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Abbreviations

amb	Ambient
C	Compressor
CFD	Computational fluid dynamics
COP	Coefficient of performance
COND	Condenser
CP	Critical point
CTRC	Conventional R-744 transcritical refrigeration cycle
E	Effectiveness
EJE	Ejector
EETRC	Ejector expansion R-744 transcritical refrigeration cycle
EETRC+IHX	Ejector expansion R-744 transcritical refrigeration cycle with internal heat exchanger
EVAP	Evaporator
EXP	Expansion / control valve
F	Total interfacial force (N)
g	Acceleration due to gravity (m/s^2)
GC	Gas cooler
GWP	Global Warming Potential
HEM	Homogeneous equilibrium model
HRM	Homogeneous relaxation model
IC	Intercooler
IHX	Internal heat exchanger
LTE	Lower temperature evaporator
M	Mass flow rate, kg/s
MToe	Million or mega tonnes of oil equivalent

MTCO2e	Million tonnes of carbon dioxide equivalents
MTE	Medium temperature evaporator
MCEETRC+IHX	Multi compressor ejector expansion R-744 transcritical refrigeration cycle with internal heat exchanger
MCMIEETRC	Multi compressor multi-intercooler ejector expansion R-744 transcritical refrigeration cycle
ODP	Ozone Depletion Potential
PR	Pressure recovery
PRR	Pressure recovery ratio
SNPD	Suction nozzle pressure drop
U	Entrainment ratio
x	Vapour quality
W	Specific work (kJ/kg)
TEWI	Total equivalent warming impact
TWh	Trillion Watt hour