm{~s}$. 9 d .
(9) $£ 2$ 18s. 3d. (10) £2 9s. (11) £2 11s. 6d. (12) $£ 215 \mathrm{~s}$. 3 d .
42. At a premium, Bengal Railway, Canadian Pacific Railway, San

Paulo Railway : the others are at a discount.
43. £60. 44. $£ 6 \cdot 25 \%$ 45. Japanese $5 \%$ @ $91 . \quad$ 46. $9 \cdot 17 \%$.
47. 274 . 48. $£ 250$.
49. £70.
50. £60.
51. $£ 4019 \mathrm{~s}$.
52. $£ 128$.
53. £2 10 s .
54. £216.
55. $£ 6010 \mathrm{~s}$.
56. $£ 810$ s.
57. £52 10s.
58. $£ 120$.
59. £205 2s.
60. $£ 166$ 1s. 11d.
61. $£ 213$ 3s.
62. $£ 390$ s. 7d.
P. 488.-63. $£ 30$ 5s. 2l.
66. $£ 65 \mathrm{~s} .4 \mathrm{~d}$.
P. 489.-69. $£ 5360$.
64. $£ 10$ 12s. 9 d . 65. $£ 1815 \mathrm{~s}$. 10d.
67. $£ 1212 \mathrm{~s} .8 \mathrm{~d}$. 68. $£ 2012 \mathrm{~s}$. 10 d .
70. $£ 7293$.
71. Western Australia $3 \frac{1}{2} \%$.
72. $£ 22$ 14s. 6 had. 73. $£ 50 . \quad$ 74. $£ 720$. 75. $£ 86510$ s.
76. Income . £9126 0

|  | 294115 |
| :---: | :---: |
|  | £12067 15 |
| Income-tax | 70319 |
| Net income | $£ 1136315$ |

## EXAMPLES. LXXIX. (b)

SECTION XXII. A.
STOCKS
P. 490. - 1 .

2. $£ 4218 \mathrm{~s}$.
3. $£ 4002 \mathrm{~s} .6 \mathrm{~d}$.
4. $£ 45216 \mathrm{~s}$. 3 d .
5. £1229 18 s .
6. $£ 1560$.
7. $£ 1312 \mathrm{los}$.
8. $£ 5856 \mathrm{los}$.
9. $£ 640213 \mathrm{~s}$.
10. £665 9s. (nearly).
11. $£ 3192 \mathrm{~s}$.
12. $£ 502$ 2s.
13. $£ 529 \mathrm{l} 6 \mathrm{~s}$.
14. $£ 5655$ 3s. (nearly).
15. £2308 3 s.
16. $£ 2388.9$ d.
17. £281 5 s .
18. £4712 10s.
19. $£ 4012$ s. 6 d .
20. $£ 900$.
21. £252.
22. 81紊童.
23. $£ 615 \mathrm{~s}$.
P. 491. .

## EXAMPLES. LXXX.

## SECTION XXII. B.

## SHARES

P. 493. - 1. § 369.
2. § 372 .
3. $\S 358$.
4. Page 492, note 2.
5. $\S 358$.
6. § 372 .
7. £25000.
P. 494. - 8. $£ 45000$.
9. 40000 .
10. £31250.
11. £14900.
12. $£ 42500$.
13. § 353.
14. $£ 20100$.
15. 2200.
16. 4000 .
17. $£ 34005$.
18. $£ 828000$; 82800 shares.
19. $£ 462000$ to be paid.
20. $£ 1710$. 21. $£ 16210$ s.
22. £133. 23. £1357 10s.
24. 5 s.
P. 495.-25. $£ 161210$ s.
27. £21 17s. 6d.
26. 1743 shares ; 2s. $7 \frac{1}{2}$ d. over.
30. $£ 210 \mathrm{~s}$. profit.
31. £490. 32. 600.
29. 15.
34. 1560.
35. 25 shares; 2 s . 6 d . over.
33. 25 shares.
37. $£ 500$.
38. $£ 550$.
39. $£ 1800$.
40. $£ 217 \mathrm{~s} .6 \mathrm{~d}$. is the price, so that they stand at a premium of $287.5 \%$.
41. 3s. 10d. or $19 \mathrm{~g} \%$.
42. £143 15 s.
43. $£ 7$.
44. $£ 309$ s. $\quad 45 . £ 57 . \quad 46 . £ 16613 \mathrm{~s} .4 \mathrm{~d}$.
P. 496.-47.

|  | Jobber's Turn. | Broker's Price to Client. |  |
| :---: | :---: | :---: | :---: |
|  |  | For Selling. | For Buying. |
| (1) | $\frac{1}{8}$ | ${ }_{366^{\frac{3}{4}}}^{128}$ | $12 \frac{7}{4}$ <br> $36+1$ <br> 18 |
| (3) | $\frac{5}{8}$ | ${ }_{4}$ | ${ }_{4}{ }_{3}{ }^{\text {g }}$ |
| (4) | 6 d | 25 s . | 26 s. |
| (5) | 3d. | 8s. 9d. | 9 s . 6d. |
| (6) | $\pm$ | $44{ }^{18}$ | 4448 |
| (7) (8) | $\stackrel{\text { d }}{\text { d }}$ | 1s. 2 d . | 18. ${ }^{13+3}$ d. |

48. $£ 3618710$ s.
49. £214065s.
50. £2660.
51. $£ 82065 \mathrm{~s}$.
52. $£ 562$ 10s., $£ 565$ s. ; $\$ \$ 166$ and 167 , Plate VI., p. 220.
53. $£ 12$ left ; income, $£ 151$ 2s. 3d.
54. $£ 37$ 10s., jobber ; $£ 75$, broker.

## REVISION QUESTIONS. III.

## A. (1)

## GECTION XVII. A. (1)

P. 497. - 1. 5s. 6d.
2. $£ 517 \mathrm{~s} .6 \mathrm{~d}$.
3. 9375 sq. yds .
4. $£ 17$ 12s.
5. $£ 5184$.
6. Increasing ; $2 \cdot 136$ per thousand in 1911 to $2 \cdot 161$ in 1912.
7. $£ 5000, £ 3500, £ 1500$.
8. 40 hours.
9. $£ 656$ 13s. 4 d .

## A. (2)

P. 498. - 1. 3,139,650 galls. (correct to 10 galls.).
2. 110000 dollars; less by 19000 dollars ; market improving.
P. 498. - 3. £4.
4. $66 \frac{2}{2}$ miles per hour.
6. 12 sq . ft. each.
6. Reduction should be 4 in .
A. (3)

1. (a) $£ 125$.
(b) $£ 160$.
(c) $£ 18710 \mathrm{~s}$.
2. $£ 408, £ 918, £ 1020, £ 1632, £ 663$.
3. (a) $£ 315(+£ 450)$.
(b) $£ 522(+£ 300)$.
(c) $£ 900$.
P. 499. - 4. (a) $£ 133612 \mathrm{~s}$. and $£ 17 \mathrm{~s} .10 \mathrm{~d}$. (b) $£ 200418 \mathrm{~s}$. and $£ 21 \mathrm{~s} .9 \mathrm{~d}$.
(c) $£ 26734 \mathrm{~s}$. and $£ 215 \mathrm{~s} .8 \mathrm{~d}$.
(d) $£ 334110$ s. and $£ 39$ s. 7d.
A. (4)

## SECTION XVII. B. (1) to B. (5)

1. $£ 668 \mathrm{~s}$.
2. Kensington produces the greater amount by $£ 381800$.
3. 7s. 3d.
4. $£ 54212 \mathrm{~s} .6 \mathrm{~d}$.
5. £11 10s.
6. $£ 25018 \mathrm{~s} .9 \mathrm{~d}$.
7. £11 13 s .
P. 500. -- 7. £174 14s. 6d.
A. (5)
8. $\frac{1}{8} \%$.
9. $£ 188$ 1s. 4 d .
10. 8s. 4 d . per annum.
11. $£ 53710 \mathrm{~s}$.
12. $£ 14 \mathrm{~s} .1 \mathrm{~d} . ; £ 20 \mathrm{~s} .1 \mathrm{~d} . ; £ 116 \mathrm{~s} .1 \mathrm{~d}$.
A. (6)
13. $£ 93 \mathrm{~s} .8 \mathrm{~s}$.
P. 501. - 2. $£ 3477$ 2s. 3d.
14. $£ 1110 \mathrm{~s}$.
15. 5s. 6d. (very nearly).
16. He receives $£ 1106$ 13s. 4d., £490, and $£ 3036$ s. 8 d. ; and he loses £840.
17. $£ 26158$.
18. 11s. 11d.
B. (1)

## GEOTION XVIII.

1. 1 ton 5 cwt .1 qr .19 lb .
2. $33.036 \%$.
3. $0.021 \%$.
4. $3.9 \%$.
5. $21.5 \%$.
P. 502. - 6. $0 \cdot 198 \%$ rise ; second date better. 7. 1892-1902 greater by $2.6 \%$.
6. $20.55 \%, 8 \cdot 4 \%, 12 \cdot 15 \%$.
7. $£ 17$ 17s. 6 d .
B. (2)

|  | 1. $0.464 \%$ 2. $65.26 \%$ | 3. $19.7 \%$ (nearly). |  |
| :--- | :--- | :--- | :--- |
| P. 503. | 4. $18.75 \%$ | 5. $28.38 \%$ |  |
|  | 6. (1) $26,039,000$ | (2) $11.62 \%$ | 7. 713.3 dollars. |

B. (3)

1. $0.07391 \%, 0.07347 \%, 0.43668 \%$.
2. $£ 225$ 12s. 10 d .
3. $7 \cdot 49$ dollars.
P. 504. - 4. £717s. duty ; $2.925 \%$
4. 1 s .1 d . 6. $3 \mathrm{~s} .8 \frac{1}{2} \mathrm{~d}$.
5. $28 \%$
6. $14 \%$.
7. $0.0045 \%$ per degree.
8. $1.96 \%$ " A steamer of 3000 tons will convey merchandise from Bilbao (Spain) to Middlesbrough or to West Hartlepool at the rate of 12 s .9 d . a ton, and to the Tyne for 12 s .6 d . per ton in May (1915)."

## C.

SECTION XIX.
P. 504. - 1 .


For complete solution to this question, see Examples LXXIII. (c), No. 21.
P. 505. - 2. (a) §278. (b) See Examples LXXIII. (c), No. 19.
3.


| JOURNAL. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nov. 2.$\text { " } 5 .$ | Goods, $D r$. To Smith \& Co., Cr. Burgess \& Co., Dr. To Goods, Cr. | ¢ 50 50 | 8. 0 0 | d. 0 0 | £ 50 50 | 8. | d. 0 0 |
|  |  | 100 | 0 | 0 | 100 | 0 | 0 |


| Dr. | F. MATHEWS: GAPITAL ACCOUNT. |  |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Nov. 1. | By Cash | ¢ 60 | 8. ${ }_{\text {c }}$ d. |
| Dr. |  | GOODS ACCOUNT. |  |  |  | Cr. |  |
| Nov. 2. <br> " | To Smith \& Co. "Oash . | $\cdot\left\|\begin{array}{c} \pm \\ 50 \\ 25\end{array}\right\|$ | s. d. <br> 0  <br> 0  <br> 0 0 <br> 0  | $\begin{array}{r}\text { Nov. } 4 . \\ \hline " 5 .\end{array}$ | $\underset{\text { By Cush }}{\text { Burgess }}$ \& Co. | ¢ <br> 20 <br> 50 | 8. $\begin{gathered}\text { d. } \\ 0 \\ 0 \\ 0 \\ 0 \\ 0\end{gathered}$ |



| Dr. |  | SMITH \& CO. |  |  |  | Cr. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Nov. 2. | By Goods | \|r | 8. $\begin{aligned} & \text { d. } \\ & 0 \\ & 0 \\ & 0\end{aligned}$ |
| Dr. |  | BURGESS \& CO. |  |  |  | $C r$. |  |
| Nov. 5. | To Goods | $\|$$\pm$ <br> 50 | 8. $\left\|\begin{array}{c}\text { a } \\ 0 \\ 0 \\ -\end{array}\right\|$ | Nov. 6. | By Cash | ${ }_{\text {£ }}^{\substack{10}}$ | 8.a <br> 0 |


| TRIAL BALANCE. |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  | Balances. |  |
|  |  | Dr. | Cr. |
| Capital Account | - • . | \& 8. $d$. | f 8.  <br> $\mathbf{6 0}$ $\mathbf{0}$ d. |
| Goods Account . . | - | ${ }_{5}^{5} 000$ |  |
| Gas, Rent, etc., Account | $\therefore \quad . \quad$ : | 500 | 5000 |
| Burgess \& Co. . . | $\cdots$. | 1000 | 50.0 |
| Cash . - . | . | 9000 |  |
|  |  | 11000 | 11000 |

PART 1I.-6
P. 505.-4.


P. 605.- 5 .


| Dr. |
| :--- |
| Dec. <br> 31 |
| To Balance c/d. |


| Dr. |
| :---: |
| Dee. <br> 31 |
| To Creditors |



P. 505.-6.

| $D r$. |  | DISCOUNT |  |  | ACCOUNT. |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \text { Dec } \\ 31 \end{gathered}$ | To Cash Book | ( $\begin{gathered}\text { ¢ } \\ 2000\end{gathered}$ | 8. | d. 0 | Dec. | By Cash Book ," P. and l. | £ 1500 500 | 8. 0 0 0 | d. 0 0 0 |
|  |  | 9000 | 0 | 0 |  |  | 2000 | 0 | 0 |


| Dr. PREMISES, PLANT, AND MACHINERY. Or. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }_{\substack{\text { Dec } \\ 31}}$ | To Cash |  |  |  |  |  |




| TRIAL BALANCE. |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Balances. |  |  |  |
|  |  |  | Dr. | Cr. |  |  |
| Capital AccountPurchases Account . |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| Sales Account . . . . . . . ${ }^{\text {a }}$ |  |  |  |  |  |  |
| Creditors Account . . . . . . 10000 0 0 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| Discount Account . . . . . . 500000 |  |  |  |  |  |  |
| Premises, Plant, and Machinery . . . 5000000 |  |  |  |  |  |  |
| Trade Expenses . . . . . . 250000 |  |  |  |  |  |  |
| Salaries and Wages . . . . . . 300000 |  |  |  |  |  |  |
| Cash . . . | - . | - - | 16500 0 0 |  |  |  |
|  |  |  | $67500 \quad 0 \quad 0$ | 67500 | 0 | 0 |



6.




P. 505. 6.

|  | DRAWINGS ACCOUNT. <br> Cr. <br>  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |
| $r$. <br> A. TROUP. <br> $C r$. <br>  |  |  |  |  |  |  |




| Dr. |  | E. BA | $C r$. |
| :---: | :---: | :---: | :---: |
| Jan. | To Goods |  |  |


P. 505.- 6 .


P. 508.-7.


The Cash Book and Purchases and Sales Book entries are similar to those of the previous exercises; see $\S \S 171-181$.

## P. 506.-8.





9.

| Item. | Side of |  |
| :---: | :---: | :---: |
|  | Balance Sheet. | Proflt and Loss Account. |
| (1) Profits |  | Credit balance. |
| (8) Liasilities : | Left hand side | Dr. |
| (4) Assets. : | Right ", " |  |
| (6) Capital Expenses Account : | Left " " | Dr. |
| (7) Sinking fund for a lease |  |  |
| (8) Debenture Issue ${ }^{\text {a }}$ | "\#pht" |  |
| (9) Stock at end of period (10) Bills payable . | Reft ${ }_{\text {Right }}$ \# " |  |

P. 506.-10.

P. 506.-10.








| Dr. |  | GOODS ACCOUN'T. |  |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Feb. 1. <br> " 25. <br> , 28. <br> 39 <br> 33 | To Stock <br> " Cash <br> " Purchases Book <br> ", Returns . <br> " Gross Profit | $\left\lvert\, \begin{gathered}\text { e } \\ 5 \\ 50 \\ 70 \\ 110 \\ 20 \\ 50\end{gathered}\right.$ | 8. $d$. <br> 7 0 <br> 8 6 <br> 0 8 <br> 6 8 <br> 10 0 <br>   | Feh. 2. | By Cash ," Sales Book ", Stock. | £ 81 352 339 | 8.  <br>  $d$ <br> 6 0 <br> 16 0 <br> 19 10 |
|  |  |  | 110 |  |  | 774 | 110 |
| Mar. 1. | To Stock |  | 1910 |  |  |  |  |









Sec. xix]
ANSWERS
P. 506.- 10 .

| Dr. |  | W. STOTT. |  |  | $C r$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\text { Feb. } 1 .$ | To Balance . , Goods | $\begin{aligned} & 5 \\ & 59 \\ & 62 \end{aligned}$ | s.s.  <br> 5  <br> 12 6 <br> 12 8 <br>   | Feb. 1. | By Bill Receivable \# Returns " Balance c/d . | 5 <br> 59 <br> 20 <br> 42 <br> 4 | 8. $d$. <br> 5 6 <br> 6 8 <br> 6 0 |
| Mar. 1. | To Balance b/d | $\frac{121}{42}$ | 18 2 <br> 6 0 |  |  |  | $18-2$ |



P. 507.-11.


P. 507.- 12. The Cash Book is shown ou opposite page.

P. 507.-12.

P. 507.-12.


| $D r$. | J. ELGOOD : CAPITAL ACCOUNT. |  |  | $C r$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Jan. 1. | By Bank . | $\|$E <br> 1000 |  |


| Dr. | J. JONES. |  |  |  | $C r$. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. 16. <br> Fe"b. 20. <br> " 21 | To Goods <br> " Interest. <br> ,, Bill Receivable <br> " Interest | £ ${ }_{\text {c }}$ \|d. | Jan. 16. Feb. 21. Mar. 22. | By Bill Receivable <br> ,, Bank <br> ", Bill Receivable | $\pm$ |
|  |  | 70000 |  |  | 70310 |
|  |  | 3100 |  |  | 30513 |
|  |  | $70313{ }^{13}$ |  |  | 400 |
|  |  | 200 |  |  |  |
|  |  | 40936 |  |  | 14093 |


| Dr. |  | J. DAY. |  |  |  | Cr. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\|\begin{array}{cc} \text { Jan. } & 15 . \\ " & " \end{array}\right\|$ | To Bank ," Discount | $\begin{array}{\|c} £ \\ 555 \\ 29 \end{array}$ | 8.  <br> 1.  <br> 5 0 <br> 5 0 | Jan. 4. | By Goods | ${ }_{585}^{\text {¢ }}$ | 8. | a |
|  |  | 585 | 0 |  |  | 585 | 0 | 0 |



| $D r$. |  | BILLS RECEIVABLE. |  |  |  |  | Cr. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\|\begin{array}{r} \text { Jan. } 16 . \\ " \\ 21 . \end{array}\right\|$ | To J. Jones ." | - $\left\lvert\, \begin{gathered} \pm \\ 703 \\ 400 \\ 40\end{gathered}\right.$ | $8 . \mid$ d. <br> 10 0 <br> 0  <br> 0  | Feb. 20. | By J. Jones." Bank |  | 8 <br> 708 <br> 400 <br> 1 | 8.  <br> 10 $d$ <br> 0  <br> 0  <br> 0  |
|  |  | 1103 | 10. |  |  |  | 1109 | 10 |

P. 507.-12.

D. (1)

## SECTION XX.

P. 508. - 1. 14s. 9d.
4. $£ 1391$ 198. 6 d .
6. $£ 166$ 16s. 3d. ; $£ 157$ 1s. 8 d .
9. $£ 4000 @ 5 \%$.
D. (2)
P. 509. - 1. $£ 630$ 168. 4 d .
4. $£ 54$ 6s. 5 d .
6. $£ 82$.
9. $£ 1807$ 1s. 11 d . part il.一 7
8. $£ 816 \mathrm{~s} .8 \mathrm{~d}$.
2. $£ 500$.
5. $£ 175$ 5s. 6 d .
2. $£ 52$ 10s. bd. ; § 322.
3. $£ 1044 \mathrm{~s} .9 \mathrm{~d}$.
5. 41930 francs (correct to 10 francs).
7. $£ 5845 \mathrm{~s} .7 \mathrm{~d}$.
8. $£ 4418 \mathrm{~s}$. 1 d .
10. $£ 200$.
3. £194 4s. 8d.
7. $374 \cdot 8$ francs (Simple Interest).
E. (1)

## SECTION XXI.

P. 509. - 1. 17s. 7 d . ..... 2. $10 \frac{1}{2} d$.P. 510. - 3. $12 \frac{1}{2} \%$. 4. $£ 48719 \mathrm{~s} .9 \mathrm{~d} . ; £ 28814 \mathrm{~s} .5 \mathrm{~d} . ; £ 5559 \mathrm{~s} .3 \mathrm{~d} . ; £ 2607 \mathrm{~s}$.5. $£ 2$ 2s. 6d.6. 7add. (very nearly).7. 14s. sl .8. $100 \%$.

1. 53246.6 roubles (currect to $\frac{1}{1}^{1} 9$ ronble). 2. 54 ' 75 ronbles.
2. $£ 743 \mathrm{l5s}$. 4. $5 \cdot 128 \%$
3. $2.5 \%$ (uearly).
P. 511. - 6. (a) £4500. (b) £4495. 7. £646 12s. 11d, 8. £618 9s. 10 d.
4. £1 3s. 3d. 10. $£ 9.111 \mathrm{~s}$. 9 d. 11. 123480 francs. 12. $5.703 \%$.
F. (1)

## SECTION XXII.

P. 512. - 1. $£ 20125$.
2. Mexican ( $£ 93 \mathrm{~s}$.) ; Consuls ( $£ 31 \mathrm{Ts}$.). Put it into Consols, for tho Mexican is more risky.
3. $£ 198$ 19s. 2 ll .
4. $£ 8218 \mathrm{~s}$.
5. (a) $£ 5$ 7s. \%.
(b) £135 0s. 6d., i.c. £135.
(c) $£ 318 \mathrm{~s} . \mathrm{tin} . \%$.
6. £6 3s. ld. 7. £т 1 !s. 10 .
8. $£+15 \mathrm{~s} .3 \mathrm{~d} . \%$.
9. $52.5 \%$.
10. $£ 64 \mathrm{~s} .5 \mathrm{~d} . \%$.
11. $£ 50$.

1. $£ 1600$ serip ; $3.317 \%$.
P. 513. - 2. £37 3s. 2d. (nearly).
2. Incomes are-
(1)
(2)
£34 20
2160
3. $£ 232$.
4. $£ 685$.
5. $£ 95$.
6. $£ 15 ; 1 \cdot 6 \%$.
7. $566 \cdot 25$ franes; $4944 \cdot 8$ franes; $773 \cdot 25 \%$.
8. £27000, £30000, £109375; Income tax 3 jo 0 Net - $£ 5230$
17.5\%.
9. $£ 1573$ (nearly) ; first income, $£ 98$ 10s.; second income, $£ 397 \mathrm{~s}$. (correct to 1s.).

## DATE OF ISSUE

This brook munt lw riturnedi
within 3, 7, 14 days of its issue. A
fine of $0 . N \mathrm{ANNA}$ fer day will the charged if the book in ovordias.



[^0]:    ${ }^{1}$ Some "drill" examples and a few problems liave been taken from examination papers set by the following authorities, to whom we tender our acknowledgments: The Lancashire and Cheshire Union of Institutes, the Society of Arts, the Institute of Chartered Accountants, the Chartered Institute of Secretaries, the London Chamber of Commerce, the Chartered Accountants of Scotland, and the Institute of Bankers.

[^1]:    ${ }^{1}$ The student should not content himself with performing the experiment once, but should do it at least three times and take the average of the results. These remarks apply equally to succeeding experiments of a similar character.
    ${ }^{2}$ If one student makes one vessel, another the second, and so on, at home, the experiment can be performed very readily before the class.
    ${ }^{8}$ Experiment 4 and Questions 14 to 16 can be repeated using a centimetre cube and vessels-(1) $3 \times 3 \times 3 \mathrm{~cm}$.; (2) $8 \times 2 \frac{1}{\mathrm{t}} \times 2 \frac{1}{\mathrm{t}} \mathrm{cm}$.; (8) $4 \frac{1}{2} \times 4 \times 3 \frac{1}{\mathrm{~g}}$ cm . ; (4) $5 \times 4 \times 1 \frac{1}{\mathrm{~cm}}$.

[^2]:    ${ }^{1}$ Note the total surface area of a cylinder = area of the curved surface + area of the two ends $=$ circumference $\times$ height $+\pi r^{2}+\pi r^{2}=2 \pi r h+2 \pi r^{2}$.

[^3]:    ${ }^{1}$ The student should be very careful to write down the units in which the answer to a question is expressed, e.g.:
    Lengths are expressed in miles, yards, feet, metres, centimetres, millimetres; Areas " " SQUǍE Miles, SQUARE Metres, etc., and Volumes " ", CUBIC ", CUBIC ", and he should not multiply feet by inches or by yards, but reduce all measurements to the same units before working the sum.

[^4]:    ${ }^{1}$ It is to be observed that we employ the term "weight" in its usually accepted commercial sense, and consequently do not discriminate between mass and weight.
    ${ }^{2}$ The student can easily find the weight of 1 cubic inch of pordered chalk, etc., by taking an inch cube, placing it in the left-hand pan of a balance, and counterpoising it with fine sand, and then filling up the cube with the chalk and weighing it in grains. Several cubes would be wanted for a set of experiments, and mercury being costly should be kept carefully and not thrown down the drain, for it would destroy the lead pipes. In just the same way we could determine the weight of a pint of water and of a pint of (say) methylated spirit, and so find rovahly the specific gravity of the spirit or of any liquid.

[^5]:    ${ }^{1}$ That is iron rods or bars embedded in concrete.
    ${ }^{2}$ Squared timber is timber which is roughly squared off, while rough timber has not been treated in this way.
    ${ }^{2}$ See Question 38, p. 309.

[^6]:    ${ }^{1}$ See $\S 97$ for the monetary systems of various countries.
    ${ }^{2}$ Bronze is not legal tender for amounts over 1 s ., nor is silver fot amounts over $£ 2$.

[^7]:    ${ }^{1}$ See footnote, page 320.
    ${ }^{2}$ The Government is encouraging rubber planting by offering "bounties" just as the Queensland Government is doing with sugar,

[^8]:    ${ }^{1}$ See Question 28, page 292.

[^9]:    ${ }^{1}$ An inquiry into ancient and modern methods of measuring time would prove most interesting to the student. The abysmal depths of the starlit skies of the south of Europe appealed to the imagination of the ancients, and many astronomical facts were known to them. Galileo is said to have used his "pulse" as a time-measurer when he observed the steady swinging of a lamp in the great cathedral at Pisa. In our own country King Alfred is said to have measured time by means of candles, which subsequently gave place to hour glasses, and pocket watches, early specimens of which are to be seen in the British Museum, were introduced in 1577. From a literary standpoint, Shakspere often refers to a clock or to a watch, e.g. "The moon is down ; I have not heard the clock" (Macbeth); "He's winding up the watch of his wit, presently it will strike" (T'empest); while Sir Thomas Browne speaks of "Time, which antiquates antiquities and hath an art to destroy all things."

    We mention these facts to direct the student's thoughts into the domain of antiquity, of history, and of literature, so that his mind may be able to expatiate in realms other than that of commerce.

[^10]:    : This is the average rate of wages in Queensland. See Queensland Year Book, p. 171.
    ${ }^{2}$ Rotterdam time, see § 215.

[^11]:    ${ }^{1}$ Page 162, note 2.

[^12]:    ${ }^{1}$ If the merchant had put his watch to agree with the local time in Venice, he would have moved the hands 48 minutes.
    'This was constructed by Giovan' Paolo Rinaldi. Two "Moors" in bronze strike the hours. Compare with the clock in old St. Dunstan's Church, London, and the one at Hampton Court Palace.

[^13]:    ${ }^{1}$ The attention of the student is drawn to the fact that the Suez Canal route is shorter for steamers from Liverpool to the chief ports of Australia as well as to Tientsin and Yokohama, while the Panama route is the shorter to New Zealand.

[^14]:    ${ }^{1}$ On the Atlantic side of the Panama Canal.
    ${ }^{2}$ The largest port on the Pacific coast of South America.
    ${ }^{3}$ See $\S 8218$ and 219.

[^15]:    ${ }^{1}$ Radiator tubes are usually black, because the amount of heat radiated from a black surface is greater than that radiated from a white, bright, or poloured surface,

[^16]:    ${ }^{1}$ A Diesel engine is an internal combustion engine-that is to say, it resembles a motor-car angine rather than a loconotive. Veiy cheap crude oil can be used as fuel, and the explosion is produced by the heat generated un compression.

[^17]:    ${ }^{1}$ My watch gave me originally Greenwich time, not Holyhead local time, for Holyhead is $4^{\circ} 48^{\prime}$ west, and is therefore earlier than Greenwich.

[^18]:    ${ }^{2}$ Note that $£ 5000$ lent for $\mathbf{6}$ months is not equivalent to $£ 5000 \div 6$ for 1 month, as many students imagine.

[^19]:    ${ }^{1}$ With acknowledgments to Brazil, J. C. Oakenful.

[^20]:    ${ }^{1}$ See B. (3) for full explanation ; here, simply deduct 2 s . 2d. in the pound on five-sixths of gross rental.

[^21]:    ${ }^{1}$ The merchant pays his landlord $£ 85$ a year in rent, therefore the landlord must pay income-tax on the $£ 85$. But the State demands the tax from the tenant (and so makes sure of it), who may deduct it from the first rent paid after the tax has been paid by him. The landlord may be fined if he refuses to allow the amount of the tax, but he need not allow it unless it is deducted from the first rent paid after the date of the receipt.

[^22]:    ${ }^{1}$ It may be necessary to read $\$ 266$ and 267 on Percentages before working through this section.

[^23]:    ${ }^{1}$ An insurance company may receive as much as $£ 1,000,000$ a year in premium income. It will invest this money and make a considerable profit. If it be a Mutual Office, then those who hold "with profit" policies will share this profit between them. If, however, it is a Company Offioe then the shareholders may take half the profit and what remains will be divided. The bonus is usually declared quinquennially. In one office, at least, it amounted to $£ 22$ s. per cent. per annum.

[^24]:    ${ }^{1}$ See Thomas Hardy, The Mayor of Casterbridge.
    ${ }^{2}$ Provided the amount due by you is over $£ 50$. If, however, you owed - £95, and had given the creditor security for $£ 55$, he could not proceed against you in this way for the "unsecured" part of the debt, which is only £40. If the "secured" part were $£ 30$, then he could get a receiving order on the ground that the "unsecured" part exceeded $£ 50$.
    ${ }^{\mathbf{a}}$ A bankruptoy petition has to bear a $£ 5$ stamp, and $£ 5$ must be do. posited to cover the preliminary expenses,

[^25]:    ${ }^{1}$ The Receiving Order usually reads as follows (where John Wilson is your oreditor, and you, Henry Jones, are the debtor) :
    "On the petition of John Wilson, a creditor, filed the 10th day of March, and on reading the affidavit* of John Wilson and it appearing to the Court that the following act of bankruptcy has been comnitted, namely, that John Wilson having obtained final judgment against Henry Jones for $£ 140$ and costs on 8th February, and a bankruptcy notice having been duly served on him requiring him to pay the same, the said Henry Jonea having failed to do so, a receiving order is hereby made against Henry Jones, and the Official Receiver is hereby constituted receiver of the estate."
    ${ }^{2}$ The creditors might refuse to agree to any arrangement if they felt it to be imperative that you should be made a bsnkrupt to prevent your trad. ing any more in your own name. For example, if you had borrowed money from a money-lender and had not paid him, he would almost certainly make you a bunkrupt ; or, if you had behaved discreditably, the same course might be followed hy creditors in general.

[^26]:    *The affidavit is called "Proof of Debt" and requires Is. stamp for debts over \&s.

[^27]:    ${ }^{1}$ See Part III.
    2 Wolfram is the heavy ore from which the metal tungsten is obtained. The latter is used, in one form, for fireproofing fabrics, as a dye and as a pigment, while the metal is used to harden steel.

[^28]:    ${ }^{1}$ Decrease cansed partly by export restrictions and partly by diminished area of cultivation and dearth of ploughing animals.
    ${ }^{2}$ Brazil exported about two-thirds of the world's production of coffee anterior to 1888, but in that year slavery was abolished in the country, and a consequent upheaval in the labour system followed. The smallest amount exported since 1900 has been 584 million Kilograms.

[^29]:    ${ }^{2}$ Page 483.
    ${ }^{2}$ The camphor produced in Japan Proper is mostly sold in the home market, while the Formosan product has a large market in Europe and in America.

[^30]:    ${ }^{1}$ In a large firm there is a room set apart for keeping the Ledgers, and is called a Counting-House. There is a Ledger clerk and often two or three assistants on each Ledger, which contains (e.g.) the names of customers who have Credit Accounts and which begin with A or B or C, ete. Thus there may be a large number of Ledgers. If then a customer comes in and wants credit, the assistant may phone up to the " E Ledger" and ask if that credit may be allowed. The desk at which the clerks sit is separated off by a glazed partition from other desks, hence we hear of "A Alley" or "R Alley," that is, the place where the A or $R$ Ledger clerk reigns supreme, Over and above the Ledger clerk is the Qounting-House manager.

[^31]:    ${ }^{1}$ The student may get confused as to Cash Account or Bank Account and Cash Book. By Cash Account we mean the account as it appears in the Cash Columns of the Cash Book, and by Bank Account the account as it appears in the Banf Columns of the Casß Book,

[^32]:    ${ }^{1}$ In all purchases or sales if you decide upon which side of the Cash Book the Cash Entry must fall (receipts Dr., payments Cr.), then the second entry MUS'T fall on the opposite side of the particular Nominal Account concerned.

[^33]:    ${ }^{1}$ The balance as it appears in the model Ledger is $£ 239$; that is becanse we have there transferred the net profit to Capital Account, but are asking you to make the Trial Balance before doing that. There will be no difficulty, however, if you have done as we asked you to do on p. 414, § 281 , I.

[^34]:    ${ }^{1}$ Here again the variations in type serve to connect the items with the corresponding entries in the Model Ledger.

[^35]:    ${ }^{1}$ Note that we are posting from H. J.'s Purchases Book, which contains details of his purchases from other people who are therefore his Creditors.

[^36]:    1 The numbers (1), (2), etc., in this section refer to the corresponding small numbers, (1), (2), etc., in § 298.

[^37]:    ${ }^{1}$ The numbers give the pages in the Ledger on which these entries are posted.

[^38]:    ${ }^{1} £ 228=$ total of entries immediately below.
    ${ }^{2}$ The difference between $£ 275$ and $£ 228$,

[^39]:    ${ }^{1}$ The numbers refer to pages in Subsidiary Books

[^40]:    ${ }^{1}$ An Internal Loan is raised if and when a Government, e.g. the Swiss Goverument, asks the inhabitants of the country (Switzerland) to subscribe it. A Forergn Loan is one which is raised by appealing to foreign bankers and nations.
    ${ }^{2}$ Look out for leap years in questions such as these (§ 216).
    ${ }^{8}$ If $x^{\prime} 1$ is put in on 30th or 31st January and remains in till 28th February no interest is paid. If it remains till the morning of 1st March, interest is paid. Deposited 16th January, drawn out 15 th February, no interest paid. Deposited 28th February, drawn out 1st April, interest is paid.

[^41]:    ${ }^{1}$ Not more than $£ 50$ can be deposited in any year, but if $£ 70$ has been withdrawn in any one year in one sum, all of it may be replaced regardless of the $£ 50$ limit. During the war the "limit" could be exceeded.

[^42]:    ${ }^{1}$ See § 818. The Post Office pays Compound Interest, but Banks in. general "throw out" the interest periodically.

[^43]:    ${ }^{2}$ Blank Bills of Exchange can be purchased from Law Stationers.
    ${ }^{2}$ The value of the stamp on a Bill of Exchange depends on the amount for which it is drawn and on the time before it is due; it ranges from 1d. for amounts under $£ 5$ to 1s. for $£ 100$, and so on. (See Whitaker's Almanack, "Bills of Exchange, Stamp on.")

[^44]:    ${ }^{1}$ Bills due on Sunday are payable on the previous Saturday, and those due on Bank Holidays the day atter.
    ${ }^{2}$ Foreign Bills of Exchange are drawn in London and are payable abroad, or vice versa. It is necessary to draft such a bill "at sight," or "on demand," as in the case of an inland bill, or at 30,60 , or " 90 days' sight," which means that it must be honoured 30, 60, or 90 days after it has been accepted and not after it has been drawn. The necessity of this is obvious, for a creditor in South Africa cannot "accept" a bill drawn in London until the mail arrives and he catches "sight" of it, whereupon he "accepts" it and meets it in due course.
    ${ }^{8}$ For value of stamp necessary see Whitaker's Almanack.

[^45]:    ${ }^{1}$ Some of the great bankers are bill-brokers as well as bankers.
    ${ }^{2}$ See Merchant of Verice, Act I. Sc. 3, 11. 10-12, "Antonio is a 'good'man."

[^46]:    ${ }^{1}$ One of the commonest illustrations of the difference between "face value" and "cash value" is the case of tickets for an opera or a theatre. A ticket for the pit is often sold at 2 s .6 d ., but as time goes on and all the tickets are sold, people are prepared to pay 7 s . or 10 s . for a pit ticket rather than miss the performance. Thus the face value is 2 s .6 d . and the cash value 7 s .

[^47]:    ${ }^{1}$ See § 363.
    ${ }^{2}$ A Bond is a legally binding promise, made by a Government or company, to repay the amount of a loan at a particular time. One class is called a "Bond to Bearer," to which coupons are attached, so that when the dividend is due the holder simply tears off the proper coupon and pre. sents it at the Bank for payment.

[^48]:    ${ }^{1}$ Look in the newspapers to-day and find the price of the various stocks, and so determine whether it has risen or fallen since this paragraph was written.

[^49]:    ${ }^{1}$ A broker is an intermediary who brings the public into touch with the Jobber who does the actual buying and selling. The student should note that the term "Jobber" is not a vulgarism, but a name applied to a class of business men who are members of the Stock Exchange, and who are not even allowed to advertise in order to get business.

    2 We shall not here consider the Causes of these fluctuations.

[^50]:    ${ }^{1}$ Now only $£ 210 \mathrm{~s}$. is paid.
    ${ }^{2}$ Pronounced something like raunt (cf. flaunt) and not at all like our English word "rent."

[^51]:    ${ }^{1}$ If more than twenty men are involved in the partnership it must be registered.
    ${ }^{2}$ Section XVII. B (1).

[^52]:    ${ }^{1}$ § 358.
    ${ }^{2}$ Sometimes the whole face value of the vouchers is not paid at once, for the directors might not want more than $£ 80000$ for a year or so, and of that amount only, say, $£ 50000$ to begin with, and so they would ask each shareholder to pay $f 5, £ 210 \mathrm{~s}$., or 10 s. per share as the case may be, and then we should say : Authorised or Nominal Capital, £100000; Subscribed, or Issued Capital, £ 80000 ; Paid-up Capital, $£ 50000$. In Whitaker's Almanack, p. 356, we find that one of the largest Banks has an Authorised Capital of $£ 26,000,000$, but a Paid-up Capital of only $£ 4,000,000$.

[^53]:    ${ }^{1}$ Tea merchants often have large stocks for customers, and they always hold them covered against fire.

[^54]:    ${ }^{1}$ This wood is said to have been brought to England first by Sir Walter Baleigh in 1595.

[^55]:    ${ }^{1}$ \& 388. See Plate XIII., p. 468.
    ${ }^{2}$ The lowest expenditure since 1902 was in 1905, namely, £2087, and the highest was in 1913.

[^56]:    ${ }^{1}$ In thinking of India think of the British Government's supreme achieve ment-irrigation.

[^57]:    ${ }^{1}$ See page 480, note 2.

[^58]:    ${ }^{1}$ Ignore Brokerage unless expressly told to allow it.

