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Abbreviations

PDF:	Probability density function
JIT:	Just-in-time
GoS:	Grade-of-service
OR:	Operations research
IT:	Information technology
PSO:	Particle swarm optimization
CS:	Cuckoo search
BA:	Bat algorithm
QN:	Quasi-Newton
DS:	Direct search
GA:	Genetic algorithm
DE:	Differential evolution
FA:	Firefly algorithm
CTMC:	Continuous-time Markov chain
FCFS:	First come first served
QBD:	Quasi-birth and death
MTTF:	Mean-time-to-failure
SOR:	Successive over relaxation
MRP:	Machine repair problem
BV:	Bernoulli vacation
SV:	Single vacation
MV:	Multiple vacation
WV:	Working vacation
MWV:	Multiple working vacation
SWV:	Single working vacation
VI:	Vacation interruption